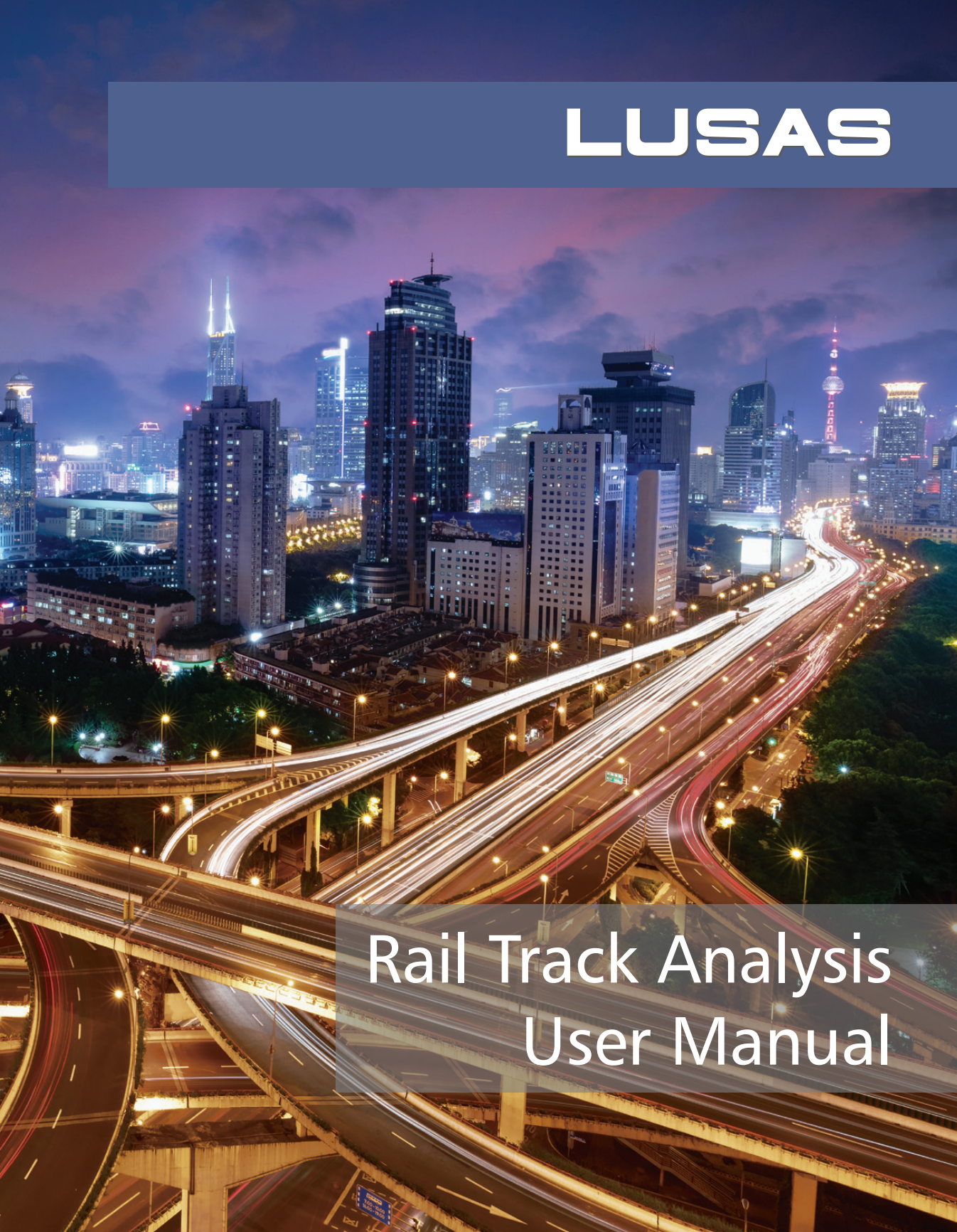


A long-exposure photograph of a city at night, featuring a complex multi-level highway interchange in the foreground with prominent white and red light trails from traffic. The background is filled with a dense urban skyline, including several tall skyscrapers, one of which is the Oriental Pearl Tower. The sky is dark with some clouds.

LUSAS

Rail Track Analysis User Manual

Rail Track Analysis User Manual

LUSAS Version 23.0 : Issue 1

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Rail Track Analysis

Introduction

The passage of one or more trains crossing a rail bridge causes forces and moments to occur in the rails that, in turn, induce displacements in the supporting bridge deck, bearings and piers. As part of the design process for rail bridges it is necessary to ensure that any interaction between the track and the bridge as a result of temperature and train loading is within specified design limits.

UIC774-3 Code of Practice

According to the Union Internationale des Chemins de fer (International Union of Railways) UIC774-3 Code of Practice, the track-structure interaction effects should be evaluated in terms of the longitudinal reactions at support locations, rail stresses induced by the temperature and train loading effects in addition to the absolute and relative displacements of the rails and deck. To accurately assess the behaviour these interaction effects should be evaluated through the use of a series of nonlinear analyses where all thermal and train loads are taken into account. These loads should be:

- ☐ Thermal loading on the bridge deck
- ☐ Thermal loading on the rail if any rail expansion devices are fitted
- ☐ Vertical loads associated with the trainsets
- ☐ Longitudinal braking and/or acceleration loads associated with the trainsets

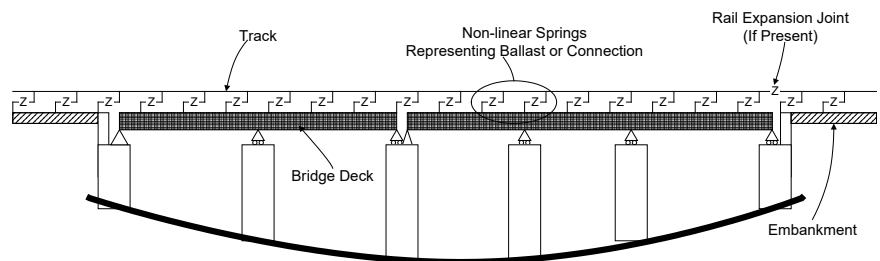


Figure 1: Representation of Structural System for Evaluation of Interaction Effects

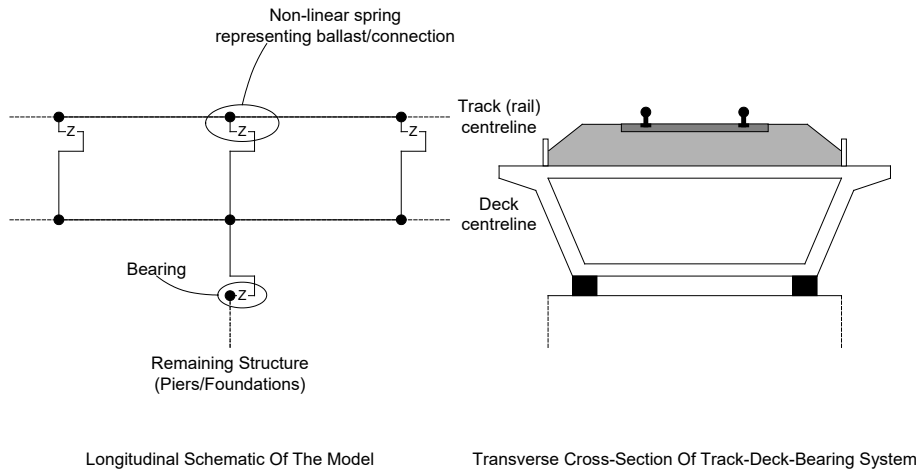


Figure 2: Typical Model of Track-Deck-Bearing System

The interaction between the track and the bridge is approximated in the UIC774-3 Code of Practice by a bilinear relationship as indicated in the following figure. The resistance of the track to the longitudinal displacements for a particular track type is a function of both the relative displacement of the rail to the supporting structure and the loading applied to the track. If the track is subjected to no train loads, then the ultimate resistance of the track to relative movement is governed by the lower curve in the figure (based on the track type). Application of train loads increases the resistance of the track to the relative displacements and the upper curve should be used for the interaction between the track and bridge where these train loads are present – unloaded resistance is still used for all other locations.

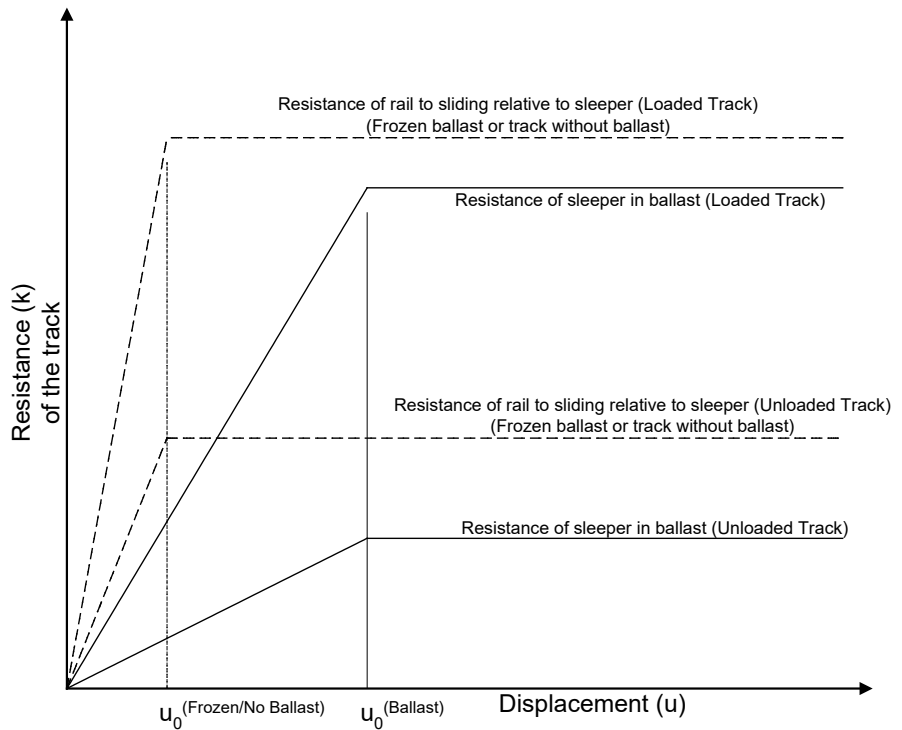


Figure 3: Resistance (k) of the Track per Unit Length versus Longitudinal Relative Displacement of Rails

The values of displacement and resistance to use in these bilinear curves are governed by the track structure and maintenance procedures adopted and will be specified in the design specifications for the structure. Typical values are listed in the Code of Practice for ballast, frozen ballast and track without ballast for moderate to good maintenance and are repeated below.

Displacement between the elastic and plastic zones, u_0 :

Resistance of the rail to sliding relative to sleeper = 0.5 mm

Resistance of sleeper in the ballast = 2.0 mm

Resistance in the plastic zone, k:

Resistance of sleeper in ballast (unloaded track), moderate maintenance = 12 kN/m

Resistance of sleeper in ballast (unloaded track), good maintenance = 20 kN/m

Resistance of loaded track or track with frozen ballast = 60 kN/m

Resistance of unloaded track for unballasted track = 40 kN/m

Resistance of loaded track for unballasted track = 60 kN/m

According to the UIC774-3 Code of Practice there is no requirement to consider a detailed model of the substructure (bearing-pier-foundation and bearing-abutment-foundation systems) when ‘standard’ bridges are considered, instead this can be modelled simply through constraints and/or spring supports that approximate the horizontal flexibility due to pier translational, bending and rotational movement. The LUSAS Rail Track Analysis option allows this type of analysis to be carried out where the behaviour of the bearing and the pier/abutment-foundation are individually specified but also provides the capability of explicitly modelling the bearing-pier/abutment-foundation systems where each component is defined, including the height and properties of the pier/abutment.

The approach outlined in the UIC774-3 Code of Practice is also incorporated in the “Eurocode 1: Actions on Structures – Part 2: Traffic loads on bridges” (EN 1991-2:2003).

LUSAS Rail Track Analysis

The Rail Track Analysis option in LUSAS provides the means to automate the finite element analyses required for conducting bridge/track interaction analyses in accordance with the UIC774-3 Code of Practice. The key features are:

- ☐ LUSAS finite element models are automatically built from general arrangement, deck/abutment/pier properties, expansion joints, supports, interaction effects, and thermal and train loading data defined in an Excel or compatible XLSX format spreadsheet file.
- ☐ Zero Longitudinal Resistance (ZLR) and Reduced Longitudinal Resistance (RLR) fastening systems can be included in the interaction analyses
- ☐ Batch capabilities allow both multiple structures to be built and multiple rail load configurations to be analysed to investigate the interaction effects on different structures, the results of which can be enveloped to determine worst effects
- ☐ Rail and structure results are automatically extracted to an XLSX format spreadsheet for presentation purposes and optional further processing by users.

Worked Examples

A worked example “Track-Structure Interaction to UIC774-3” is provided. This examines the track-structure interaction between a braking train and a single span bridge to replicate (as far as the original test data allows) testcase E1-3 which can be found in Appendix D.1 of the UIC774-3 Code of Practice.

Enhanced features of the Rail Track Analysis tool are demonstrated in additional worked examples such as the “Rail Track-Structure Interaction with Offset Bearings and Train Loading Groups” worked example which provides an example of more complex trainset configuration modelling, and the “Rail Track-Structure Interaction with Zero Longitudinal Resistance” worked example which provides an example of the use of Zero Longitudinal Resistance rail fasteners.

The Rail Track Analysis Spreadsheet

An Excel or compatible XLSX format spreadsheet is used to define the data from which a LUSAS finite element model is built and a track/bridge interaction analysis is carried out. The spreadsheet is separated into a number of worksheets that relate to particular aspects of the Rail Track Analysis input requirements. These worksheets cover:

- ☐ **Number of Decks, Tracks and Embankment Lengths**
- ☐ **Structure Definition**
- ☐ **Geometric Properties**
- ☐ **Material Properties**
- ☐ **Interaction and Expansion Joint Properties**
- ☐ **Loading**

For each worksheet comments are included to advise on the appropriate input to the spreadsheet. These can be seen when hovering the mouse cursor over the cell of interest.

The template for the input spreadsheet is located in the \<**Lusas Installation Folder**>**Programs****Scripts****User** folder. This template should be edited and saved under a different file name in the working folder in order to carry out analyses.

SI units / US units

Model data is entered in the spreadsheet in “convenient” SI or US units. The required units are indicated in the various sections of the spreadsheet and should be adhered to for the correct modelling of the interaction analysis. When the model is built from the data in the spreadsheet, all input is converted to consistent SI units of N,m,kg,s and C, or as consistent US units of kip,ft,kslug,s,F, if specified.

Screenshots and dialogs shown in this manual will generally show SI units.

Non-standard unit conversion during import of data from Excel or compatible XLSX format spreadsheet

Quantity description	Metric units		US customary units	
	Input units	Standard units	Input units	Standard units
Bearing spring stiffness	kN/mm	N/m	kip/in	kip/ft
Young's modulus	N/mm ²	N/m ²	kip/in ²	kip/ft ²
Density	kg/mm ³	kg/m ³	kslug/in ³	kslug/ft ³
Interaction joint spring stiffness	kN/mm per m of track	N/m per m of track	kip/in per ft of track	kip/ft per ft of track
Interaction joint yield force	kN per m of track	N per m of track	kip per ft of track	kip per ft of track
Expansion joint initial gap	mm	m	in	ft
Train loading	kN/m	N/m	kip/ft	kip/ft
Bearing spring stiffness	kN/mm	N/m	kip/in	kip/ft

Worksheet 1: Decks, Tracks and Embankment Lengths

	A	B	C	D	E	F	G	H	I	J	K	L	M
1	Decks, Tracks and Embankment	Units - m											
2													
3	Model Units	N,m,kg,s,C	Changing the unit set will not update the values in the spreadsheet										
4	Number of Decks	2											
5	Number of Tracks	1											
6	Left Embankment Length	100											
7	Left Embankment Ballast Type	1											
8	Right Embankment Length	100											
9	Right Embankment Ballast Type	1											
10	Length of Decks Only / Total Length (m)	120	320										
11													
12													
13													
14													
15													
16													
17													
18													
19													
20													
21													
22													
23													
24													
25													
26													
27													
28													
29													
30													
31													
32													

Figure 4: Definition of Number of Decks, Tracks and Embankment Lengths

This worksheet defines the global arrangement details of the bridge structure. The inputs to the worksheet are:

Model Units

Model units can be specified as either 'N,m,kg,s,C' or 'kip,ft,kslug,s,F'. The first row of each worksheet states the units in use.

Within the worksheets, model data is entered in "convenient" SI or US units. When the model is built from the data supplied, all input is converted to consistent SI units or to consistent US units as specified.

Note that, by design, changing the model units in use (on this 'Decks, Tracks and Embankments' worksheet) does not convert the values in the spreadsheet.

Number of Decks

This defines the number of decks in the structure and controls the importing of the structure layout in the **Structure Definition** worksheet. The number of decks is initially limited to 100 but this number can be increased by modifying the **Structure Definition** worksheet as outlined in the following section.

Number of Tracks

This defines the number of railway tracks that pass along the structure and embankments. The number of tracks must be equal to one or more. For two or more tracks, one track should take the braking load of a trainset and another the acceleration load of a separate trainset in accordance with the UIC77-3 Code of Practice (Clause

1.4.3). In addition, Code of Practice such as “Eurocode 1: Actions on Structures – Part 2: Traffic loads on bridges (EN 1991-2:2003)” have additional conditions when two or more tracks have the same permitted direction of travel.

Each track consists of two rails which act together (see the *Geometric Properties* section).

Left and Right Embankment Length

This defines the lengths of the left and right embankments in the model illustrated in the figure below. These lengths should be sufficiently long to allow enough of the trainset loading to be placed on the embankment to model the approach of the trainset to the structure. For very long trainset definitions the embankment does not have to be long enough to accommodate the whole trainset, the Rail Track Analysis tool will allow train loading to remain outside of the model for some trainset positions of the analysis (a warning will be issued before the model is built).

The lengths of the embankments should also be long enough to allow the rail stress to return to a constant value away from the abutments where additional stresses are typically introduced into the rails from temperature variations applied to the decks of the structure. Figure 6 shows typical rail stress variations for a simply supported deck for (a) where there is Continuously Welded Rail (CWR) and just a temperature increase has been applied to the deck and (b) where temperature increases have been applied to both the rails and the deck. For both models the embankment lengths are just sufficient for the rail stresses to be considered constant at the embankment limits.

When defining the lengths of the embankments the UIC774-3 Code of Practice states that these should be a minimum of 100m (Clause 1.7.3).

