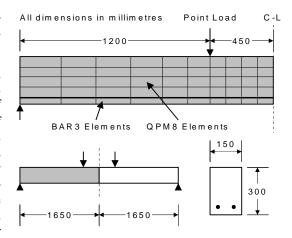
Nonlinear Analysis of a Concrete Beam

For LUSAS version:	19.0
For software product:	Any Plus version. Bridge Plus version for the modelling
	described in the discussion at the end.
With product options:	Nonlinear.

Description

A nonlinear plane stress analysis is to be carried out on a model of a reinforced concrete beam.

The reinforcement is provided in the lower face of the beam and has a total cross-sectional area of 400 mm². The superposition of nodal degrees of freedom assumes that the concrete reinforcement are perfectly bonded. It is assumed that the selfweight of the beam is negligible compared with the applied load and that the effects of any shear reinforcement can be ignored.



Due to the symmetrical nature of the problem, only the left-hand span of the beam is modelled. The beam is simply supported at the left-hand end with a symmetry support at the right-hand axis of symmetry. A concentrated vertical load is applied to the top of the beam 1200mm from the left-hand end. The concrete section is represented by plane stress (QPM8) elements, and the reinforcement bars are represented by bar (BAR3) elements. A nonlinear concrete cracking material model will be applied to the plane stress elements and a von Mises plastic material will be applied to the reinforcement bars.

Units of N, mm, t, s, C are used throughout.

Objectives

The behaviour of the beam under cracking/yielding is to be examined by producing the following:

A Deformed Mesh Plot showing the final deformed shape.
A Load Displacement Graph for the top node on the axis of symmetry of the beam.
Stress contour plot showing the stress distribution in the beam.
Crack pattern plot showing the crack patterns produced.
Animation of stresses and crack patterns for selected load increments.
A graph of variation in stress through selected slice sections through the beam.

Keywords

2D, Inplane, Plane Stress, Bar Elements, Nonlinear Concrete Model, Element Selection, Concrete Cracking, Steel Reinforcement, Groups, Crack Patterns, Animation, Graphing, Load Displacement Curve, Slice Sections

Associated Files



□ **beam_nl_modelling.vbs** carries out the modelling of the example.

Modelling

Running LUSAS Modeller

For details of how to run LUSAS Modeller, see the heading *Running LUSAS Modeller* in the *Introduction to LUSAS Worked Examples* document.



Note. This example is written assuming a new LUSAS Modeller session has been started. If continuing from an existing Modeller session select the menu command **File>New** to start a new model file. Modeller will prompt for any unsaved data and display the New Model dialog.

Creating a new model

• Enter a File name of beam nl

- Use the default User-defined working folder.
- Ensure an Analysis type of **Structural** is set.
- Select an Analysis Category of 2D Inplane
- Set Model units of N,mm,t,s,C
- Leave the Timescale units as **Seconds**
- Select a Startup template of **2D Plane Stress**.
- Ensure the Layout grid is set as None
- Enter a Title of Nonlinear Concrete Beam
- Click the **OK** button.

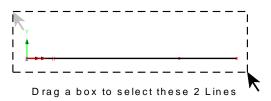


Note. Save the model regularly as the example progresses. Use the Undo button to correct any mistakes made since the last save was done.

Defining the Geometry

| Ceometry | Line | > | By Coords...

Enter coordinates of (0, 0), (1200, 0) and (1650, 0) to define two Lines representing the bottom of the left hand span of the beam. Click the **OK** button to finish.

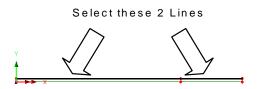


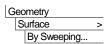
 Select both Lines just drawn by dragging a selection box around them.

Geometry
Surface >
By Sweeping...

Enter a translation value of 25 in the Y direction to create the Surface which represents the concrete cover from the face of the beam to the centreline of the reinforcement.

- Click the **OK** button.
- Select the upper Lines of both of the Surfaces just drawn as shown.





Enter a translation value of **275** in the **Y** direction to create the Surface which represents the extent of the concrete above the centreline of the reinforcement.

• Click the **OK** button.

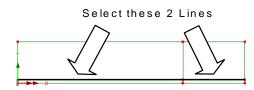
The model should appear as shown.