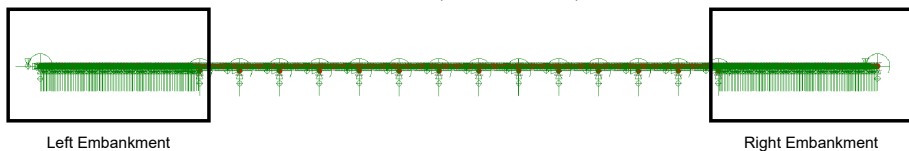


Figure 5: Left and Right Embankments in Model

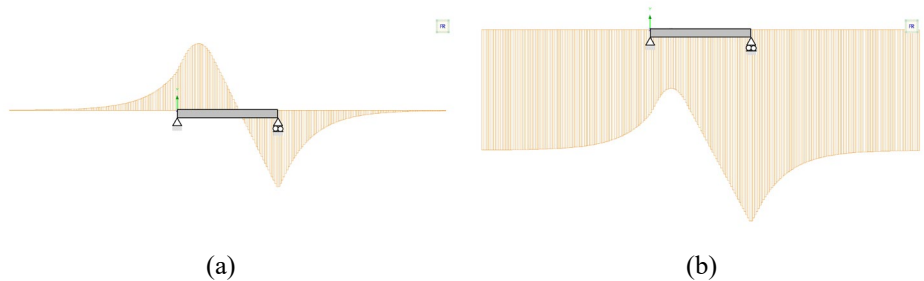


Figure 6: Rail Stresses due to Temperature Variations for a Simply Supported Deck
(a) Temperature Increase in the Deck Alone, (b) Temperature Increase in the Deck and Rail

Left and Right Embankment Ballast Type

This defines the type of ballast that characterises the interaction between the tracks and the left and right embankments of the model. The ballast type is defined through bilinear relationships that are input in the *Interaction and Expansion Joint* properties worksheet and the integer ID must correspond to one of the definitions in this worksheet.

Worksheet 2: Structure Definition

Structure Definition		Units	Pier Height	m	Bearing springs on top of each pier	kN/mm	Span Length	m									
		Spring Support for each Abutment / Pier	Pier Height	Pier Geo. Assign.	Pier Mat. Assign.	Bearing Springs on Top of each Pier	Bearing Offset from End of Deck	Span Length	Geo. Assign.	Mat. Assign.	Ballast Type						
Deck 1	Left End	R					0.25	30	1	1	1						
	Span 1	R	6.5	2	2	F	0.5	30	1	1	1						
	Span 2	R	9	2	2	F	0.5	30	1	1	1						
	Span 3																
	Span 4																
	Span 5																
	Span 6																
	Span 7																
	Span 8																
	Span 9																
Number of Supports for the Deck / Length		3				3		60									
Deck 2	Left End	R	8	2	2	F	0.5	30	1	1	1						
	Span 1	R	9	2	2	F	0.25	30	1	1	1						
	Span 2	R	9	2	2	F	0.25	30	1	1	1						
	Span 3																
	Span 4																
	Span 5																
	Span 6																
	Span 7																
	Span 8																
	Span 9																
Number of Supports for the Deck / Length		3				3		60									
Deck 3	Left End																
	Span 1																
	Span 2																
	Span 3																
	Span 4																
	Span 5																
	Span 6																
	Span 7																
	Span 8																
	Span 9																
Number of Supports for the Deck / Length		0				0		0									
Deck 4	Left End																
	Span 1																

Figure 7: Structure Definition

The **Structure Definition** worksheet allows the geometry of the bridge to be input deck by deck. For each deck the worksheet allows the definition of the length, geometric, material and ballast type assignments of the internal spans plus pier/abutment arrangements along with their support and bearing characteristic. The input allows the modelling of the piers through equivalent springs using the method proposed in the UIC774-3 Code of Practice (see note below) or through the physical modelling of the piers by entering input of the pier heights plus geometric and material assignments. The inputs to the worksheet are:

Spring Support for each abutment/pier

This defines the longitudinal stiffness for the abutment or pier. The longitudinal stiffness for the abutment or pier should be entered as either free 'F', restrained 'R' or a positive stiffness in kN/mm.

For the equivalent spring approach, if the displacement behaviour of the support and the bearings are modelled separately the supports should be set to take account of the displacement at the top of the support due to elastic deformation, the displacement at the top of the support due to the rotation of the foundation and the displacement at the top of the support due to the longitudinal movement of the foundation. If instead the displacement behaviour of the support and bearings are lumped together, as illustrated in the example in Figure 7, the spring supports for the piers and abutments should be set to 'R' for restrained.

If the piers are physically modelled then the spring support for the pier should represent the longitudinal stiffness of the foundation at the base of the pier.



Note. The pier properties for the last pier of one deck must exactly match the properties defined for the next deck or an error will be reported when the spreadsheet is used to carry out the analysis.



Note. When the pier/foundation system is modelled as a spring this spring can be calculated by combining the component movements associated with the pier as indicated below and described further in the UIC774-3 Code of Practice:

$$\delta_{\text{total}} = \delta_p + \delta_\varphi + \delta_h [+ \delta_b]$$

where

δ_p = displacement at top of support due to elastic deformation

δ_φ = displacement at top of support due to rotation of the foundation

δ_h = displacement at top of support due to horizontal movement of the foundation

δ_b = relative displacement between the upper and lower parts of bearing (Only included if bearings effects lumped into support conditions)

and the total spring stiffness is calculated from:

$$K = \frac{H}{\delta_{\text{total}}} \quad (\text{in kN/mm})$$

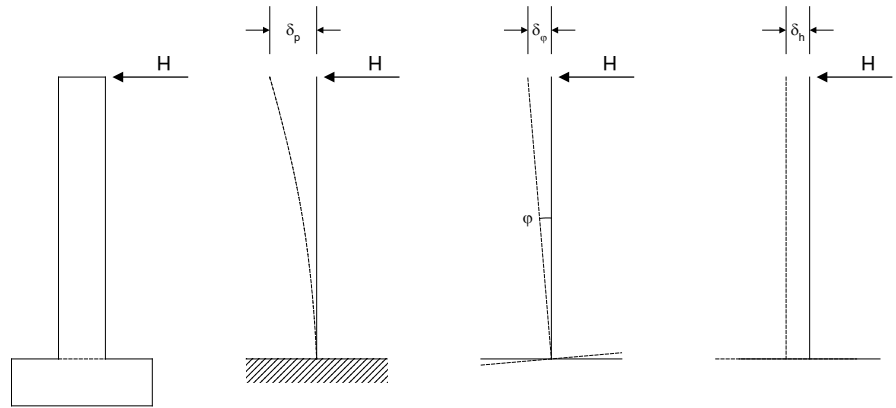


Figure 8: Component Behaviour for Calculating Support Stiffness



Note. If the piers are modelled in the analysis the rotation of the foundation is assumed to be zero in the analysis. This can be adjusted by modifying the support conditions manually after a temperature only analysis has been performed (see user interface discussions).

Bearing springs on top of each pier

This defines the longitudinal stiffness of the bearings between the top of the support and the deck. The longitudinal stiffness for the bearing should be entered as either free 'F', restrained 'R' or a positive stiffness in kN/mm.

For the equivalent spring approach where the stiffness of the support due to elastic deformation, rotation of the foundation and horizontal movement of the foundation are lumped with the bearing behaviour this input should include all of the stiffness contributions and the *Spring support for each abutment/pier* should be set to 'R'. If the bearing behaviour is separated from the behaviour of the support the input should match the requirements for the bearing alone.

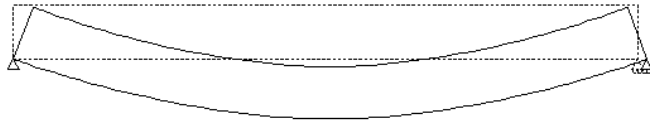
When the piers are physically modelled in the model by setting their height and properties the longitudinal stiffness of the bearing alone should be input since the behaviour of the pier will be incorporated by the extra beam elements representing the pier in the model.

Bearing offset from end of deck

This defines the offset from the end of the deck for the longitudinal location of the bearing. The bearing offset should be in m.

The bearing at the end of the deck may not be at the end (or sufficiently close to the end) of the deck to be able to justify such modelling as contained in UIC774-3 where bearings are assumed to be at the end. If the bearing is inboard of the end of the deck this can have a significant effect on the displacement / bending behaviour of the deck which itself can have an effect on the track-structure interaction and the displacement behaviour between decks plus the deck ends and the abutments as illustrated below..

Bearings At Deck Ends



Bearings Inboard of Deck Ends

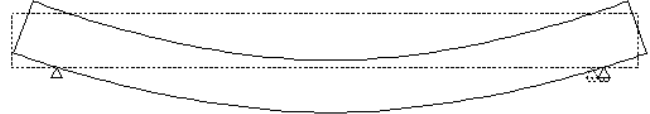


Figure 9: Effect of Bearings Inboards of the Deck Ends

When bearing offsets are used with physical pier modelling the physical geometry of the pier will be built with rigid offsets modelled to ensure the bearing bases are at both the correct longitudinal location relative to the pier and also at the correct elevation as shown in the image below. This modelling ensures the correct translational and rotational behaviours of the bases of the bearing for the displacement and rotation of the supporting pier.

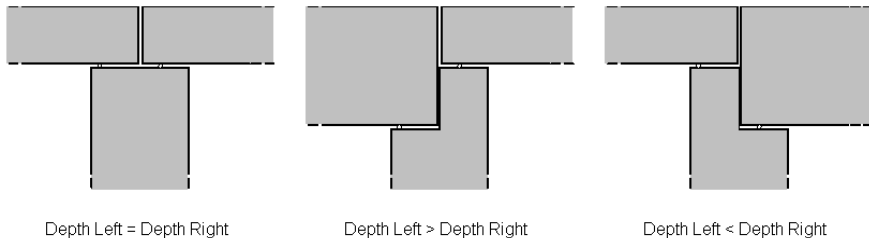


Figure 10: Pier Geometry Configurations for Bearing Elevations

This additional displacement from the correct longitudinal bearing offset modelling could increase the observed displacements of the decks themselves and could be more detrimental to the track-structure interaction.

Bearing offsets can be used when the equivalent spring pier modelling is being used but there is no ability to incorporate the additional rotation of the top of the pier and its effect on the bases of the bearings since the rotation behaviour of the pier is accounted for solely in the longitudinal stiffness used in the equivalent spring pier modelling and not through a degree of freedom in the analysis. It is therefore recommended that bearing offsets are **not** used when equivalent spring pier modelling in accordance with UIC774-3 is being used.

Span Length

This defines the span length between support locations for a deck. Up to nine spans can initially be defined for each deck but this can be increased (see the section on ***Increasing the number of spans modelled in the decks***). In the example illustrated in Figure 7 the first two decks have two 25m spans each and the third deck has three 25m spans.

Geometric Assignment

This defines the geometric properties that are assigned to the spans of the decks. The integer ID must match one of the geometric properties that is defined in the ***Geometric Properties*** worksheet. Different properties can be assigned to each span of the deck. Although the input only allows a single ID to be assigned to each span, continuously varying properties can also be modelled (see the section on ***Geometric Properties***).

Material Assignment

This defines the material properties that are assigned to the spans of the decks. The integer ID must match one of the material properties that is defined in the ***Material Properties*** worksheet.

Ballast Type

This defines the ballast type properties representing the track-structure-interaction that is assigned to the spans of the decks. The integer ID must match one of the bilinear interaction properties that is defined in the ***Interaction and Expansion Joint*** worksheet. The ballast type can be varied between decks and the input also allows different ballast types to be assigned to different spans within the same deck. This could be used if, for example, different bilinear interaction properties were required to represent different ballast conditions along a structure.

If physical modelling of the piers is to be included in the analysis then additional input is required for these piers. The inputs to the worksheet are:

Pier Height

This defines the height of the support / pier for the current location in the deck. If the pier height is blank the Rail Track Analysis tool assumes that the pier behaviour is represented solely by the spring supports and bearing springs.

Pier Geometric Assignment

This defines the geometric properties that are assigned to the support / pier for the current location in the deck. The integer ID must match one of the geometric properties that is defined in the **Geometric Properties** worksheet. Although the input only allows a single ID to be assigned to the support / pier, continuously varying properties can also be modelled (see the section on **Geometric Properties**).

Pier Material Assignment

This defines the material properties that are assigned to the support / pier for the current location in the deck. The integer ID must match one of the material properties that is defined in the **Material Properties** worksheet.

Increasing the number of decks modelled

If more than 100 decks are required the spreadsheet can be modified. To do this, scroll to the end of the **Structure Definition** worksheet and select the last complete deck definition as indicated on the figure below.

A1093

= "Deck "&J1103

A	B	C	D	E	F	G	H	I	L	M	N	O	P
1	Structure Definition	Units : Pier Height : m : Bearing springs on top of each pier : kN/mm, Span Length : m											
2		Spring Support for each Abutment /Pier	Pier Height	Pier Geo. Assign.	Pier Mat. Assign.	Bearing Springs on Top of each Pier	Bearing Offset from End of Deck	Span Length	Geo. Assign.	Mat. Assign.	Ballast Type		
3													
1089	Span 7												
1090	Span 8												
1091	Span 9												
1092	Number of Supports for the Deck / Length	0				0		0					
1093	Left End												
1094	Span 1												
1095	Span 2												
1096	Span 3												
1097	Span 4												
1098	Span 5												
1099	Span 6												
1100	Span 7												
1101	Span 8												
1102	Span 9												
1103	Number of Supports for the Deck / Length	0				0		0					
1104													
1105													
1106													
1107													
1108													
1109													
1110													
1111													
1112													
1113													
1114													
1115													
1116													
1117													
1118													
1119													
1120													
1121													
1122													
1123													

Decks, Tracks and Embankment

Structure Definition

Geometric Properties

Material Properties

Figure 11: Selection and Copying of Structure Definition Worksheet to Increase Number of Decks

Copy and paste this section as many times as required at the end of the worksheet, ensuring that the row formatting is not altered as indicated below. If successful, the deck number should be correctly calculated for the added entries. The number of decks in the **Decks, Tracks and Embankment** worksheet of the spreadsheet can now be increased to the number of decks added to the structure definition.



Note. This may require the worksheet to be unprotected first. This worksheet protection should be turned back on immediately after the extra entries for additional decks have been inserted into the worksheet to avoid accidental changes to other parts of the worksheet that could cause errors when the spreadsheet is imported into the Rail Track Analysis tool.

Structure Definition		Units	Pier Height	m	Bearing springs on top of each pier	kN/mm	Span Length	m
		Spring Support for each Abutment / Pier	Pier Height	Pier Geo. Assign.	Pier Mat. Assign.	Bearing Springs on Top of each Pier	Bearing Offset from End of Deck	Span Length
1099	Span 7							
1090	Span 8							
1091	Span 9							
1092	Number of Supports for the Deck / Length	0				0		0
1093	Left End							
1094	Span 1							
1095	Span 2							
1096	Span 3							
1097	Span 4							
1098	Span 5							
1099	Span 6							
1100	Span 7							
1101	Span 8							
1102	Span 9							
1103	Number of Supports for the Deck / Length	0				0		0
1104	Left End							
1105	Span 1							
1106	Span 2							
1107	Span 3							
1108	Span 4							
1109	Span 5							
1110	Span 6							
1111	Span 7							
1112	Span 8							
1113	Span 9							
1114	Number of Supports for the Deck / Length	0				0		0

Figure 12: Pasting of Additional Decks to Ensure Formatting Maintained

Increasing the number of spans modelled in the decks

If more than 9 spans are required in any of the decks of a structure, then the spreadsheet can be modified. To do this, select the whole row containing the **Structure Number of Supports for the Deck / Length** cell for the deck you wish to increase the number of spans for within the spreadsheet as indicated on the figure below (in the figure we are adding spans to the second deck of a structure we are defining).

A1		Structure Definition												
A		B	C	D	E	F	G	H	I	L	M	N	O	P
1		Structure Definition	Units : Pier Height : m ; Bearing springs on top of each pier : kN/mm, Span Length : m											
2			Spring Support for each Abutment / Pier	Pier Height	Pier Geo. Assign.	Pier Mat. Assign.	Bearing Springs on Top of each Pier	Bearing Offset from End of Deck	Span Length	Geo. Assign.	Mat. Assign.	Ballast Type		
3														
4		Deck 1	Left End	R			F	0.25						
5			Span 1	R	6.5	2	2	300		30	1	1	1	
6			Span 2	R	9	2	2	F	0.5	30	1	1	1	
7			Span 3											
8			Span 4											
9			Span 5											
10			Span 6											
11			Span 7											
12			Span 8											
13			Span 9											
14			Number of Supports for the Deck / Length	3			3		60					
15			Left End											
16			Span 1											
17			Span 2											
18			Span 3											
19			Span 4											
20			Span 5											
21			Span 6											
22			Span 7											
23			Span 8											
24			Span 9											
25														
26														
27														
28														
29														
30														
31			Number of Supports for the Deck / Length	0			0		0					
32			Left End											
33			Span 1											
34			Span 2											
35			Span 3											
36			Span 4											
37			Span 5											
38			Span 6											
39			Span 7											
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113														
114														
115														

Figure 14: Inserted Spans Lack the Labelling of the Original Template

B29

Span 14

1

A

2

B

3

C

4

D

5

E

6

F

7

G

8

H

9

I

10

L

11

M

12

N

13

O

14

P

1

Structure Definition

2

Units : Pier Height : m, Bearing springs on top of each pier : kN/mm, Span Length : m

		Spring Support for each Abutment / Pier	Pier Height	Pier Geo. Assign.	Pier Mat. Assign.	Bearing Springs on Top of each Pier	Bearing Offset from End of Deck	Span Length	Geo. Assign.	Mat. Assign.	Ballast Type
Deck 1	Left End	R				F	0.25				
	Span 1	R	6.5	2	2	300		30	1	1	1
	Span 2	R	9	2	2	F	0.5	30	1	1	1
	Span 3										
	Span 4										
	Span 5										
	Span 6										
	Span 7										
	Span 8										
Number of Supports for the Deck / Length		3				3		60			
Deck 2	Left End										
	Span 1										
	Span 2										
	Span 3										
	Span 4										
	Span 5										
	Span 6										
	Span 7										
	Span 8										
	Span 9										
	Span 10										
	Span 11										
	Span 12										
	Number of Supports for the Deck / Length		0				0		0		
Deck 3	Left End										
	Span 1										
	Span 2										
	Span 3										
	Span 4										
	Span 5										
	Span 7										

1

2

3

4

5

6

7

8

9

10

11

12

13

14

Decks, Tracks and Embankment

Structure Definition

Geometric Properties

Material Properties

Figure 15: Corrected Labels of Inserted Spans to Match Template

In addition to adding extra spans to the end of the deck definition it is also possible to insert spans part of the way through the definition of an existing deck should, for example, the arrangement of a deck need to be altered due to a design change and the analysis re-run. The span labelling will need to be corrected should this be done. It is generally advised that extra spans are inserted at the end of the deck definition prior to entering the structure details where possible.

While it is also possible to remove span rows from the deck definitions in the input spreadsheet this is not advisable and is also not necessary because the import of a deck stops when it detects the first blank row within a deck definition.

Worksheet 3: Geometric Properties

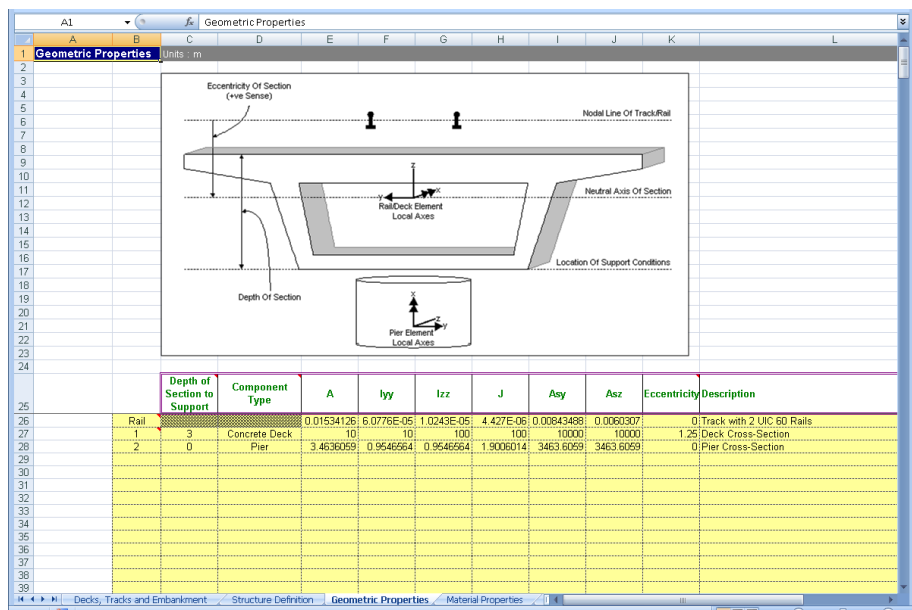


Figure 16: Geometric Properties Table for Structure

The geometric properties worksheet should list all of the section properties required for the modelling of the structure and the unique ID numbers must include all of the geometric properties that have been assigned in the **Structure Definition** worksheet. The properties should be entered in metres and are all standard LUSAS values except the **Depth of Section** to the support and the **Component Type** entries.

When the tracks are modelled the two rails of a track are assumed to behave together and the section properties should therefore take account of both rails.

Depth of Section to the Support

The **Depth of Section** to the support defines the distance from the top of slab / surface that the track interacts with to the elevation of the bearing supports for the deck and is required to ensure that the correct support conditions are maintained in combination with the overall interaction modelling. For different structure types the depth of section to support is defined slightly differently as indicated in the following figure. For a lot of structures it will often be the overall depth of the section as indicated by the left-hand and central images but for 'U'-shaped sections such as at the right-hand image the depth of the section will just be the depth of the bottom slab.

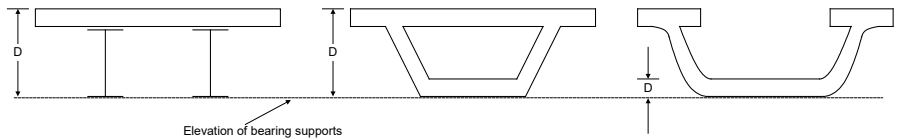


Figure 17: Depth of Section to the Support for Different Bridge Cross-Sections

Component Type

This defines the component type of the geometric property and is used for the application of the appropriate deck temperature loads defined in the **Loading** worksheet. The component type will usually be **Concrete Deck**, **Steel Deck** or **Pier**. A **User Deck** type is also provided and this can be used for a user-defined deck type.

Element Orientations

The orientations of the sectional properties should obey the axes indicated in the illustration within the worksheet and the element local axes indicated in the following figure where the double-headed arrow indicates the element local x-axis, the single headed arrow indicates the element local y-axis and the line without an arrowhead indicates the element local z-axis. For both the spans and the piers the element local y-axis is orientated into the lateral direction for the bridge with the local z-axis orientated vertically for the spans and in the longitudinal direction for the piers.

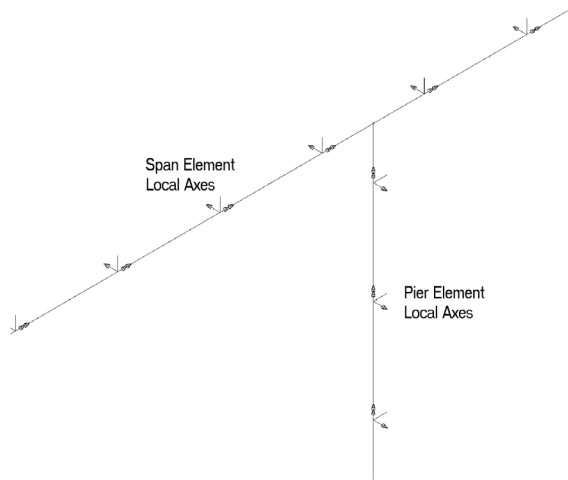


Figure 18: Beam Element Local Axes for Deck and Pier Modelling

For defining the geometric properties of the decks and rails the section axes are illustrated in Figure 19.

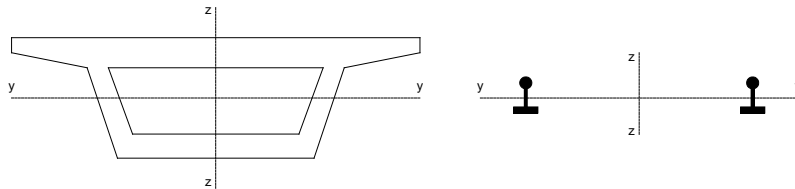


Figure 19: Section Axes for Deck and Rail Definitions

Eccentricity

All eccentricity in the modelling is defined relative to the nodal line of the track/rail and therefore a positive eccentricity will place a section below this line as indicated in the following figure. If an eccentricity is entered for the geometric property of the rail then the neutral axis of the rail will be offset from this nodal line based on the positive sense described. For this reason the eccentricity of the rail should generally be set to zero for all cases.



Notes

The number of entries can be increased by adding data to the bottom of the table. Data input will terminate on the first blank ID number in column B.

The depth of section should not be defined for geometric properties assigned to piers.

The eccentricity between the rail/slab indicated in the figure is defined later in the interaction worksheet and should not be defined as a geometric property.

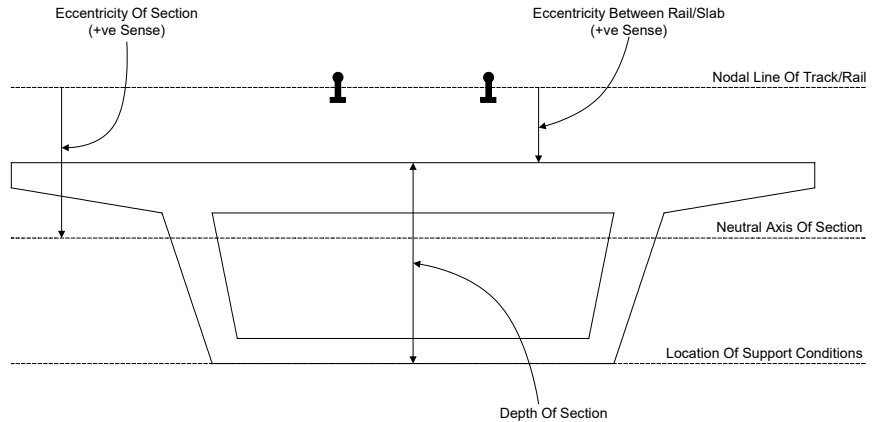


Figure 20: Eccentricity Definition for Geometric Properties and Depth of Section

Varying Section Geometric Properties

Although the spreadsheet does not allow the input of geometric properties with varying sections it is possible to analyse structures with varying sections by modifying the temperature loading only model after it has been built by the Rail Track Analysis tool before subsequently using the **Apply Rail Loads** dialog to include the trainset loading. To do this the model should be defined in the spreadsheet with an initial set of deck geometric properties.

All sections that will be used to define the varying sections of the deck must be defined externally in separate models using either the Precast Beam Section Generator, the Box Section Property Calculator or the Arbitrary Section Property Calculator and the sections added to either a local library or the server library. This will make these sections available to other models.



Note. The *Depth of Section* must be correctly set in the *Geometric Properties* worksheet for each of the deck support locations to ensure that the behaviour of the decks is correct. All other entries will be determined from the varying section.

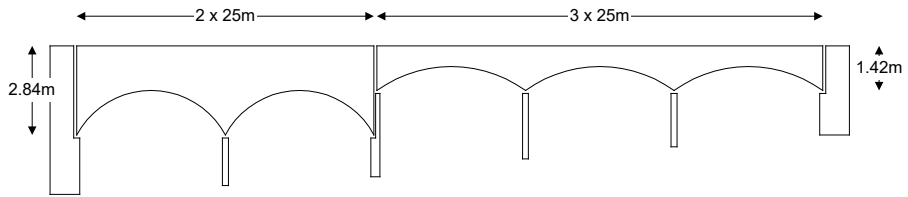


Figure 21: Example Varying Section Structure

If the structure in Figure 21 was required, the main track-structure interaction model could be set up using a spreadsheet with the **Structure Definition** and **Geometric Properties** indicated in Figure 22 and Figure 23. This would define the base model indicated in Figure 24.

Structure Definition		Units: Pier Height: m; Bearing springs on top of each pier: kN/mm; Span Length: m									
		Spring Support for each Abutment / Pier	Pier Height	Pier Geo. Assign.	Pier Mat. Assign.	Bearing Springs on Top of each Pier	Bearing Offset from End of Deck	Span Length	Geo. Assign.	Mat. Assign.	Ballast Type
Deck 1	Left End	R				F					
	Span 1	R				307		25	1	1	1
	Span 2	R				F		25	1	1	1
	Span 3										
	Span 4										
	Span 5										
	Span 6										
	Span 7										
	Span 8										
	Span 9										
	Number of Supports for the Deck / Length	3				3		50			
Deck 2	Left End	R				F					
	Span 1	R				259		25	2	1	1
	Span 2	R				F		25	2	1	1
	Span 3	R				F		25	2	1	1
	Span 4										
	Span 5										
	Span 6										
	Span 7										
	Span 8										
	Span 9										
	Number of Supports for the Deck / Length	4				4		75			
Deck 3	Left End										
	Span 1										
	Span 2										
	Span 3										
	Span 4										
	Span 5										
	Span 6										
	Span 7										
	Span 8										
	Span 9										
	Number of Supports for the Deck / Length	0				0		0			
Deck 4	Left End										
	Span 1										

Figure 22: Structure Definition for Sample Varying Section Structure

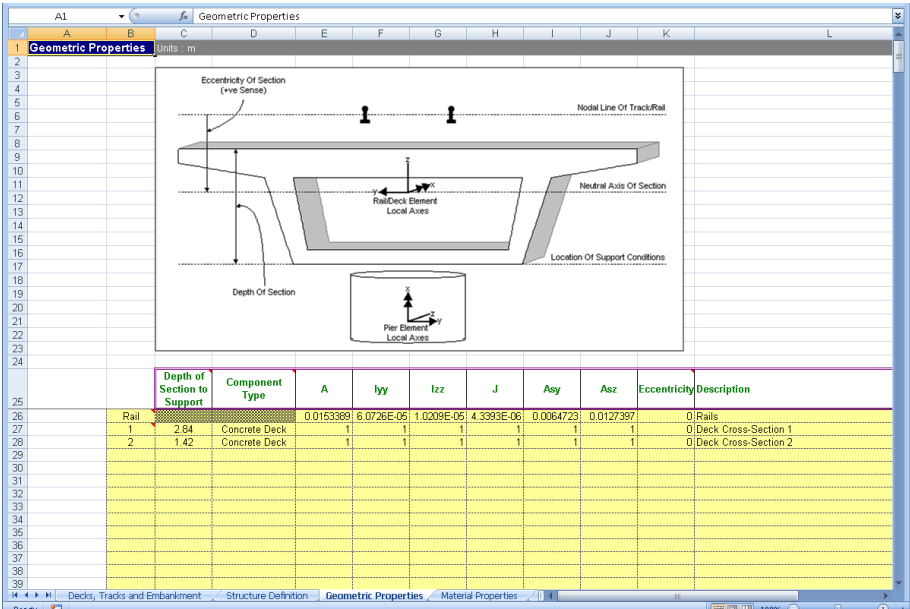


Figure 23: Geometric Properties for Sample Varying Section Structure

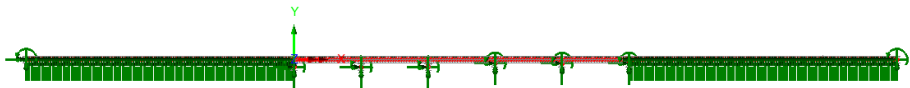


Figure 24: Base Model for Sample Varying Section Structure

In order to define the smooth variation for a single span of the decks the minimum number of sections for interpolation is five. For the 2.84m and 1.42m deep deck spans these sections are defined in separate models, calculated with the *Arbitrary Section Property Calculator* (as illustrated in the figure below for one of the sections from the 2.84m deep deck spans) and then added to the local library so they can be accessed from other models (NOTE: Only three actual sizes need to be defined for each due to symmetry).

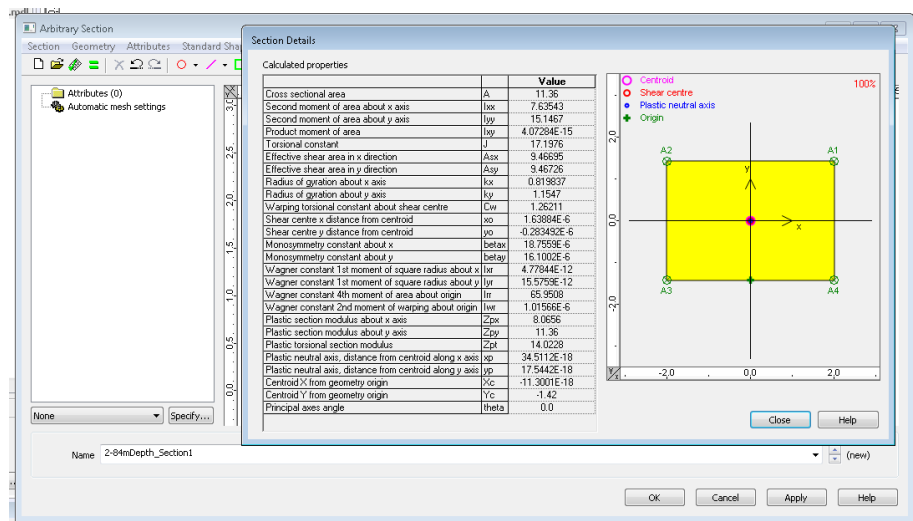


Figure 25: Arbitrary Section Property Calculation for 2.84m Depth of Section Span

These sections can now be used to define the **Multiple Varying Section** facility in Modeller. Before defining these multiple varying sections the reference paths along which the variation will take place must be defined. Define a reference path for each of the spans as illustrated in Figure 26 for the first span of the first deck. In this definition the X coordinates match the extent of the span and the Y coordinate has been set to 10 so it can be visualised easily. Four additional reference paths should also be defined, one for each of the other spans. On completion the model will resemble the one in Figure 27 where each reference path has been offset in the Y direction for visualisation purposes.

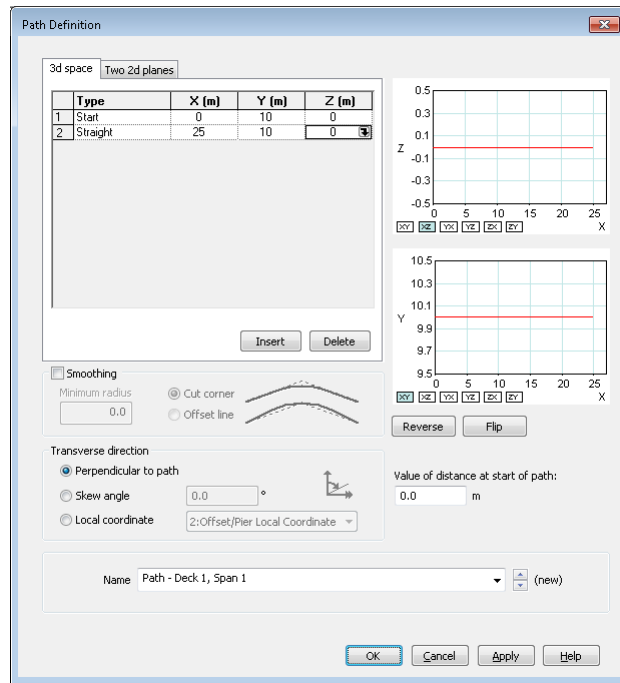


Figure 26: Definition of Reference Path for Deck 1, Span 1

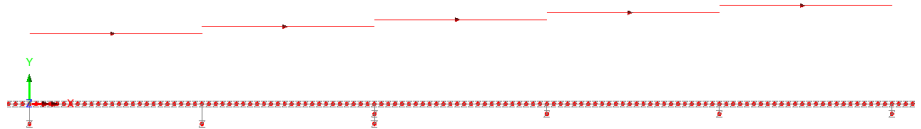


Figure 27: Reference Path for all Decks and Spans (Offset for Visualisation Purposes)

The varying sections can now be defined using the *Multiple Varying Section* dialog. For the definition of the varying section for the first span of the first deck the distance interpretation should be set to **Along reference path** and the path for the first span of the first deck selected (“Path – Deck 1, Span 1” in this example – see Figure 26). For the start of the varying section the 2.84m deep section (“2-84mDepth_Section1” in this case) should be selected from the arbitrary section library and the section edited. The eccentricity in the z direction (ez) should be set to the required value of 1.42m to obtain the required eccentricity of the neutral axis of the section from the nodal line of the track / rail which would have been entered into the *Geometric Properties* worksheet (to place the nodal line on the top of the slab). At this stage the Multiple Varying Section dialog will just have the starting section as illustrated in Figure 28.