Defining Groups

To simplify the assignment of model attributes certain model features will be grouped together to allow selection by name in the Treeview as opposed to selection by cursor in the graphics window. The 2 Lines representing the reinforcement bars are to be grouped together:

• Ensure the 2 Lines are still selected as shown.



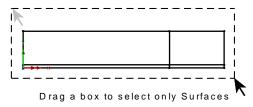
Geometry
Group >

Enter **Bars** for the group name.

 Click the **OK** button to complete creation of the group.

The Surfaces representing the concrete are to be grouped together.

 Holding-down the S key, (and noting that the cursor changes to show the type of feature that will be selected) drag a box around the whole model to select only the <u>Surfaces</u> defining the concrete.



Geometry
Group >
New Group

Enter **Concrete** for the group name. Click the **OK** button to complete creation of the group.

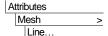


Note. In this example, model attributes will be defined but not assigned to the model straight away. They will be assigned to the model later by making use of the Groups facility.

Defining the Mesh Reinforcement Bars

Separate mesh datasets need to be defined for the reinforcement bars and the concrete. For the reinforcement bars a uniform mesh is to be used to the right of the applied load and a graded mesh is to be used on the horizontal lines to the left of the applied load.

The reinforcement bars will be modelled using Line meshes.



- Set Generic element type to **Bar** and Interpolation order to **Quadratic**
- Ensure the Number of divisions is set to 4
- Enter the attribute name as **Bar**, **quadratic order**, **divs** = **4**
- Click the Apply button to create the attribute in the Treeview and leave the dialog visible to allow additional datasets to be defined.
- Change the **Number of divisions** to **6** and click the **Spacing** button.
- Select a **Uniform transition** ratio of first to last element of **2** and click **OK**
- Change the attribute name to **Bar**, **quadratic order**, **divs** = **6 graded**
- Click the **OK** button to finish to add the attribute to the A Treeview.

Defining the Mesh Concrete

The concrete will be modelled using a Surface mesh with Line mesh divisions to control the mesh density..



- Select Plane stress, Quadrilateral, Quadratic elements.
- Enter the attribute name as **Plane stress quadratic**
- Click the OK button to add the attribute to the Treeview.

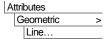
The default mesh density of 4 divisions per line is sufficient for the Surface to the right of the applied load. A graded line mesh will be created for use on the Surface to the left of the applied load.

• In the A Treeview double click the Line mesh attribute name Bar, quadratic order, divs = 6 graded

The Line mesh properties dialog will appear.

- Change the element type to **None**
- Change the attribute name to Null, divs=6 graded
- Click the **OK** button to add the attribute to the A Treeview.

Defining the Geometric Properties



- Select Bar from the drop down list and enter a value of 400 for the total cross sectional area of the reinforcement.
- Enter the attribute name as **Steel Area** and click the **OK** button to add the attribute to the Treeview.

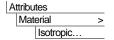


- Enter a value of **150** for the thickness. Leave the eccentricity blank.
- Enter the attribute name as **Beam Thickness** and click the **OK** button to add the attribute to the Treeview.

Defining the Material Properties

Steel

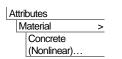
Nonlinear steel properties will be defined for the reinforcing bar elements.



- Enter Young's modulus as **210e3** and Poisson's ratio as **0.3** and leave the mass density field blank.
- Click the Plastic option and enter an Initial uniaxial yield stress of 300
- Select the **Hardening** option, click the **Hardening gradient** button and enter a hardening **Slope** value of **2121** with a **Plastic strain** of **1**
- Enter the attribute name as Nonlinear Steel
- Click the **OK** button to add the attribute to the & Treeview.

Concrete

Nonlinear concrete material properties will be defined for the Surface elements representing the concrete.