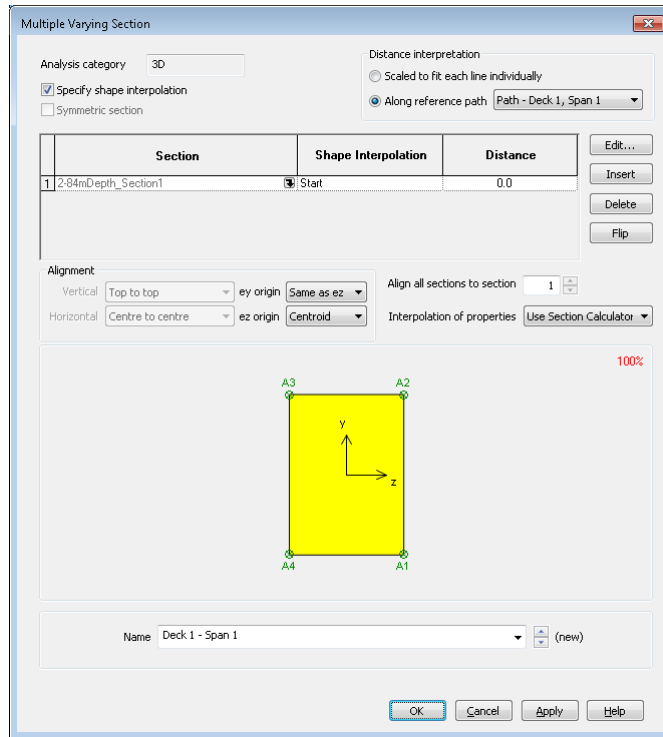


Figure 28: Definition of Multiple Varying Section for Deck 1, Span 1 (1 of 2)

The other sections defining the span also need to be added to the varying section definition and these are input as follows with the *Vertical alignment* set to *Centre to centre* and the *Horizontal alignment* set to *Right to right*:

Section	Shape Interpolation	Distance
2-84mDepth_Section2	Smoothed	5.0
2-84mDepth_Section3	Smoothed	12.5
2-84mDepth_Section2	Smoothed	20.0
2-84mDepth_Section1	Smoothed	25.0

Table 1: Section Interpolation for Deck 1, Span 1

Multiple Varying Section

Analysis category: 3D

☒ Specify shape interpolation
☐ Symmetric section

Distance interpretation:
☐ Scaled to fit each line individually
☒ Along reference path Path - Deck 1, Span 1

	Section	Shape Interpolation	Distance
1	2.84mDepth_Section1	Start	0.0
2	2.84mDepth_Section2	Smoothed	5.0
3	2.84mDepth_Section3	Smoothed	12.5
4	2.84mDepth_Section2	Smoothed	20.0
5	2.84mDepth_Section1	Smoothed	25.0

Alignment:
 Vertical: Top to top ey origin Same as ez
 Horizontal: Right to right ez origin Centroid

Align all sections to section: 1
 Interpolation of properties: Use Section Calculator

Name: Deck 1 - Span 1 (new)

OK Cancel Apply Help

Figure 29: Definition of Multiple Varying Section for Deck 1, Span 1 (2 of 2)

This multiple varying section can now be assigned to all of the lines defining the first span of the first deck, overwriting the original assignment from the Rail Track Analysis tool. A similar multiple varying section can also be defined and assigned but using the appropriate reference path for the second span of the first deck.

The same procedure should also be followed for the 1.42m deep section using associated sections and a starting eccentricity in the z direction (ez) of 0.71m to obtain the required eccentricity of the neutral axis of the section from the nodal line of the track / rail which would have been entered into the *Geometric Properties* worksheet. On completion and assignment of the multiple varying section geometric attributes to the appropriate spans of the model the structure would look similar to the model in Figure 30.

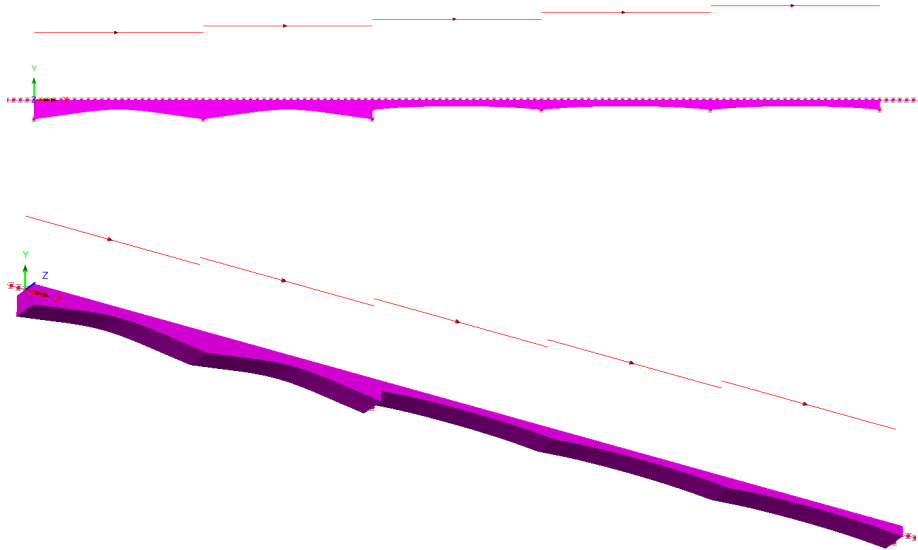


Figure 30: Model after Assignment of Multiple Varying Sections



Note. The multiple varying section could be defined with just two reference paths, one for each of the decks and the geometric attributes defined as indicated in Figure 31. When modelling structures where the sections do not vary smoothly, for example over a pier as indicated in Figure 21, caution should be exercised as using a single reference path per deck could lead to artificial smoothing of the section variation. This is illustrated in Figure 32 and Figure 33 which examine the behaviour at an intermediate pier of a deck when a single path is used for each deck. In Figure 33 the image on the left is from the use of a single reference path for the whole deck and shows the smoothing that has occurred over the pier when compared to the image on the right which is from the use of a single reference path for each span of the deck.

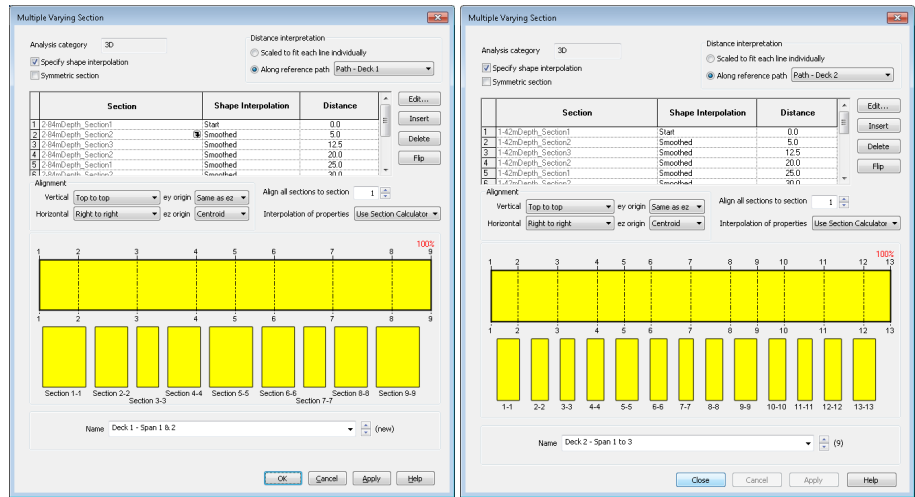


Figure 31: Definition of Multiple Varying Section for Deck 1 and Deck 2 for Two Reference Paths



Figure 32: Model after Assignment of Multiple Varying Sections with Two Reference Paths

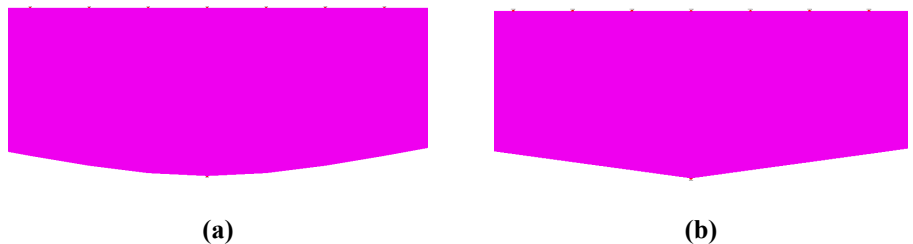


Figure 33: Zoomed Plot of Pier Location between Spans of Deck 1 Showing (a) Smoothed Section for a Multiple Varying Sections with One Reference Path per Deck and (b) Correct Unsmoothed Section for a Multiple Varying Sections with One Reference Path per Span

Worksheet 4: Material Properties

	A	B	C	D	E	F	G	H	I	J	K	L	M
1	Material Properties		Units - N, mm, kg										
2													
3													
4													
5													
6													
7													
8													
9													
10													
11													
12													
13													
14													
15													
16													
17													
18													
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30													
31													
32													
33													
34													
35													
36													
37													
38													
39													
40													
41													
42													

Figure 34: Material Properties Table for Structure

The material properties worksheet should list all of the material properties required for the modelling of the structure and the unique ID numbers must include all of the material properties that have been assigned in the **Structure Definition** worksheet. The elastic properties are all standard LUSAS values which should be entered in Newtons, millimetres and kilograms. The mass density (ρ) is not used in the analysis but is provided to allow the model to be solved with self-weight loading and for it to be combined with the thermal/train loading effects covered in these analyses.



Note. The number of entries can be increased by adding data to the bottom of the table. Data input will terminate on the first blank ID number in column B.

Worksheet 5: Interaction and Expansion Joint Properties

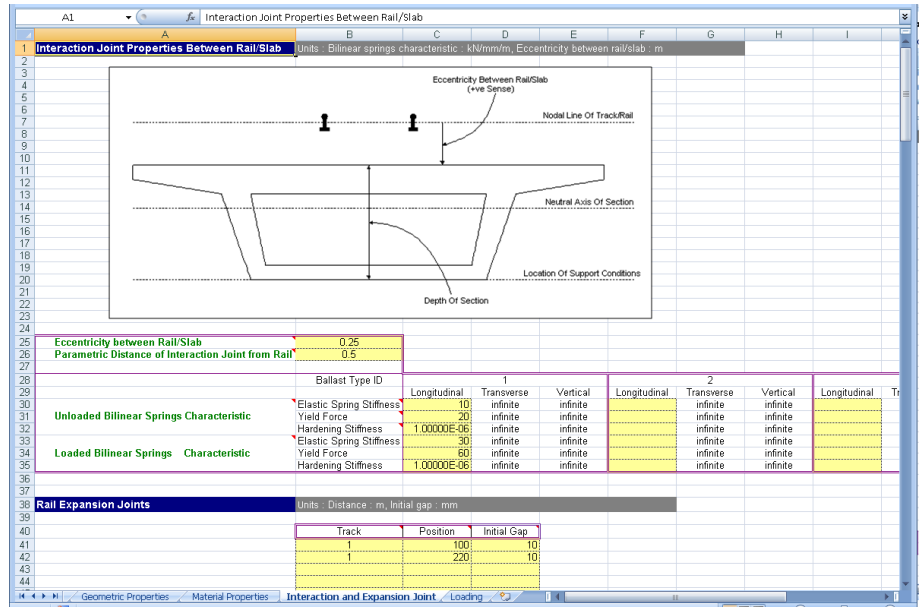


Figure 35: Interaction Properties Between the Track/Bridge and Expansion Joint Definition

The main bilinear interaction effects for the track/bridge interaction are defined in this worksheet along with additional properties associated with the rail/track. These include the eccentricity between the rail/slab (see Figure 11 and the *Geometric Properties* section) and the presence of any rail expansion joints.

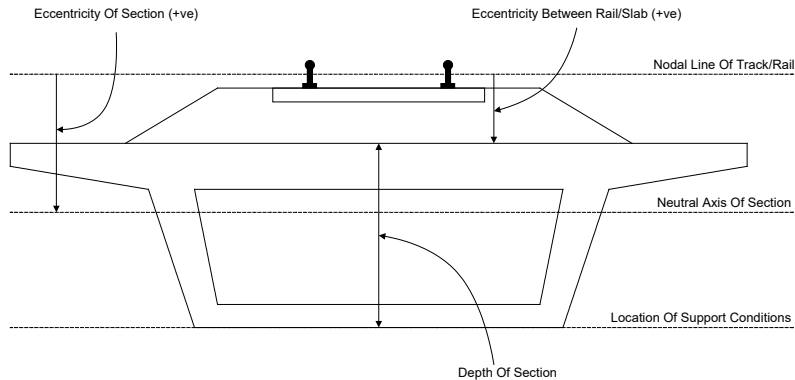
Eccentricity Between Rail/Slab

The eccentricity between the rail/slab is used to define the distance between the nodal line of the rail/track and the top of the bridge slab/deck as indicated in Figure 11. In general, all eccentricities will be positive in the modelling unless the neutral axis of the structure section is above the level of the rails. This only happens for certain types of structures and the definitions of eccentricity should generally follow the sign conventions defined in the following figure.

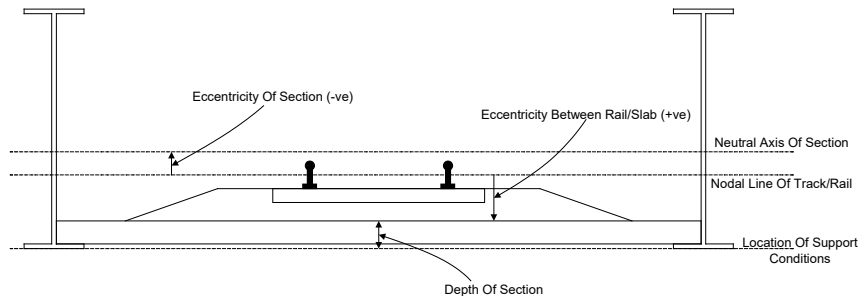
Parametric Distance of Interaction Joint from Rail

The position of the interaction joint from the rail is controlled by this entry. When the eccentricity between the rail/track and the top of the bridge slab/deck is small the eccentricity can be modelled using eccentricity in the elements representing the components of the model. For larger eccentricities the positioning of the rail/track relative to the bridge slab/deck should be modelled using rigid offsets and the positioning of the interaction joints can be set to be at the elevation of the rail/track by

setting this entry to 0, at the elevation of the bridge slab/deck by setting this entry to 1, or at any position in between by setting a value between 0 and 1. A value of 0.5 should normally be used to place the interaction joints midway between the rail/track and the bridge slab/deck. If the "Eccentricity Between Rail/Slab" entry is small then this value will not be used (as already stated).



Eccentricity Definitions (Section Neutral Axis Below Rail Level, Support At Base)



Eccentricity Definitions (Section Neutral Axis Above Rail Level, Support At Base)

Figure 36: Sign Conventions for Eccentricity Definition

Bilinear Interaction Properties

The bilinear interaction properties are derived from the bilinear curves defined in the UIC774-3 Code of Practice and it is possible to define up to five separate sets of properties by default. Properties are entered for both the unloaded state where just temperature loads are applied in the model to the track and the loaded state where both temperature and trainset loads are applied to the track. For each state of loading the elastic spring stiffness is defined in kN/mm per metre length of track, the yield force (onset of plastic yield) is defined in kN per metre length and the hardening stiffness

defined as a small value so there is no stiffness once plastic yielding has started. The values in Figure 35 are for unballasted track where the displacement between the elastic and plastic zones and the associated resistance in the plastic zone are (see the earlier discussion on the bilinear relationship):

$$\begin{aligned} u_0 &= 0.5 \text{ mm} \\ k &= 40 \text{ kN/m (Unloaded)} \\ k &= 60 \text{ kN/m (Loaded)} \end{aligned}$$

The elastic spring stiffness is calculated directly from:

$$\text{Elastic Spring Stiffness} = \frac{k}{u_0}$$

giving 80 kN / mm per m of track for the unloaded and 120 kN / mm per m of track for the loaded interaction elastic spring stiffness values.



Note. If a zero or small yield force is used in the interaction characteristics the default settings for the nonlinear convergence scheme used in the solution may not result in a converged solution. These convergence parameters may need to be adjusted and the model resolved if this occurs.

Increasing the number of bilinear interaction properties

The input spreadsheet allows the input of five different ballast types by default for the model which can be specified in the *Decks, Tracks and Embankment* and *Structure Definition* worksheets for the modelling. If more than five ballast definitions are required to fully define the variation of ballast properties characterising the track-structure-interaction then the number of definitions can be increased by copying and pasting the last bilinear definition section as many times as required as demonstrated below.



Note. This may require the worksheet to be unprotected first. This worksheet protection should be turned back on immediately after the extra entries for additional interaction properties have been inserted into the worksheet to avoid accidental changes to other parts of the worksheet that could cause errors when the spreadsheet is imported into the Rail Track Analysis tool.

In the example below we have defined four bilinear interaction properties but we need to define a total of seven. Using the fifth and final definition in the worksheet we will create the input sections for the additional two definitions required and adjust the column widths to match the rest of the worksheet.

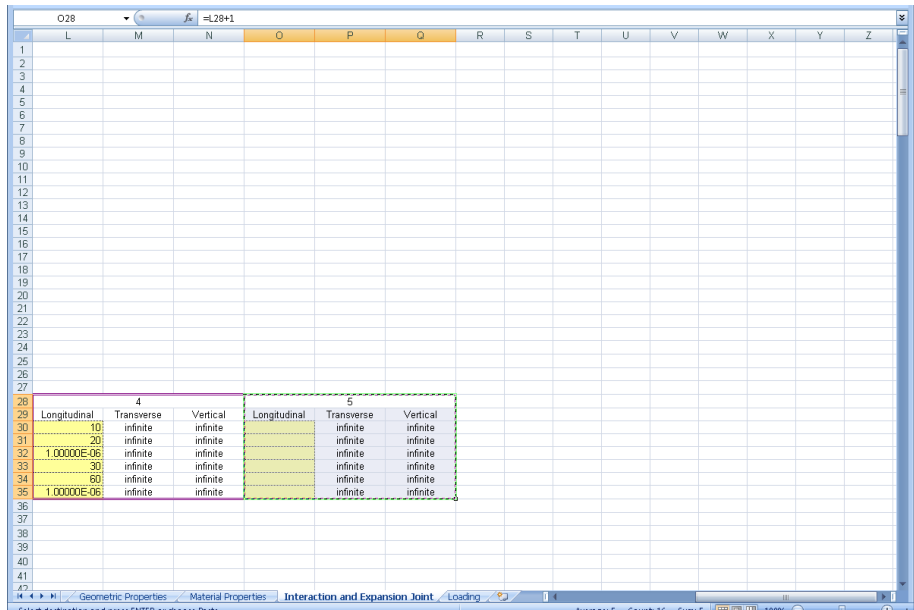


Figure 37: Select the Fifth Bilinear Definition Section

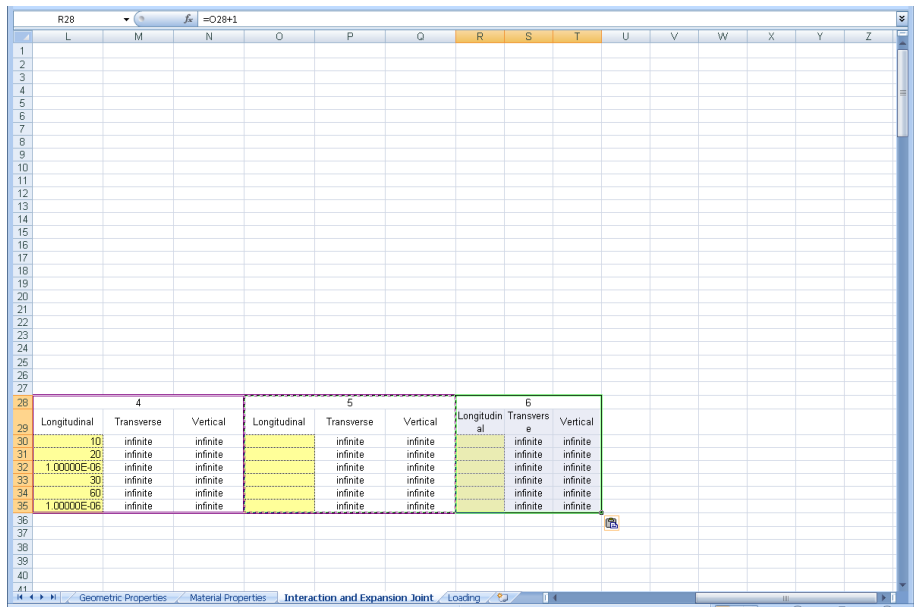


Figure 38: Paste the Bilinear Definition Section to Create the Sixth Definition

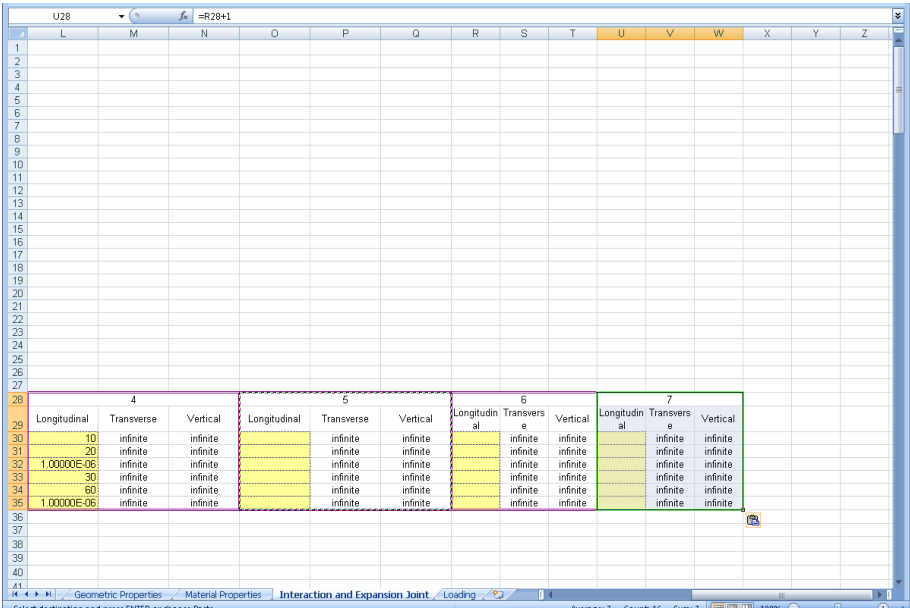


Figure 39: Paste the Bilinear Definition Section to Create the Seventh Definition

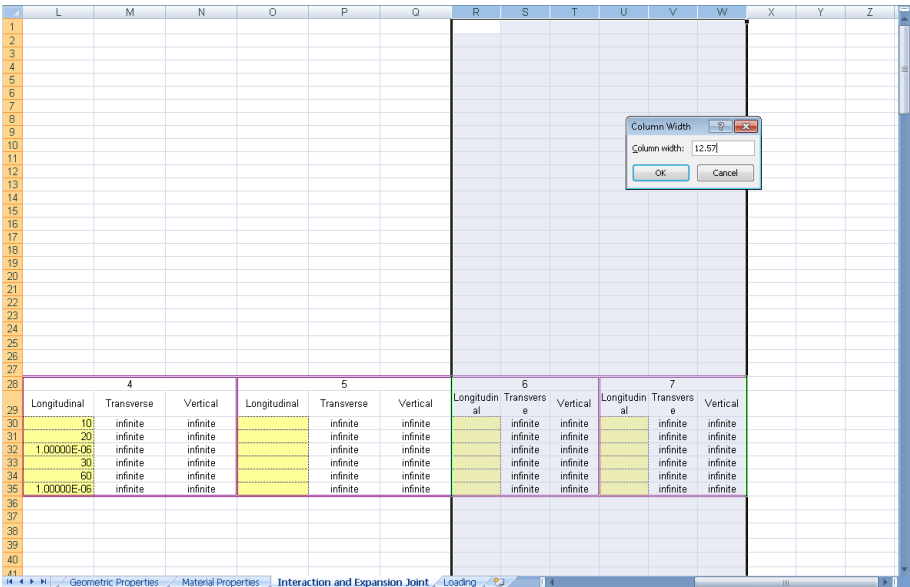


Figure 40: Select the Columns to Adjust the Column Width to Match Other Columns

ID	Longitudinal	Transverse	Vertical
10	infinite	infinite	infinite
20	infinite	infinite	infinite
30	1.00000E-06	infinite	infinite
60	1.00000E-06	infinite	infinite

Figure 41: Completed Bilinear Definitions Ready for Input

Any number of bilinear interaction definitions can be added to the worksheet up to the limit of the number of columns in the spreadsheet. The only restriction for the Rail Track Analysis tool is that the formatting / layout of the columns must be identical to the existing bilinear interaction definitions in the worksheet. When the new bilinear interaction definition section is copied and pasted into the worksheet it will automatically take the next integer ID above the previous definition.



Note. It is possible to manually edit the bilinear interaction definition integer IDs at the top of the sections and even change their order but this is not recommended. If these definition IDs are edited then the onus is entirely on the user to ensure that they are valid integer IDs and IDs are not repeated otherwise data input errors will occur.

Including Zero and/or Reduced Longitudinal Resistance Interaction Modelling

Zero Longitudinal Resistance (ZLR) and Reduced Longitudinal Resistance (RLR) interaction modelling cannot be included directly in the input spreadsheet. The inclusion of ZLR and/or RLR rail fastener modelling is usually dependent on the inspection axial stress and displacements in the rail track and these having exceeded acceptable levels. For this reason a rail track analysis must have been built and analysed (and post-processed) before the ZLR and/or RLR can be included into the modelling and is covered in detail in the section on *Performing a ZLR/RLR Rail Track Analysis*.

Defining Rail Expansion Joints

If rail expansion joints/devices are present in the bridge then the information for these can be entered into the worksheet for each track. The data input takes the form of a unique track ID number, the position and initial gap. For each track ID number the expansion joint is defined by entering the position in metres from the start of the left-hand embankment and initial gap in millimetres. The expansion joint data will be read from the spreadsheet until a blank track ID entry is detected. The expansion joints can be specified in any order.

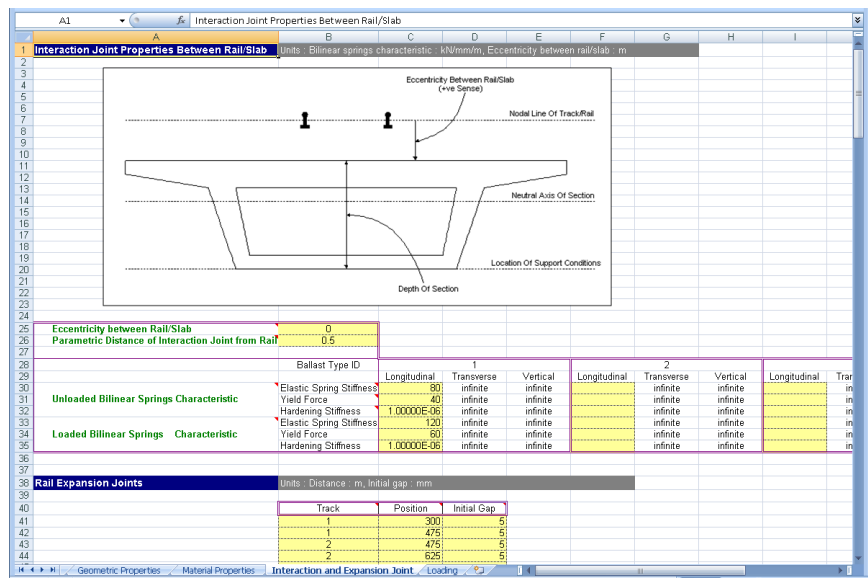


Figure 42: Sample Expansion Joint Definitions

Worksheet 6: Thermal and Train Loading

Loading												
Unit	Temperature	Celsius	Load Position/Length	m	Load	kN/m						
Temperature Loads												
Concrete Deck	Amount	30										
Steel Deck												
User Deck												
Rails	Amount	50										
Train Loads												
Number of Train Loading Groups to Analyse: 3												
Train Loading Group: 1												
Number of Track Loading Locations: 5												
Loading Type	Track Selection to be Loaded	Parametric Starting Position for Loadings	Parametric End Position for Loadings	Amount (per unit length)	Loaded Length	Starting Location of Loading for First Analysis	Finishing Location of Loading for Last Analysis	Location Increment for each Analysis	Loading Type	Track Selection to be Loaded	Part St Pos Loc	
Vertical SW0 (Left UDL)	1	-17.65	-2.65	133	15	82.35	237.65	38.625	Vertical SW0 (Left UDL)	1		
Braking SW0 (Left UDL)	1	-17.65	-2.65	20	15	82.35	237.65	38.625	Braking SW0 (Left UDL)	1		
Vertical SW0 (Right UDL)	1	2.65	17.65	133	15	82.35	237.65	38.625	Vertical SW0 (Right UDL)	1		
Braking SW0 (Right UDL)	1	2.65	17.65	20	15	82.35	237.65	38.625	Braking SW0 (Right UDL)	1		

Figure 43: Definition of Thermal and Train Loading for Structure

The loading worksheet allows the input of the temperature and trainset loading characteristics that are to be considered for the structure. This includes the capability of defining multiple trainset configurations and locations using the Train Loading Groups and parametric loading facilities which are described below.

Temperature Loading

The temperature effects in the rails for a continuously welded rail (CWR) track do not cause a displacement of the track and do not need to be considered (UIC774-3 Clause 1.4.2), only changes in temperature of the bridge deck relative to the reference temperature need to be considered for CWR track.

For all other tracks the change in temperature of the bridge deck and rails relative to the reference temperature of the deck when the rail was fixed needs to be considered in accordance to the Code of Practice and design specifications.

The temperature loads for both the slab/deck and the rail should be entered (zero if not required) in Celsius (degrees centigrade) where temperature rises are entered as positive values and temperature drops are entered as negative values.

Within the *Geometric Properties* worksheet the assignment of the geometric attributes to the decks and spans of the structure allowed the selection of whether the structural components were constructed from concrete, steel or from a user-defined fabrication

type. Within the temperature loading definitions different temperature changes from the reference temperature can be defined in the **Loading** worksheet for each of these types as shown in Figure 43. Where a deck type does not exist in the model the temperature change can be left blank or set to zero.



Note. For an analysis where more than one temperature loading may need to be entered for the same deck type either the user-defined type can be used or the model should be defined with a single deck type temperature and then a temperature only model built. This temperature only model can then have its temperature loading for the appropriate decks adjusted before the **Apply Rail Loads** dialog is then used to include the trainset loading to the rail tracks. It should however be noted that it is the responsibility of the user to ensure that such an analysis with multiple temperatures for the same deck type adheres to the appropriate Codes of Practice.

Trainset Loading to Rails of Tracks

The Rail Track Analysis tool allows the analysis of the positioning / movement of multiple trainset configurations within the same overall Rail Track Analysis. This is done through the Train Loading Groups and parametric positioning of the trainsets within each of these Train Loading Groups. This can be used for either the global passage of multiple different trainset configurations across the whole structure (such as an analysis containing SW/0, SW/2 and HSLM-A trainset configurations / loadings to assess the overall behaviour to each of these) or the targeted and / or more detailed placement of a single (or more) trainset configuration(s) at critical positions indicated by a prior global analysis or by engineering judgement.

For each of the Train Loading Groups the trainset loading is defined in terms of the type, track to load, position and magnitude. The loading allows for multiple trainset loading positions to be defined in each Train Loading Group and all of these positions will be analysed in one model by the Rail Track Analysis tool.

Since trainset configurations can be longer than the approach embankment recommendations of UIC774-3 (and in some cases could be significantly longer than the approach embankment and structure) the Rail Track Analysis tool allows the trainset loading to fall outside the extents of the model.

Currently the **Loading** worksheet of the input spreadsheet allows up to 10 Train Loading Groups (each with formatted input of 125 rows of loading definitions to describe the longitudinal and vertical loading pattern) to be defined within the formatting.

As many rail/train loads that are required can be defined in the spreadsheet with data input terminating when blank data is detected in the loading type column. This allows more complex loading patterns to be defined such as those illustrated in Figure 44 and “Appendix B: Definition of Complex Trainset Configurations”. To extend the bottom of the table beyond the 125 loading definitions extra rows can be inserted (making sure to copy the formulae in columns G and J for Train Loading Group 1 and similarly for others) or the last rows copied and pasted as many times as required.

Similarly, should the number of Train Loading Groups need to be increased from the 10 provided in the template this can be done by selecting the whole of the region defining the tenth Train Loading Group (as indicated in Figure 45) and pasting it as many times to the right of the existing Train Loading Groups (as indicated in Figure 46).



Note. This may require the worksheet to be unprotected first. This worksheet protection should be turned back on immediately after the extra entries for additional loads have been inserted into the worksheet to avoid accidental changes to other parts of the worksheet that could cause errors when the spreadsheet is imported into the Rail Track Analysis tool.

The inputs to the worksheet are:

Number of train loading groups to analyse

This defines the number of Train Loading Groups to include in the analysis. If only a single trainset configuration is to be considered then this should be set to 1. To analyse more than one Train Loading Group the number should be set to a positive integer equal to (or less than) the number of Train Loading Groups that have been defined in the worksheet. No breaks / gaps are permitted in the definition of the Train Loading Groups.

Then, for each of the Train Loading Groups the inputs are:

Number of track loading locations

This defines the number of parametric locations for the placement of the trainset loading carried out in the analysis of this Train Loading Group. If only a single position of the trainset loading is to be considered then this should be set to 1. To analyse more than one location the number should be set to a positive integer.

Loading type

This defines the loading type that will be assigned to the selected track. The first character governs the loading type with valid options being **A**cceleration or **T**raction, **B**raking and **V**ertical. A more descriptive definition of the loading type may be entered if required as illustrated in “Appendix B: Definition of Complex Trainset Configurations” so long as the first character in the description is set to either A, B, T or V.

Track selection to be loaded

This defines the track that the loading will be assigned to for the current Train Loading Group and can be any of the tracks within the model.

For structures supporting two or more tracks the UIC774-3 Code of Practice (Clause 1.4.3) and “Eurocode 1: Actions on Structures – Part 2: Traffic loads on bridges (EN 1991-2:2003)” state that the braking forces on one track shall be considered with the acceleration/traction forces on one other track. In addition, “Eurocode 1: Actions on

Structures – Part 2: Traffic loads on bridges (EN 1991-2:2003)” states that where two or more tracks have the same permitted direction of travel either traction on two tracks or braking on two tracks shall be taken into account. Other codes of practice may have different conditions that need to be considered.

Parametric starting position for loadings

This defines the starting parametric position of the loading of the trainset for the current Train Loading Group. For the trainset the starting position is the left-most position of the load when considering the trainset alone (i.e. independent of the structure). The reference parametric position used for the combination of the trainset loading and the current position on the structure is at a value of zero so positions that are negative will place the defined loading to the left of the reference position defined using the entries in columns H and I and positions that are positive will place the loading to the right.

Parametric end position for loadings

This defines the ending parametric position of the loading of the trainset for the current Train Loading Group. For the trainset the ending position is the right-most position of the load when considering the trainset alone (i.e. independent of the structure). These are relative to the reference position as described for the parametric starting position above.

Amount (per unit length)

This defines the magnitude of the trainset loading in units of kN per metre length for the current Train Loading Group. For longitudinal loads such as acceleration, traction and braking loads a positive value will cause the loading to act towards the right embankment, a negative value will cause the loading to act towards the left embankment. For vertical loads a positive value will cause the loading to act downwards onto the track and structure.

Loaded length

The loaded length is automatically calculated from the parametric starting and end position for the loading and provides a check that these values have been entered correctly. Negative or zero loaded lengths are not permitted in the modelling.

Figure 44 illustrates some trainset loading configurations and their input into the worksheet. Examples (d) and (e) in this figure are equivalent and both definition methods are equally valid in the worksheet. Further examples are illustrated in “Appendix B: Definition of Complex Trainset Configurations”.

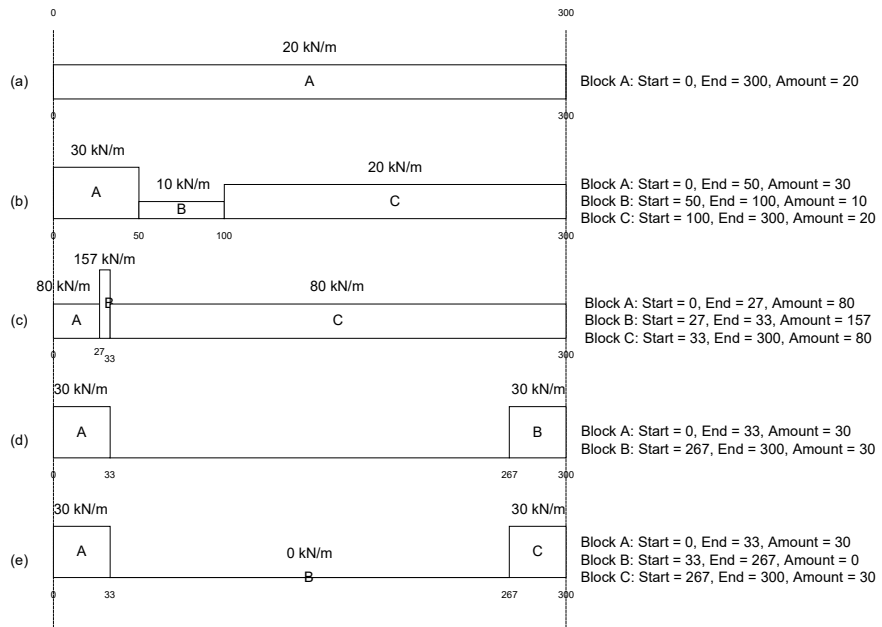


Figure 44: Sample Trainset Loading Position Definitions



Note. It is possible to approximate concentrated loads in trainset loading configurations through the use of UDLs over small contact lengths. Due to the scale of the modelling, with elements typically 1 to 2m in length, the use of a small contact length (such as 5 to 10% of the element length or smaller) allows the concentrated load to be modelled. The procedure for modelling concentrated loads within the Rail Track Analysis tool is covered in “Appendix B: Definition of Complex Trainset Configurations”.