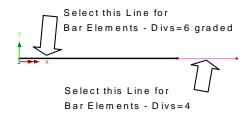
- Ensure the concrete model **Smoothed multi-crack** (model 109) is selected.
- Ensure that Creep model code **None** is selected.
- Ensure that Shrinkage model code **None** is selected.
- Enter a Young's modulus of **42000**, a Poisson's ratio of 0.2 and leave the mass density field blank.
- Enter a Uniaxial compressive strength value of 31.58
- Enter a Uniaxial tensile strength value of **3.158**

- Leave the Strain at peak uniaxial compression as the default value.
- Select the Strain at end of softening curve radio button, and set the value to be 0.003 and press OK to return.
- Enter the attribute name as Nonlinear Concrete
- Click the **OK** button to add the attribute to the A Treeview.

Assigning Attributes to the Bars

The various Line and Surface mesh, geometric and material attributes defined previously will now be assigned to the model using the groups that have been defined.

- In the Treeview right-click the group name **Bars**. Select the **Set as Only Visible** option. The features in the group will be displayed.
- Select the left hand Line of the two Lines representing the bars.
- Drag and drop the Line mesh attribute Bar, quadratic order, divs
 = 6 graded from the Treeview onto the selected Line.



- Select the right hand Line of the two Lines representing the bars.
- Drag and drop the Line mesh attribute **Bar**, **quadratic order**, **divs** = **4** from the Treeview onto the selected Line.
- In the Treeview double-click on the Mesh entry and select Show nodes.



The Line mesh divisions will be seen defined with the spacing as shown.

- Select both Lines.
- Drag and drop the geometric attribute **Steel Area** from the Area from the Treeview onto the selected features. Click **OK**.
- Drag and drop the material attribute **Nonlinear Steel** from the A Treeview onto the selected features. Click **OK**.



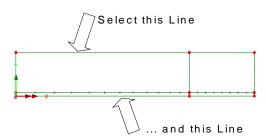
Note. The diagrams in this example show element nodes. To see these at any time you can go to the Treeview and double-click the **Mesh** layer. On the Mesh tab select **Show nodes** and click the **Close** button.

Assigning Attributes to the Concrete

• In the Treeview right-click the group name Concrete. Select the Set as Only Visible option.

The Lines in the Bars group will be made invisible and the lines of the Concrete group will be made visible.

- Select the left-top and leftbottom Lines as shown. (Hold the **Shift** key down after selecting the first line)
- From the Treeview drag and drop the Line mesh attribute
 Null, div=6 graded onto the selected features.



- Select the whole model using the **Ctrl** and **A** keys together.
- Drag and drop the Surface mesh attribute Plane stress quadratic from the Treeview onto the selected features.

A graded mesh will be drawn on the left-hand Surface and a uniform mesh will be drawn on the right-hand Surface.

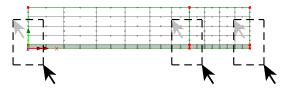


• Drag and drop the geometry attribute **Beam Thickness** from the A Treeview onto the selected features. Click **OK**.

Select the fleshing on/off button to turn-off the geometric visualisation. If at any time during the example you wish to visualise the geometry select this button.

The mesh on the Lines representing the cover to the centreline of the reinforcement needs to be altered. This is because they currently have a default Line mesh of 4 divisions per line when only 1 division per line is required.

• Drag boxes to select the 3 Lines as shown. (Remember to hold the **Shift** key down after the first line is selected so the other lines are added to the selection)



Drag 3 boxes to select these 3 Lines

Drag and drop the Line mesh attribute Null, div =1 from the Treeview onto the selected Lines.

The mesh will be redisplayed with the revised mesh pattern.

Making all groups visible

• From the Treeview right-click the group heading name **beam_nl.mdl**. Select the **Set as Only Visible** option. Click **Yes** to act on sub groups as well.

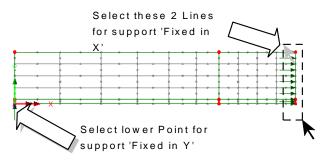
All features in the model will now be displayed as shown.



Supports

When using the Standard template, LUSAS provides the more common types of support by default. These can be seen in the Treeview. The beam is to be simply supported in the Y direction at the left-hand end and a horizontal restraint in the X direction is required to satisfy the symmetry requirements at mid-span.

- Select the lowest Point at the left hand end of the model as shown.
- Drag and drop the support attribute
 Fixed in Y from the
 Treeview onto the selected Point. Ensure the Assign to points



and All analysis loadcases options are selected and click OK

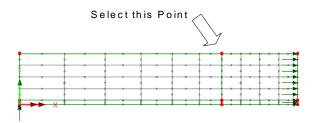
- Drag a box around the 2 Lines at the right hand end of the model as shown.
- Drag and drop the support attribute **Fixed in X** from the Treeview onto the selected Lines. Ensure the **Assign to lines** and **All analysis loadcases** options are selected and click **OK**

Loading

A single concentrated load is to be applied to the Point at the top of the beam. A unit load will be applied and the load factor in the nonlinear control will be used to control the magnitude of loading.

Attributes Loading...

- With the Concentrated option selected click Next
- Enter a Concentrated load in Y Dir loading value of -1
- Enter the attribute name as **Point Load** and click **Finish**
- Select the Point on the top of the beam as shown.
- Drag and drop the loading dataset Point Load from the Treeview onto the selected Point.

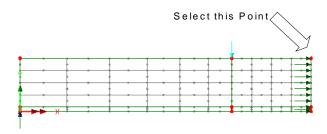


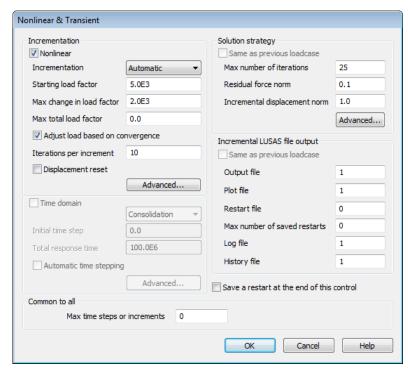
• Ensure the **Assign to points** option is set and click **OK** to assign the load to **Analysis 1, Loadcase 1**.

Nonlinear Control

Nonlinear analysis control properties are defined as properties of a loadcase. The nonlinear analysis is to be terminated when the beam deflection at mid span reaches a limiting value.

- Select the point shown.
- In the Treeview ensure the Analysis 1 entry is expanded, then right-click on Loadcase 1 and from the Controls menu select Nonlinear & Transient





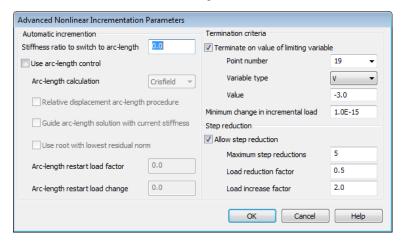
The Nonlinear & Transient dialog will appear:

- Select the Nonlinear option and set Incrementation to Automatic
- The load to be applied to the model is the concentrated load previously defined and assigned to the model multiplied by the starting load factor. Set the **Starting load** factor to 5000
- Enter the Max change in load factor as 2000 to restrict the second and subsequent load increment sizes to ensure sufficient points are obtained to observe the load deflection behaviour of the beam.
- Change the **Max total load factor** to **0** because the solution is to be terminated on the limiting displacement at mid span.
- Change the number of desired **Iterations per increment** to **10**



Note. If the number of iterations on the previous increment is less than the desired number, the next load increment will be increased (up to the maximum change in load increment). If the number of iterations is less than the desired number, the next load increment will be reduced.

- In the Solution strategy section of the dialog, ensure the Maximum number of iterations is set to 25
- Leave the **Residual force norm** as **0.1** and the **Incremental displacement norm** to **1** so convergence of the solution at each load increment will be achieved when the out of balance forces are as less than 0.1% of the reactions and the iterative change in displacements is less than 1% of the displacements for that load increment.
- In the Incrementation section of the dialog, select the **Advanced** button.



- Ensure that the Stiffness ratio to switch to arc length value is set to 0.0
- Select the **Terminate on value of limiting variable** option.
- The point number of the previously selected point (this may differ depending on how the model was created) will appear in the Point number drop down list.
- Set the Variable type to V to monitor the deflection at the selected point in the Y direction.
- Enter a value of -3 so the analysis is terminated when the central deflection reaches this value.
- In the Step reduction section ensure that the Allow step reduction option is selected.
- Click **OK** to return to the Nonlinear & Transient dialog.
- Click **OK** again to set the loadcase properties.