Starting location of loading for first analysis

This defines the starting location of the reference position of the parametric trainset loading on the track for the first analysis for the current Train Loading Group. The location should be defined from the left-most end of the left-hand embankment which is at a location of 0.0m.

The starting position can be defined outside the limits of the rail track. A negative value will place the reference position of the trainset before the left-most end of the left-hand embankment and a value greater than the total track length (available from the Decks, Tracks and Embankment worksheet of the input spreadsheet) will place it after the right-most end of the right-hand embankment.

Any trainset loading outside of the model extents (embankment lengths) will be excluded from the track-structure-interaction analysis.

Finishing location of loading for last analysis

This defines the finishing location of the reference position of the parametric trainset loading on the track for the last analysis for the current Train Loading Group. The location should be defined from the left-most end of the left-hand embankment which is at a location of 0.0m.

The finishing position can be defined in a similar manner to the starting position described above. Any trainset loading outside the model extents (embankment lengths) will be excluded from the track-structure-interaction analysis.

Location increment for each analysis

The location increment for the loading for each analysis is automatically calculated from the starting and finishing locations of the loading and the defined number of track loading locations. All of the loading for a given track should have the same increment to ensure that each component of the loading moves as a group. Generally the starting and finishing locations for the reference position of the loading for a given track should be identical for that track. Different location increments are possible between tracks when more than one track is analysed with positive location increments indicating that the trainset is moving from left to right and negative location increments indicating that the trainset is moving from right to left.

For a single track structure the trainset loading may be stationary (location increment = 0.0m) but for this condition the number of track loading locations must be set to 1. For a two or more track structure, one of the trainsets on one of the tracks may be stationary but an error will result if all trainset loading the tracks are stationary if the number of track loading locations is greater than 1. To analyse multiple stationary trainsets on a two or more track structure the number of track loading locations must be set to 1.

CC	CD	CE	CF	CG	CH	CI	CJ	CK	CL	CM	CN	CO	CP	CQ
1														
2														
3														
4														
5														
6														
7														
8														
9														
10														
11														
12														
13														
14														
15														
16														
17														
18														
19														
20														
21														
22														
23														
24														
25														
26														
27														
28														
29														
30														
31														
32														
33														
34														
35														
36														
37														

Figure 45: Adding Extra Train Loading Groups (Copy)

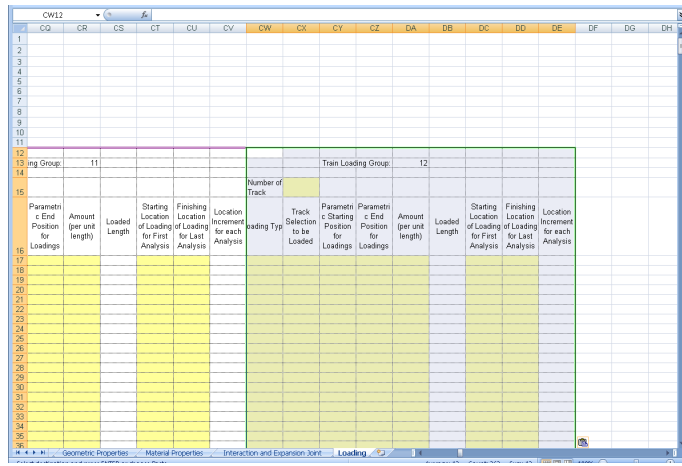


Figure 46: Adding Extra Train Loading Groups (Paste)

Rail Track Analysis Menu Options

The Rail Track Analysis option is accessed through the Bridge menu by selecting the Rail Track Analysis entry. This menu entry provides the following five options:

- ☐ Build UIC774-3 Model...
- ☐ Apply Rail Loads...
- ☐ Extract Results to Excel...
- ☐ Define ZLR/RLR Properties...
- ☐ Define ZLR/RLR Regions...

Build UIC774-3 Model Dialog

Model units are specified on the 'Decks, Tracks and Embankments' worksheet and can be specified as either 'N,m,kg,s,C' or 'kip,ft,kslug,s,F'. The first row of each worksheet states the units in use. Note that, by design, changing the model unit units in use (on the 'Decks, Tracks and Embankments' worksheet) does not convert the values in the spreadsheet.

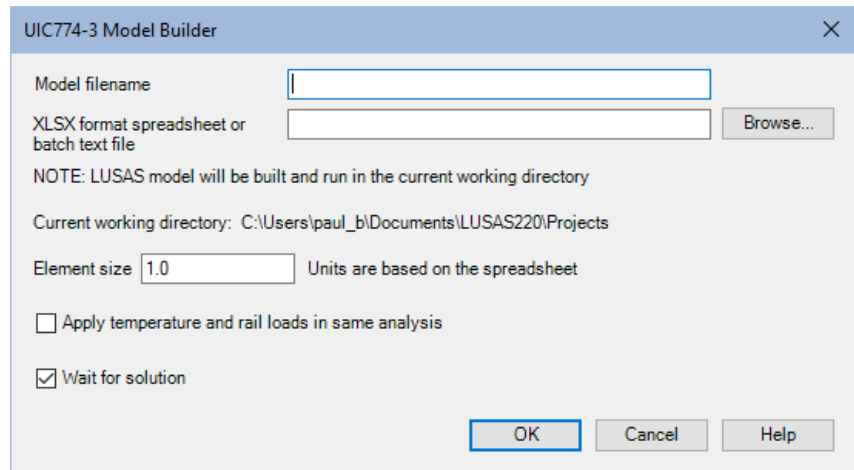


Figure 47: UIC774-3 Model Builder Dialog

- ☐ **Model filename** The model filename for the analysis should be entered into the box if batch processing is not being used (see below). The file should not contain any folder specification as all models created will be placed in the current working folder indicated on the dialog.
- ☐ **XLSX format spreadsheet or batch text file** If batch processing is not being used and a single model is being created, the filename of the spreadsheet that will be used to define the analysis must be entered into the box (including file extension). If no folder structure is specified, the spreadsheet should be located in the current working folder. Alternatively, the Browse... button may be used to locate the spreadsheet.

If batch processing of multiple models is being performed, then a batch text file listing the spreadsheets to use for defining the models should be entered into the box (must have a *.txt file extension). The batch text file can be entered explicitly into the dialog or located using the Browse... button and selecting “Batch text file (*.txt)” as the file type.

For batch processing, the batch can contain spreadsheets with different units.

The format of the batch text file is indicated below and simply contains a TAB delimited list of the spreadsheet files to build the models from and an optional LUSAS model name (if no model name is supplied the basename of the Excel or compatible XLSX spreadsheet will be used) with one model entry per line. If no folder structure is defined for the spreadsheet files then the current working folder will be assumed to contain them, otherwise they may exist at any folder level on the computer system. If a spreadsheet file cannot be found or contains invalid data it will be skipped in the batch processing and an error reported in the “UIC774-3_BuildModel.log” file created in the

current working folder. Blank lines are ignored and batch processing will terminate at the end of the batch text file. The number of analyses in the batch process is unlimited.

In the example below the first model built from the Bridge1.xlsx spreadsheet will be called LUSAS_Bridge1.mdl, the second model will take its basename from the spreadsheet and will be called Bridge2.mdl and the third model will be called RTA_Bridge3.mdl.

```
Bridge1.xlsx      LUSAS_Bridge1
..\SomeFolder\Bridge2.xlsx
D:\Project\Spreadsheet\Bridge3.xlsx  RTA_Bridge3
```

Figure 48: Example Batch Text File With Three Bridges To Build

- ☐ **Element Size** The element size to use in the finite element mesh should be specified in this box. According to the UIC774-3 Code of Practice, the maximum element size that is permitted in an analysis is 2.0m (Clause 1.7.3). The dialog therefore generally allows element sizes of $0 < \text{Element Size} \leq 2.0\text{m}$ (or $0 < \text{Element Size} \leq 6.56168\text{ft}$ in the case of US units) for the building of the models. Larger element sizes can be used (up to the length of the smallest bridge deck span) but a warning will be issued about non-compliance with the UIC774-3 Code of Practice. In the case of a batch text file input for multiple input spreadsheets, the units shown in the dialog will be based upon the first indicated spreadsheet.



Note. For large bridges and/or embankments the use of small element sizes can generate excessively large models which take significant time to manipulate / solve. Use of element sizes below 1.0m should be used with caution.

- ☐ **Apply temperature and rail loads in same analysis** Two analysis types are available from the model building dialog. These are:
- The solution of the combined temperature and rail loading effects (option turned on)
 - The solution of just the temperature effects (option turned off)

If only a single rail loading configuration is going to be analysed for a particular model then this option should be switched on.

If, on the other hand, a range of rail loading configurations needs to be applied to a model (for different train positions with varying braking / accelerating loading configurations) then this option should be turned off to allow the rail loads to be applied separately by the **Apply Rail Loads** dialog described below.

Building a model to solve only temperature effects also allows the structural model to be updated prior to applying the rail loading. A situation where this may be needed is

the case where full representation of piers has been included in the track-structure-interaction model rather than the simplified longitudinal equivalent spring approach and the support conditions need be modified for pier foundations to change them from full fixity to a rotational stiffness (see the discussion of the ***Structure Definition*** section of the Excel or compatible XLSX spreadsheet). Other situations may be the need to incorporate varying cross-sections to the decks and spans of the structure (see section “***Varying Section Geometric Properties***”) or the addition of girder modelling or additional detailing to the basic deck modelling provided by the Rail Track Analysis tool which couldn’t be included within the spreadsheet input (although such additional modelling must be carried out with caution). All of these are possible when a “temperature effects only” model is built in the Rail Track Analysis tool.



Caution. Models created from the original spreadsheet data contain named groups that are used in the creation of results worksheets. Care should be taken to avoid making changes to these groups, the definition/layout of the track-structure-interaction between the tracks and the decks and the loadcases themselves otherwise the application of the rail loading and post-processing may fail. It is also advisable to keep backups of the models and, unless you have extensive experience of modifying Rail Track Analysis models, regularly test the modifications that are made to the model to ensure at minimum that a single trainset loading can still be applied to the rails and post-processed (this will avoid spending a lot of time making modifications to the model only to ultimately find that you have invalidated the track-structure-interaction model for the Rail Track Analysis tool).

- ☐ **Wait for solution** If the option to wait for the solution is selected then all of the analyses will be run from Modeller and nothing can be carried out in the current Modeller window until the solution has finished. For relatively small structures or analyses with a limited set of parametric trainset loading locations this is may be fine. If a large number of parametric trainset loading locations are included in an analysis and/or a large number of models are being built using the batch processing, then waiting for the solution can take a considerable amount of time. Under this situation the wait for solution option can be turned off which will cause the analyses to be built and run but the Modeller application will be free for additional tasks.



Caution. You should not attempt to run another rail track analysis in the same folder as an existing analysis is being built or solved. Attempting to do this will corrupt the current analysis that is being built or solved. If sufficient LUSAS / rail track analysis licenses are available on the machine that is being used, then additional rail track analyses can be performed so long as each analysis is performed in a different folder.

Apply Rail Loads Dialog

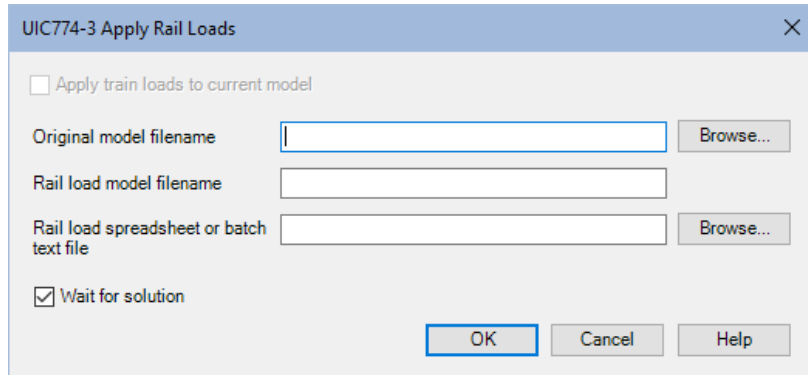


Figure 49: UIC774-3 Apply Rail Loads Dialog

If the bridge model was built and solved with only the temperature loads (**Apply temperature and rail loads in same analysis** turned off in model building dialog) then this model can subsequently be used for applying rail load configurations using this dialog. The dialog should not be used for models that have been built with both the temperature and rail loading applied and will report an error if attempted.

- ☐ **Apply train loads to current model** If the current model loaded was generated from the **Build Model...** dialog with the **Apply temperature and rail loads in same analysis** option turned off then this option can be selected. If this option is not selected then the **Original model filename** entry is available for manual selection of the original model containing only temperature loads.
- ☐ **Original model filename** If a single rail load configuration is to be analysed and the currently loaded model is not being used, the original model filename should be entered into the box. Alternatively, the Browse... button can be used to locate the original model file containing only the temperature loading. For batch processing the original model filename is ignored.
- ☐ **Rail load model filename** If a single rail load configuration is to be analysed the new filename for the model incorporating the temperature and rail loads should be entered into the box. This filename can contain the path name for the model location (folder must exist) but should generally only have the filename defined which will then be saved in the current working folder. This filename can be the same as the original model filename but should generally be different to allow the temperature loading model to be reused for another rail load configuration. For batch processing the new rail load model filename is ignored.
- ☐ **Rail load spreadsheet or batch text file** If a single rail load configuration is to be analysed for the specified bridge model the filename of the Excel or compatible XLSX format spreadsheet containing the required loading should be

entered into the box. Alternatively the Browse... button can be used to locate the file. Once the spreadsheet has been specified the OK button can be clicked to carry out the modification of the original bridge model to include the combined effects of the temperature and rail loading. The units in the selected XLSX format spreadsheet must match the units the Rail Track Analysis model was built with.

If multiple models and/or multiple rail load configurations are to be analysed, then only the batch text file (which must have a *.txt file extension) listing the information required by the software should be entered into this box.

Alternatively, the Browse... button can be used, selecting “Batch text file (*.txt)” as the file type.

For each model/rail configuration analysis the batch text file should contain a separate line of data. Each line should specify the original temperature model, the new combined loading model to create, and the XLSX format spreadsheet that contains the rail configuration definition. Each item on a line should be TAB delimited to allow spaces to be used in the filenames. An example batch text file is shown below.

Bridge1.mdl	Bridge1_RailConfig1.mdl	Bridge1_RailConfig1.xlsx
Bridge1.mdl	Bridge1_RailConfig2.mdl	Bridge1_RailConfig2.xlsx
Bridge1.mdl	Bridge1_RailConfig3.mdl	Bridge1_RailConfig3.xlsx
Bridge1.mdl	Bridge1_RailConfig4.mdl	Bridge1_RailConfig4.xlsx
Bridge2.mdl	Bridge2_RailConfig1.mdl	Bridge2_RailConfig1.xlsx
Bridge2.mdl	Bridge2_RailConfig2.mdl	Bridge2_RailConfig2.xlsx
Bridge3.mdl	Bridge3_RailConfig1.mdl	Bridge3_RailConfig1.xlsx

Figure 50: Sample Rail Loading Batch Text File

In the above example, three different bridge deck temperature models have been selected and four rail load configurations analysed for the first, two rail load configurations for the second and one rail load configuration for the third. The number of entries in the batch text file is unlimited and batch processing will terminate once the end of the file is reached. If any analysis fails due to missing or invalid files an error will be reported to the “UIC774-3_RailLoads.log” file in the current working folder.



Note. If the batch text file method is being used the **Apply train loads to current model** option will be ignored since the list of temperature only models to use for the applying of the rail loads for each of the analyses is contained within the batch text file.

- ☐ **Wait for solution** If the option to wait for the solution is selected then all of the analyses will be run from Modeller and nothing can be carried out in the current Modeller window until the solution has finished. For relatively small structures or analyses with a limited set of parametric trainset loading locations this is may be fine. If a large number of parametric trainset loading locations are included in an analysis and/or a large number of models are being built using the batch

processing then waiting for the solution can take a considerable amount of time. Under this situation the wait for solution option can be turned off which will cause the analyses to be built and run but the Modeller application will be free for additional tasks.



Caution. You should not attempt to run another rail track analysis in the same folder as the one where an existing analysis is being built or solved. Attempting to do this will corrupt the current analysis that is being built or solved. If sufficient LUSAS / rail track analysis licenses are available on the computer that is being used, then additional rail track analyses can be performed so long as each analysis is performed in a different folder.

Extract Results to Excel Dialog

Figure 51: UIC774-3 Post Processor Dialog

A dedicated post-processing dialog is provided that allows the automatic extraction of the results from the track/bridge interaction analysis to an XLSX format spreadsheet. On start-up, if nothing is selected in Modeller, the dialog will inspect the active model to ensure that there are results present and also detect whether the UIC774-3 groups defined during the model building process are present in the Groups Treeview. For this reason any manual editing of the model should be kept to a minimum and the track groups (for example “Track 1”, “Track 2”), deck group (“Decks”) and interaction joint groups (for example “Interaction Springs - Track 1”) should not be modified or renamed.

- ☐ **Filename** The filename for the XLSX format spreadsheet that will be created should be entered into this box. The filename must not have any folder structure specified as the file will be placed in the folder selected below.

- ☐ **Working folder / Save In** If the spreadsheet is to be saved in a folder other than the current working folder then the User defined option can be selected and the required folder entered into the box or browsed for using the ... button.
- ☐ **Output control** The output from the post-processor can be customised. By default all output for all tracks and all Train Loading Groups/positions in the analyses are output to the spreadsheet with charts. For very large analyses this can not only take time, but it can also exceed the memory limits. The **Included model extent** allows the selection of the tracks / Train Loading Groups / track extent to be controlled for the post-processing. Further options are also included to control the generation of the envelopes / peak result tables and the generation of individual charts within the post-processing.
- ☐ After clicking **OK** the software will perform the requested post-processing and generate a XLSX format spreadsheet in the chosen output folder.