One additional setting is required for this analysis to ensure no element mechanisms are induced as the material yields.

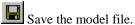
File Model Properties...

- Select the **Options** tab.
- Click on the **Element Options** button and select the **Fine integration for stiffness** and mass (structural) option.
- Click the **OK** button to return to the Model Properties dialog.
- Click the **OK** button to finish.

Save the model

The model is now complete and the model data is to be saved before an analysis is run using the LUSAS Solver.





Running the Analysis

Open the **Solve Now** dialog, and press **OK** to run the analysis.

During the analysis 2 files will be created:

- □ **beam_nl.out** this contains the statistics of the analysis, for example how much disk space was used, how much CPU time was used, and any errors or warning messages from LUSAS, and so on. Always check the LUSAS output file for error messages.
- □ **beam_nl.mys** this is the LUSAS results database which will be used for results processing.



Note. Warnings will be written to the text output window during this analysis. Warnings are not to be confused with errors which normally stop an analysis from being run. The warnings are written to advise you of modelling-related issues that are found during the analysis and of the steps LUSAS has taken (if any) to allow the analysis to continue.

If the analysis is successful...

Analysis loadcase results are added to the Treeview.

If the analysis fails...

If the analysis fails, information relating to the nature of the error encountered can be written to an output file in addition to the text output window. Select **No** to not view

the output file. Any errors listed in the text output window should be corrected in LUSAS Modeller before saving the model and re-running the analysis.

Rebuilding a Model

If it proves impossible for you to correct the errors reported a file is provided to enable you to re-create the model from scratch and run an analysis successfully.

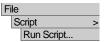


□ **beam nl modelling.vbs** carries out the modelling of the example.

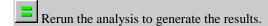


Start a new model file. If an existing model is open, Modeller will prompt for unsaved data to be saved before opening the new file.

Enter the file name as beam_nl



To recreate the model, select the file **beam_nl_modelling.vbs** located in the **\<LUSAS Installation Folder>\Examples\Modeller** directory.



Viewing the Results

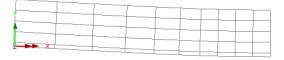
Analysis loadcase results are present in the Treeview.

Changing the Active Results Loadcase

• In the Treeview the last load increment Increment 7 Load Factor = 17000 should be already Set Active.

Deformed Shape

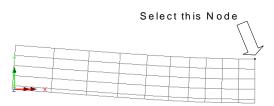
 In the Treeview turn off the Geometry, Attributes and Mesh layers by right clicking on each entry and selecting the On/Off option.



Creating a Load versus Displacement Graph

A graph of displacement at midspan is to be plotted against the applied load. To do this a node on the line of symmetry is selected:

 With the **Deformed mesh** layer visible, select the top node on the axis of symmetry as shown.



Using the Graph Wizard

The graph wizard provides a step-by-step means of selecting which results are to be plotted on the X and Y axes of the graph. The X axis is always defined first.

Utilities

Graph Wizard...

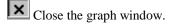
- Ensure the **Time history** option is selected and click the **Next** button.
- Ensure the **Nodal** results is selected and click **Next**
- Select entity **Displacement** for component resultant displacement **RSLT**
- The node number selected earlier will be displayed in the Specify drop-down list.
- Click the **Next** button.

The Y axis results to be graphed are now defined.

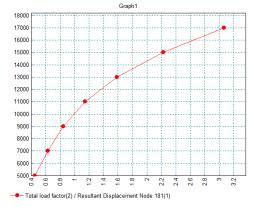
- Select the Named option and click Next
- Select **Total load factor** from the drop down list.
- Click the Next button.
- Leave all title information blank and click the **Finish** button to display the load deformation graph.



Note. Graphs can be modified using the right hand mouse button in the graph window and selecting the **Edit Graph Properties** option.



• In the Treeview turn off the **Deformed mesh** layer and turn on



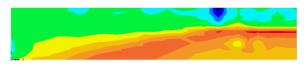
the Mesh layer.

Maximum Principal Stress Contour Plots

• With no features selected, click the right-hand mouse button in a blank part of the graphics window and select the **Contours** option to add the contours layer to the Treeview.

The properties dialog will be displayed.

 Select entity Stress -Plane Stress, Component of stress in the x direction, SMax, and Averaged nodal contours.



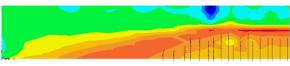
• Click the **OK** button to display contours of stresses for the final load increment.

Viewing Crack Patterns

 With no features selected, click the right-hand mouse button in a blank part of the graphics window and select the Values option to add the values layer to the Treeview.

The properties dialog will be displayed.

- Select Stress Plane Stress contour results of type Crack/crush
- Select Values Display tab and press the Failure details... button to change the pen colour that is used to plot negative yield to Black.
- Click the **OK** button to return to the previous dialog, and **OK** again to display the cracking



pattern for final load increment superimposed onto the stress contours.

Animating the Results

As an alternative to viewing results individually for each loadcase, the change of stress due to the increasing load increments can be animated instead. To ensure consistent contour values throughout the animation the interval, and the maximum and minimum values for the range of contours is to be specified.

In the Treeview double-click on the Contours layer.

The contour properties will be displayed.

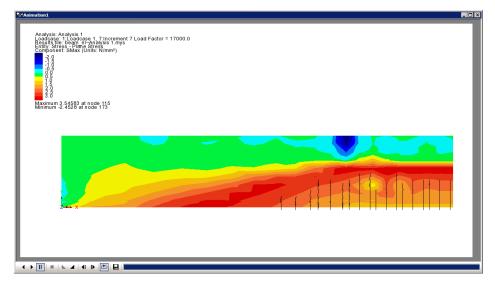
- Select the Contour Range tab and click the Interval option and set the contour interval as 0.5
- Click the **Maximum** button and set the maximum value as **3**
- Click the **Minimum** button and set the minimum value as -2
- Click the **Set as global range** and **Use global range** options.
- Click the **OK** button to redisplay the stress contours using the new contour range.

Using the Animation Wizard

Tools

Animation Wizard...

- Select the **Load History** option and click the **Next** button.
- Select the All loadcases option and select the Finish button to create the animation sequence.





Note. The buttons at the bottom of the window may be used to slow-down, speed-up, pause, step through frame by frame, or stop the animation.



Note. To see the animation window in isolation use the **Window > Layout > Multiple documents** menu option.

Saving Animations

Animations may be saved for replay in Windows animation players.

Ensure the animation window is the active window.

File Save As AVI... Browse to your projects folder and enter beam nl for the animation file name. An .avi file extension is automatically appended to the file name. Click Save



Note. Animations can be compressed to save disk space by changing the **Compression Quality.** Reducing the quality will, however, result in a lower definition image. It is also possible to reduce file size by setting smaller dimensions on the first page of the **Animation Wizard**.



Close the animation window, choosing not to save changes.

Creating a slice section of results

In this example a graph is to be plotted of the variation in stress through the specified section of the beam. The X axis values of distance are defined by the section slice. The Y axis results are specified from the graph wizard dialog.

If necessary, return the model to the default starting view by clicking Z: N/A on the status bar at the bottom of the graphics window.

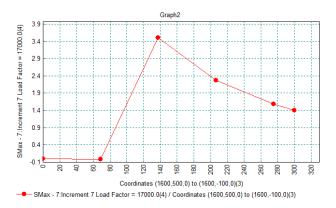
Utilities Graph Through 2D

- Ensure the **Snap to grid** option is selected and a grid size of **100** is specified.
- Click the **OK** button.
- Using the screen ruler as a guide, click and drag the cursor shown to define the location of a section slice through the beam

at a distance of 1600 from the left-hand end.

- For the loadcase and extent option accept the default of the current loadcase and click Next
- Select **Stress** results for Stress **SMax** and click the **Next** button.
- Leave all title information blank.

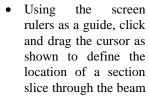
• Click the **Finish** button to create the graph of stress through the section of beam.

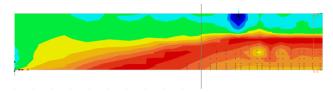


Adding Additional Results to a Graph

Window

LUSAS View: beam_nl.mdl Window 1 Re-select the window containing the results contours. The cursor will still be in section slice mode.