Output Control

The automatic post-processor allows the output extracted from the track-structure-interaction analysis to be customised. This is particularly useful for very large models that may include long structures where specific decks need to be interrogated or where only specific train loading configurations of a larger parametric study need to be considered. Within the **Output control** input of the post-processor the options to perform enveloping/peak summary tables and charting may also be adjusted.

Included model extent

By default all tracks, all Train Loading Groups and the whole track length will be included in any post-processing, and this will be reported in the **Included model extent** textbox when the post-processor is run for the first time on a model as indicated in Figure 51. To change the selected output extent click on the **Modify...** button to display the **Modify Output Control** dialog shown in Figure 52. In this dialog the tracks, Train Loading Groups and track extent to be post-processed can all be selected as illustrated in Figure 53. On clicking the **OK** button in the **Modify Output Control** dialog the main post-processing dialog will mirror the selection in the **Included model extent** textbox (Figure 54).

These settings will be saved with the model and will be available the next time model is loaded, and the post-processing dialog is started to post-process a different track / Train Loading Group / extent of track.

The default settings of outputting all tracks, all Train Loading Groups and the whole rail track length can be reset by clicking the **Defaults** button in the **Modify Output Control** dialog.

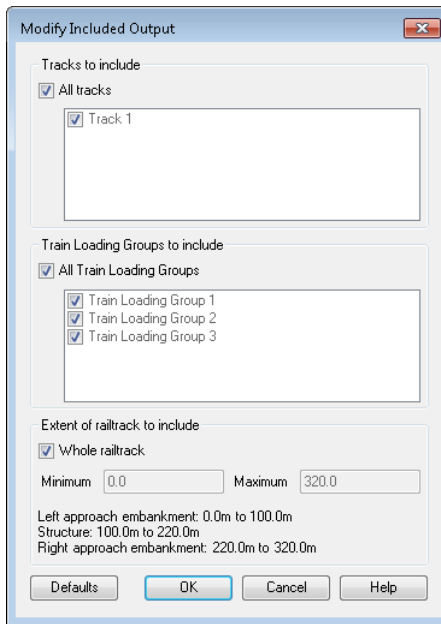


Figure 52: Modify Included Output Dialog

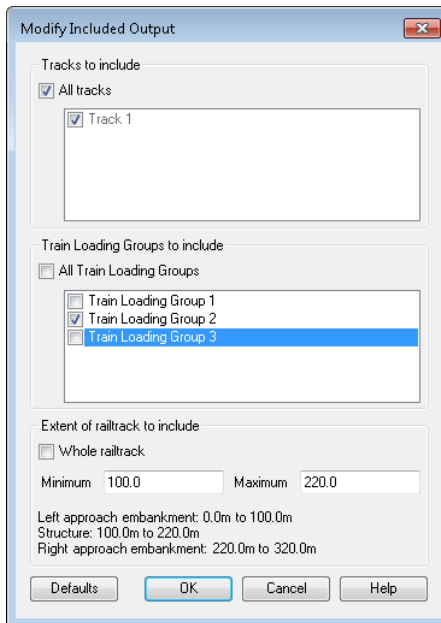


Figure 53: Train Loading Group 2 and Structure Selected Only

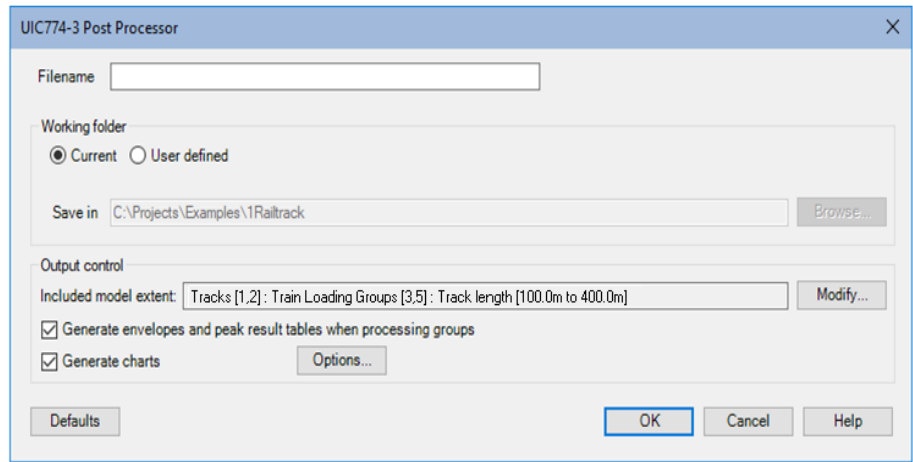


Figure 54: Revised Main Post Processor Dialog

Generate envelopes and peak result tables when processing groups

This option allows the post-processor to perform enveloping prior to outputting the results of these (including charts) to the final XLSX spreadsheet itself. The key advantage of this is that the quantities output can also include derived quantities such as the longitudinal relative railbed displacement (displacement of the track relative to the bridge deck / embankment).

As part of this enveloping operation the post-processor also generates peak result tables for quantities such as the longitudinal relative railbed displacement, displacements between the ends of bridge decks, longitudinal reactions and track axial stresses to allow comparison of the peak observations for each Train Loading Group / trainset position considered with the Code of Practice limits (see section “*Additional Results from Enveloping*” for more information).

Generate charts

By default the post-processing will create charts for all of the key quantities in the output XLSX spreadsheet generated for all of the tracks, Train Loading Groups and track extent selected. Clicking on the *Modify...* button will allow the included charts to be adjusted from the defaults shown in Figure 55.

The track charts available for output are:

- ☐ ***Railbed / track / deck*** Plots the longitudinal displacements of the track and the structure along with the longitudinal relative railbed (displacement of the track relative to the deck) on a single chart.
- ☐ ***Axial rail stress (single track)*** Plots the axial stress for the track that is currently being post-processed.

- ❑ ***Axial rail stress (multiple tracks)*** Plots the axial stresses for the current track being post-processed and all other tracks being post-processed. The chart has two further display options to control the legibility of the chart when the number of tracks plotted on the same chart increases.

Limit for all curves to have peaks labelled controls the maximum number of curves (tracks) allowed in the chart for all of them to still have the peak value labels included. If the number of tracks plotted exceeds this value, then no track plots will have the peaks labelled.

Limit on total number of curves in chart controls the maximum number of curves (tracks) allowed in the chart. If the number of tracks to be plotted exceeds this value, then the multiple track axial rail stress chart will be excluded from the post-processing spreadsheet.

The deck charts available for output are:

- ❑ ***Longitudinal displacement*** Plots the longitudinal displacement of the deck of the structure where the track-structure-interaction occurs between the structure and the ballast. This is generally the “top of the slab” for most decks. These displacements are at the nodal line in the Finite Element model (the geometric sections are modelled eccentric to this with rigid offsets to ensure correct support locations) and they are not the displacements at the neutral axis or the displacements at the bearings.
- ❑ ***Vertical displacement*** Plots the vertical displacement of the deck of the structure where the track-structure-interaction occurs.
- ❑ ***Rotational displacement*** Plots the rotation of the deck of the structure where the track-structure-interaction occurs.
- ❑ ***Axial force*** Plots the axial force in the deck of the structure.
- ❑ ***Shear force*** Plots the vertical shear force in the deck of the structure.
- ❑ ***Bending moment*** Plots the vertical bending moment in the deck of the structure.

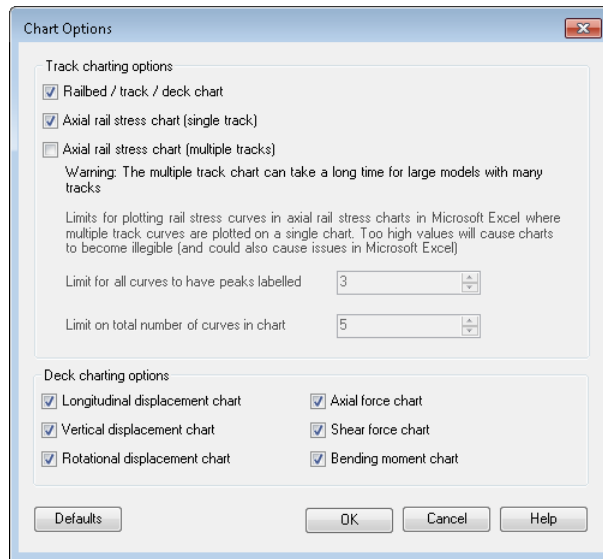


Figure 55: Chart Options Dialog

Define ZLR/RLR Properties Dialog

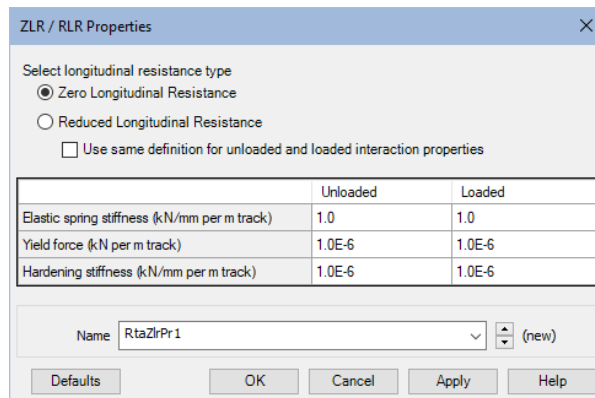


Figure 56: ZLR/RLR Property Definition Dialog

If Zero Longitudinal Resistance (ZLR) and/or Reduced Longitudinal Resistance (RLR) regions are to be included in the track-structure-interaction modelling, then the definitions of the ZLR and/or RLR properties need to be created using the **ZLR/RLR Properties** dialog.

- ☐ **Zero Longitudinal Resistance** For a rail fastener connection which provides effectively frictionless movement of the rail in the longitudinal direction. The default properties can be modified if minor resistance is observed or if the rail fastener is able to resist some longitudinal load when the train loading is present (under the “Loaded” condition).
- ☐ **Reduced Longitudinal Resistance** For a rail fastener connection/ballast system that provides reduced resistance in the longitudinal direction compared to the original system modelled in the track-structure-interaction model. See below for defaults.
- ☐ **Use same definition for unloaded and loaded interaction properties** If selected, only a single set of bilinear interaction properties needs to be defined which applies to both the Unloaded (temperature only) and the Loaded (temperature and train loading) conditions. If the option is not selected (the default), then separate bilinear interaction properties are defined for the two conditions.
- ☐ **Name** Enter a unique attribute name for the ZLR/RLR property. The ZLR/RLR property definition will appear under the “Rail Track Analysis>ZLR/RLR Properties” entry in the  Utilities Treeview.

The input for the ZLR and RLR property definitions is the same as the input for the original Excel or compatible XLSX format spreadsheet described in the ***Bilinear Interaction Properties*** sub-section under the ***Worksheet 5: Interaction and Expansion Joint Properties*** section.

For a RLR resistance type the default properties for a model that has a single ballast type will be the original properties that were input into the spreadsheet that was used to build the Rail Track Analysis model. This makes it easy to define the reduced resistance attribute as these values can then be modified using standard formulae such as $0.5 * Val$ where Val is the default number that has been placed into the dialog. Clicking the “Defaults” button for a model with a single ballast type will populate the RLR properties with these original spreadsheet values again.

For a RLR resistance type for a model with multiple ballast types there will be no default properties and clicking the “Defaults” button will clear the dialog for this type of model. When a Rail Track Analysis model has multiple ballast types, the dialog is unable to determine which ballast type the default should be returned for.



Note. The hardening stiffness for all resistance types is normally set to a very small number, default = $1.0E-6$ kN/mm per m track, to ensure perfectly plastic yielding without numerical issues. Setting a larger hardening stiffness will cause plastic hardening after yielding and usually incorrect results from the Rail Track Analysis.

Define ZLR/RLR Regions Dialog

Extent of track-structure-interaction model
 Left approach embankment: 0.0m to 300.0m
 Structure: 300.0m to 625.0m
 Right approach embankment: 625.0m to 925.0m

Model ZLR / RLR Regions

Track	Start Position from Left End of Track	End Position from Left End of Track	ZLR/RLR Property
1	550	625	1:ZLR_Zone
2	550	625	1:ZLR_Zone

1:ZLR_Zone
 2:RLR_Zone1
 3:RLR_Zone2

Add
 Delete

Name: RtaZlrRe1 (new)

OK Cancel Apply Help

Figure 57: ZLR/RLR Region Definition Dialog

Any ZLR and/or RLR regions are defined using the **ZLR/RLR Regions** dialog. A region contains all of the zones of different longitudinal resistances (ZLR and/or RLR) that define the entire changes to the original bilinear track-structure-interaction definitions that were created from the original input spreadsheet used to build the Rail Track Analysis model. If it is selected for the Rail Track Analysis, a ZLR/RLR Region definition will overwrite the original track-structure-interaction definitions over the zones that have been specified in the region definition.

Each region definition includes one or more of the following entries to define a zone within the region:

- ☐ **Track** The rail track that the current ZLR/RLR zone applies to.
- ☐ **Start Position from Left End of Track** The start (left end) of the current ZLR/RLR zone relative to the far left end of the track / start of the left-hand approach embankment.
- ☐ **End Position from Left End of Track** The end (right end) of the current ZLR/RLR zone relative to the far left end of the track / start of the left-hand approach embankment.
- ☐ **ZLR/RLR Property** Name of the ZLR/RLR property to use for the current zone.

The final input for the region definition is:

- ❑ **Name** Enter a unique attribute name for the ZLR/RLR region. The ZLR/RLR region definition will appear under the “Rail Track Analysis>ZLR/RLR Regions” entry in the  Utilities Treeview.

To add a new ZLR/RLR zone click the **Add** button. Select the required rail track for the new zone from the list and enter the required start and end positions then select the required ZLR/RLR property from the available list. To delete zones from the region definition, select cells in the rows of the grid that you wish to delete and click the **Delete** button.

The start and end of the modified longitudinal resistance zones for each rail track are defined relative to the left end of the rail track (relative to the start of the left approach embankment). This allows zones of ZLR or RLR to be placed anywhere within the length of the model. To assist with the placing of the zones a summary of the key model geometry is provided above the main input table in the dialog.

The ZLR/RLR property is selected from the properties that have been previously defined in the **ZLR / RLR Property** definition dialog.

If a ZLR/RLR zone is specified later in the region definition that overlaps a previous ZLR/RLR zone for the same rail track, the new ZLR/RLR zone will overwrite the previous zone where the overlap occurs in the definition for that rail track.

A ZLR / RLR region will not affect the behaviour of the track-structure-interaction model until it is set active. Only a single ZLR / RLR region can be active in the model.

Within a single model it is possible to define more than one region should a master model be needed for a sensitivity study – this will be discussed more in the section below on how to use ZLR/RLR modelling.

Exporting/Importing ZLR/RLR Data from Models

Where a set of ZLR/RLR property and potentially ZLR/RLR region definitions need to be shared across multiple models the data export/import tools within Modeller can be used to store the definitions within a library. All or just part of the data within the library can then be transferred from one model to the other via the library. The tools are accessed from the **File > Import/Export Model Data...** menu entry.

Figure 58 shows an example of the exporting of the full definition of a combined ZLR/RLR region with its associated ZLR and RLR property definitions from a model. For a different rail track analysis model Figure 59 shows that the library has been selected for importing. For this model only the ZLR and RLR properties are going to be imported though and not the region.

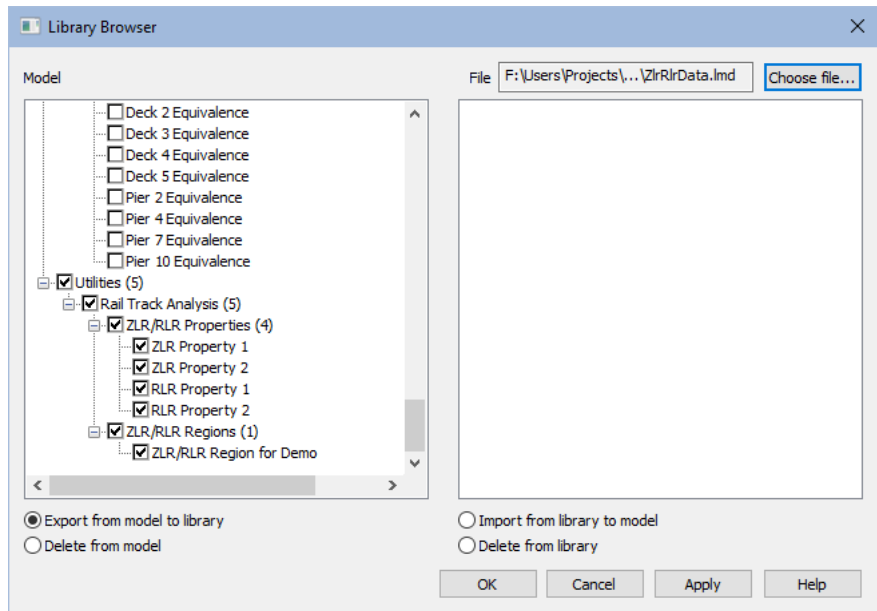


Figure 58: Exporting the ZLR and RLR Properties and Region

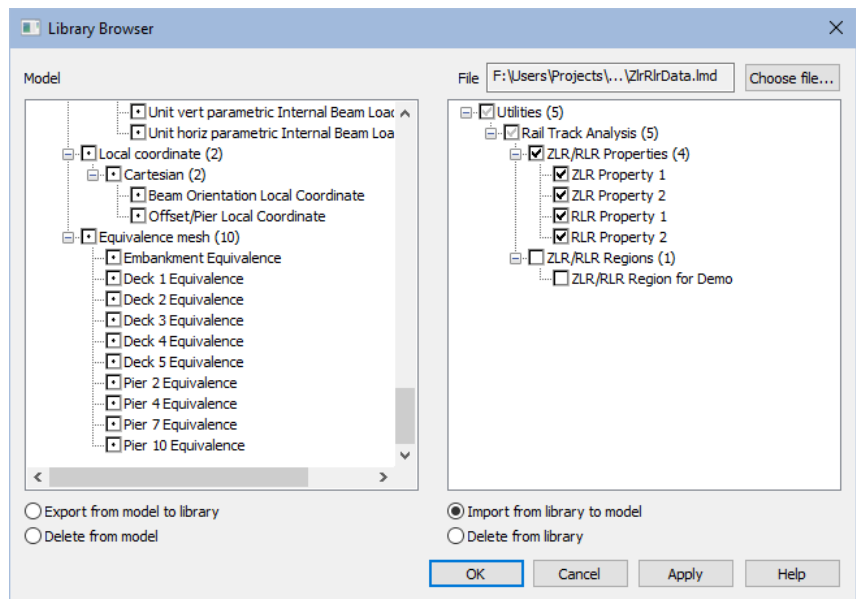


Figure 59: Importing the ZLR and RLR Properties Only



Note. Care should be taken when importing both RLR properties and ZLR/RLR regions from libraries. RLR properties may be specific to the track-structure-interaction parameters of the models that they were originally defined for. Similarly, the zones / lengths of zones defined in the ZLR/RLR regions in a library may specifically relate to a particular structure that was analysed and from which the library was created.