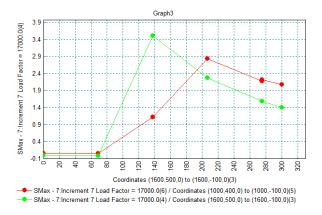


at a distance of 1000 from the left-hand end.

- For the loadcase and extent option accept the default of the current loadcase and click Next
- Select Stress Plane Stress results for Stress SMax and click the Next button.
- In the 'Include existing graphs' panel select the check box for **Graph 2**.

 Click the Finish button to see the results for the second slice section alongside the results for Graph 2.

Close the graph window.



Plotting Crack Width Contours and Values

Crack width values as calculated by the use of the Smoothed Multi Crack Concrete Model can be plotted in contour and value form:

Double-click the Contours layer name in the Treeview.

The properties dialog will be displayed.

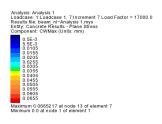
- Select entity Concrete Results for component of stress in the x direction, CWMax
- Select the Contour Range tab and deselect Use global range
- Deselect the Maximum button
- Deselect the **Minimum** button
- Set the contour **Interval** to be **0.005**
- Ensure the Value to pass through is set to be **0.005**
- Click the **OK** button to redisplay the stress contours using the new contour range.
- Press **Yes** to confirm the Values layer will be adjusted to match.

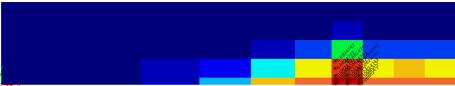


Note. Contouring of crack width values effectively shows the elements affected by cracking and identifies those elements where the maximum crack widths occur. This is done using unaveraged, or unsmoothed values at nodes. To see the actual values of crack width within elements (at the locations where the Crack/crush patterns were plotted earlier in the example), values for gauss points need to be plotted.

To see the crack width values:

- Double click the Values layer name in the Treeview.
- With the Values Results tab active, ensure the following are selected: Concrete Results of Component CWMax at Location Gauss Point.
- Select the Values Display tab and ensure the Symbols and Values are checked, and change the Font angle to 45 degrees.





• Click **OK** to update the display and show the actual crack width value calculated at gauss points within the element.

This completes the example

Discussion

Plotting Crack Widths to EN1992-1-1

In this example nonlinear steel properties were defined for the reinforcing bar elements. Reinforcement bar attributes (accessed from the **Attributes** > **Geometric** > **Bar reinforcement** menu item) may alternatively be used to model the steel reinforcement in reinforced concrete, but only if a linear steel material model is used in place of the nonlinear steel material to represent the steel reinforcement and the Crack Widths calculation utility (which is accessed from the **Bridge** > **Crack Widths to EN1992-1-1** menu item) is employed. Note that a linear steel material model (rather than a nonlinear one) is required for the steel reinforcement because of the steel strains used in the calculations.

Reinforcement bar attributes are similar to geometric line attributes but need to be assigned to lines meshed with bar elements for a chosen analysis to enable a crack width calculation to be carried out.

Bar attributes may be defined for a single reinforcing bar (termed a Discrete bar), as would be used in a 3D model, or be defined with suitable properties to represent a bundle or simplified arrangement of bars (termed Equivalent bars) as would be used typically in a 2D plane strain analysis, and done in this example. Appropriate settings for this example are shown on the dialog right.

When linear steel material and reinforcement bar attributes have been defined to the lines representing the reinforcement, and the model solved, contours and values of crack widths



can be plotted in accordance with EN1992-1-1:2004 Eurocode 2 by selecting the Entity **Crack Widths EN 1992-1-1** and the Component **Maximum Crack Width** on the Contour Properties dialog.

Crack width contours can be plotted along the bar elements (actually on the surface of the fleshed bar section) corresponding to the steel strains used in the calculation, and not on any concrete face or surface in the model. Contours and values are plotted for an active loadcase (or combination) and are re-computed if a different loadcase is set active. This visualisation method is used because the approach used in EN 1992-1-1:2004 to calculate crack widths is generally unclear as to where the crack width calculation applies.

A typical crack width contour plot for the bar reinforcement attribute described previously to represent the steel in this example is shown below.