Only the export/import of ZLR/RLR properties should be attempted using this tool. Attempting to export/import any other aspects of the rail track analysis modelling is likely to invalidate the rail track analysis and could stop an analysis from being performed successfully.

Performing a ZLR/RLR Rail Track Analysis

A Rail Track Analysis model must have been built from the input Excel or compatible XLSX spreadsheet before any ZLR/RLR properties or regions can be defined in a model. It is also usual that the results of the Rail Track Analysis would have been inspected (either manually or using the automatic post-processing facilities provided by the Rail Track Analysis tool) to determine where the regions of ZLR/RLR should be placed to relieve regions of high axial stress in the tracks.

The ZLR/RLR properties and regions can then be defined in the model using the dialogs that are described above. Once a fully qualified ZLR/RLR region has been defined the region needs to be set active in Modeller before it will affect the Rail Track Analysis. A region is set active by right-clicking on it in the  Utilities Treeview and selecting the “Set Active” option. More than one ZLR/RLR region can be defined in the model but only one ZLR/RLR region can be set active within the model at any time. The definition of the regions (in terms of the ZLR/RLR zones within the region) may be as complex as necessary though to define the model.

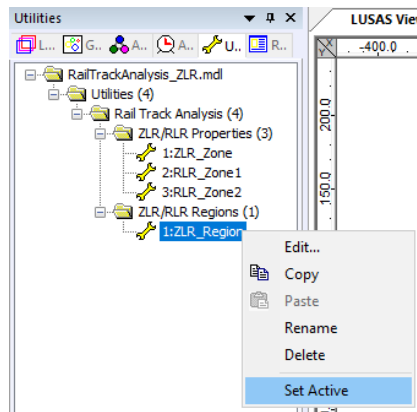


Figure 60: Setting a ZLR/RLR Region Active



Note. It is also possible to set all regions inactive (by right-clicking on the active region and deselecting the “Set Active”) to return the track-structure-interaction model to the state it was before any ZLR / RLR regions were defined.

There are two ways that the ZLR / RLR modelling can be used in the Rail Track Analysis tool, iteratively or through a sensitivity study using a master model that has a variety of ZLR/RLR configurations defined within it.

Method 1: Iteratively

The iterative approach will generally be the more common approach to find a configuration that meets the design criteria. For this an initial track-structure-interaction analysis will have been carried out and the response obtained.

- 1) Where excessive rail axial stresses have been observed in particular regions, the interaction is modified to include ZLR and/or RLR at strategic locations,
- 2) The model is saved (often as a new filename to preserve the original model), resolved and post-processed again to assess the effect of the configuration of ZLR and/or RLR,
- 3) The performance of the current design is assessed: If the performance is unacceptable then the arrangement of ZLR and/or RLR is modified and we return to 2); if the performance is acceptable then exit the iteration process.

Method 2: Sensitivity

The sensitivity approach is based more on engineering judgement and past experience since it generally requires some knowledge of the types of layouts of ZLR and/or RLR that would be needed to meet the design criteria for reducing the excessive rail axial stresses. It could also be used if specific layouts to be considered were specified from the start of a project. An initial track-structure-interaction analysis will have been carried out and the response obtained.

- 1) Excessive rail axial stresses are observed in particular regions indicating where it may be beneficial to include ZLR and/or RLR,
- 2) Based on engineering judgement and past experience multiple configurations of ZLR and/or RLR are ‘designed’ and input into a ‘master’ model but are left deactivated, so they have no effect on the track-structure-interaction analysis. This master model is saved (often as a new filename to preserve the original model) to be used for the creation of all subsequent sensitivity models,
- 3) For each ZLR and/or RLR region in the master model:
 - a. Load the master model,

- b. Set the appropriate ZLR/RLR region active,
- c. Save the model as a new filename, solve and post-process the analysis to allow the assessment of the effect of the configuration of ZLR and/or RLR,
- d. The performance of the current design is assessed: If the performance is unacceptable then the next arrangement of ZLR and/or RLR in the master model will be considered and we return to 3); if the performance is acceptable then
 - i. Either accept the current design and exit the study, or
 - ii. Return to 3) to continue with the sensitivity study to see if another of the ZLR and/or RLR configurations gives a better performance.

Rail Track Analysis Results Spreadsheet

The results spreadsheet contains worksheets of results for specific areas of interest. The number of worksheets created will depend upon the number of tracks and decks modelled and whether enveloping of results was selected.

When using the Rail Track Analysis post-processor dialog the post-processing carried out is dependent upon whether any selections have been made in LUSAS Modeller. The Rail Track analysis post-processor can carry out:

- ☐ **Post-processing of automatically defined groups** (when no selections have been made in Modeller)
- ☐ **Post-processing of selected track / rail nodes**
- ☐ **Post-processing of selected lines if groups are missing** (if they are meshed with beam elements)

Results Worksheets Created

The spreadsheet created will contain worksheets that typically include results for:

- ☐ **Track 1, 2 etc**
- ☐ **Deck 1, 2, 3 etc**
- ☐ **Envelope, Track 1, 2 etc**
- ☐ **Envelope, Deck 1, 2, 3 etc**
- ☐ **Railbed Check**
- ☐ **Longitudinal Reactions Check**

☐ **Rail Stresses Check**

and, if more than one deck is defined in the model, additional results for:

☐ **Deck End Longitudinal Displacements (axial, end rotations and total)**

☐ **Deck End Vertical Displacements**

plus, if ZLR/RLR modelling is included:

☐ **ZLR-RLR Summary**



Note. Results shown in this version of the manual were captured in previous versions of the software. Colours used for charting will differ in the latest version owing to updates made by LUSAS and changes made by Microsoft to the default colour scheme in Excel, from which they were captured.

Post-processing of Automatically Defined Groups

If nothing is selected in the Modeller window and all of the UIC774-3 groups are present in the Groups Treeview then separate results worksheets are generated for the tracks/rails and decks. If more than one results file is loaded, no combinations or envelopes are defined in the LUSAS model and enveloping has been selected then additional envelope results output is generated in separate results worksheets.

If basic combinations or envelopes were defined in the LUSAS model the results from these are output to the tracks/rails and decks worksheets in addition to the temperature only and combined temperature and train loading results. If enveloping has been selected, then an additional envelope will be generated for the basic combinations included in the model (and these results will be included in the overall envelope of all results).



Note. Basic combinations that contain only pure loadcases can be post-processed but basic combinations that contain envelopes or smart combinations cannot be post-processed. Envelopes cannot be post-processed if they contain smart combinations. It should, however, be noted that the creation of combinations of nonlinear results (such as those from the Rail Track Analysis tool) is not strictly valid and results should be used with caution.

ZLR/RLR Summary

If a Rail Track Analysis that includes ZLR and/or RLR modelling has been performed, then the first worksheet in the results spreadsheet will contain a summary of the zone and associated property definitions used within the active region for the analysis.

A sample summary for a Rail Track Analysis with a simple ZLR region is shown in Figure 61. The summary shows that the Rail Track Analysis has an active ZLR/RLR region consisting of matching ZLR zones for the two tracks that use a single ZLR property definition.

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Summary of Zero Longitudinal Resistance / Reduced Longitudinal Resistance Definitions

Job Title: UIC 774-3 Model: Esvel-TempAndTGV

Analysis Filename: EsvelZLR_TempAndTGV_Analysis 1

Model Directory: F:\Users\Projects\RailTrackAnalysis

Analysis Date: 12/08/2022

Model Units: N,m,kg,s,C

ZLR / RLR Region Definition

Region Name: Deck 6: 75m ZLR Region

Track	Start Position from Left End of Track (m)	End Position from Left End of Track (m)	ZLR/RLR Property
1	610	685	ZLR Properties
2	610	685	ZLR Properties

NOTE: Finite Element mesh discretisation for track-structure-interaction joint modelling means that some minor differences may occur

ZLR / RLR Property Definitions

ZLR/RLR Property	Property Type	Unloaded			Loaded		
		Elastic spring stiffness (kN/mm per m track)	Yield force (kN per m track)	Hardening stiffness (kN/mm per m track)	Elastic spring stiffness (kN/mm per m track)	Yield force (kN per m track)	Hardening stiffness (kN/mm per m track)
ZLR Properties	ZLR	1	0.000001	0.000001	1	0.000001	0.000001

ZLR-RLR Summary

Track 1

Track 2

Decks

Figure 61: ZLR/RLR Properties and Active Region Summary

The ZLR/RLR region definition can consist of a simple zone as illustrated in Figure 61 or it could consist of multiple zones with different properties – the number of ZLR/RLR properties that can be defined and assigned to a ZLR/RLR region is unlimited. When the zones of ZLR/RLR are defined in the ZLR/RLR region dialog, if positions within the definitions of the zones of a rail track overlap the last zone defined in the table for a particular rail track will overwrite the previous definitions for that rail track. Messages will have been issued when the original region was defined and these will be repeated in the summary as illustrated in the example shown in Figure 62 below.

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Figure 62: Region Summary with Multiple Zones and Properties (including overlaps)

Rail Track Results

A separate results worksheet is created for each track in the model. In this worksheet the displacement (including railbed relative displacement), forces / moments and axial stresses in the track rails are reported for all of the results files. If only temperature results exist in a results file the post-processing will only generate the output for these (Increment 1 of the nonlinear analysis), Figure 63 to Figure 65. If trainset loading is also present in the analyses then for each results file the results for the temperature only (Increment 1 of the nonlinear analysis) and the combined temperature and trainset loading (Increment 2 of the nonlinear analysis) are output for each results file, Figure 66 to Figure 68.

Figure 69 shows a zoomed out version of the worksheet showing the output for multiple results files. In this figure the temperature only and combined results for two results files are illustrated with the analyses incrementing from left to right and for each, the first column of results and graphs are for the temperature only case and the second column are for the combined case for each analysis.



Note. When only a single Train Loading Group is analysed the results and charts will report results / chart titles as “Position ? – Deck Temp (Manual NL)” or “Position ? – Train Loads”. For analyses where multiple Train Loading Groups are included then each of the results / chart titles will reflect the Train Loading Group and position with text such as “Train Loading Group ? – Position ? – Train Loads” to identify the results and charts within the post-processing spreadsheet (and provide fully titled charts should these be copied and pasted from the spreadsheet).

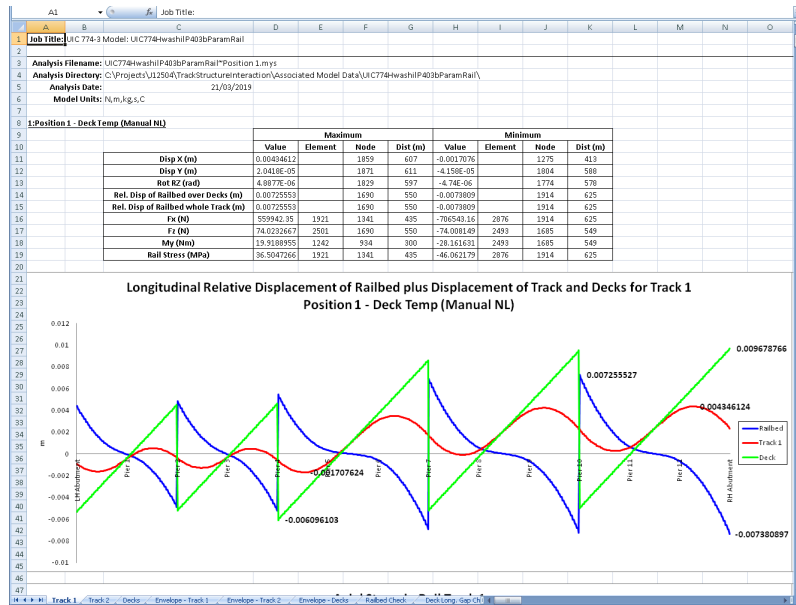


Figure 63: Track Worksheet Summary and Railbed Graph for Temperature Only Results of Analysis, Increment 1 (1 of 3)

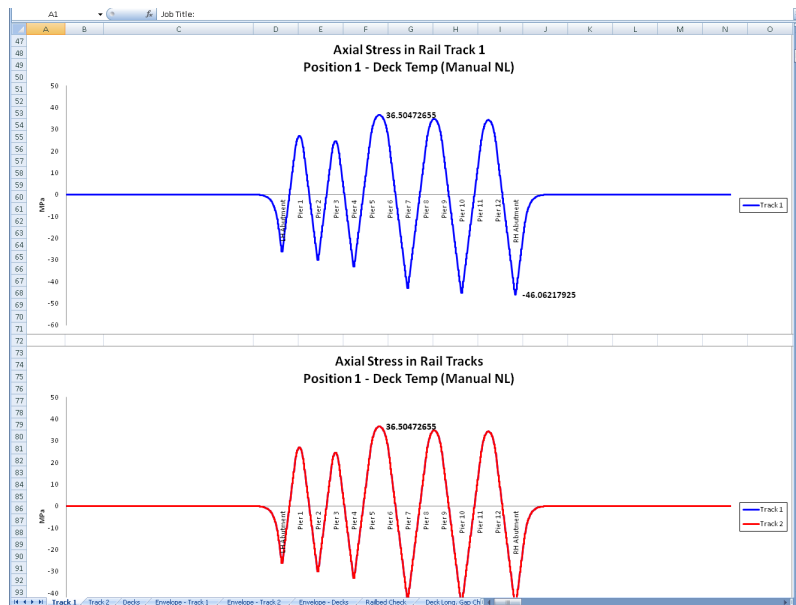


Figure 64: Track Worksheet Rail Stress Graphs for Temperature Only Results of Analysis, Increment 1 (2 of 3)

Rail Track Analysis Results Spreadsheet

A1		Job Title:													
Element	Node	Abutment / Pier	Distance (m)	X (m)	Y (m)	Z (m)	Disp X (m)	Disp Y (m)	Rot RZ (rad)	Rel. Disp of Railbed (m)	Fx (kN)	Fy (kN)	My (kNm)	Rail Stress (MPa)	
99	39	23	0	-300	0	0	0	0	0	-0.004E-15	1.212E-209	2.886E-210	-1.978E-19		
100	39	30	1	-299	0	0	-9.42E-25	9.172E-219	1.111E-216	-9.42E-25	-3.034E-15	1.212E-209	2.886E-210	-1.978E-19	
101	39	30	1	-299	0	0	-9.42E-25	9.172E-219	1.111E-216	-9.42E-25	-3.11E-15	-4.49E-209	-1.95E-209	-2.027E-19	
102	44	30	2	-298	0	0	-1.907E-24	-2.40E-210	-4.61E-216	-1.907E-24	-3.11E-15	-4.49E-209	-1.95E-209	-2.027E-19	
103	44	39	2	-298	0	0	-1.907E-24	-2.40E-210	-4.61E-216	-1.907E-24	-3.262E-15	1.76E-200	5.208E-200	-2.127E-19	
104	40	39	0	-297	0	0	-2.92E-24	9.113E-210	1.81E-215	-2.92E-24	-3.262E-15	1.76E-200	5.208E-200	-2.127E-19	
105	40	43	0	-297	0	0	-2.92E-24	9.113E-210	1.81E-215	-2.92E-24	-3.406E-15	-6.95E-200	-2.03E-200	-2.279E-19	
106	51	43	4	-296	0	0	-4.005E-24	-3.55E-217	-7.05E-215	-4.005E-24	-3.406E-15	-6.95E-200	-2.03E-200	-2.279E-19	
107	51	46	4	-296	0	0	-4.005E-24	-3.55E-217	-7.05E-215	-4.005E-24	-3.814E-15	-2.668E-207	-7.892E-200	-2.408E-19	
108	56	46	5	-295	0	0	-5.19E-24	1.801E-216	2.74E-214	-5.19E-24	-3.814E-15	-2.668E-207	-7.892E-200	-2.408E-19	
109	56	49	5	-295	0	0	-5.19E-24	1.801E-216	2.74E-214	-5.19E-24	-3.814E-15	-2.668E-207	-7.892E-200	-2.408E-19	
110	59	49	5	-295	0	0	-5.19E-24	1.801E-216	2.74E-214	-5.19E-24	-4.232E-15	-1.04E-206	-3.07E-207	-2.759E-19	
111	59	52	6	-294	0	0	-6.504E-24	-5.98E-216	-1.07E-213	-6.504E-24	-4.232E-15	-1.04E-206	-3.07E-207	-2.759E-19	
112	63	52	6	-294	0	0	-6.504E-24	-5.98E-216	-1.07E-213	-6.504E-24	-4.752E-15	-4.008E-206	-1.197E-206	-3.098E-19	
113	63	55	7	-293	0	0	-7.979E-24	2.094E-215	4.165E-213	-7.979E-24	-4.752E-15	-4.008E-206	-1.197E-206	-3.098E-19	
114	67	55	7	-293	0	0	-7.979E-24	2.094E-215	4.165E-213	-7.979E-24	-5.39E-15	-1.58E-205	-4.66E-206	-3.514E-19	
115	67	58	8	-292	0	0	-9.659E-24	-8.14E-215	-1.63E-212	-9.659E-24	-5.39E-15	-1.58E-205	-4.66E-206	-3.514E-19	
116	71	58	8	-292	0	0	-9.659E-24	-8.14E-215	-1.63E-212	-9.659E-24	-6.14E-15	-6.14E-205	-6.03E-205	-4.010E-19	
117	71	62	9	-291	0	0	-1.157E-23	3.177E-214	6.318E-212	-1.157E-23	-6.14E-15	-6.14E-205	-6.03E-205	-4.010E-19	
118	76	62	9	-291	0	0	-1.157E-23	3.177E-214	6.318E-212	-1.157E-23	-7.088E-15	-2.39E-204	-7.07E-205	-4.621E-19	
119	76	65	10	-290	0	0	-1.377E-23	-1.24E-213	-2.46E-211	-1.377E-23	-7.088E-15	-2.39E-204	-7.07E-205	-4.621E-19	
120	79	65	10	-290	0	0	-1.377E-23	-1.24E-213	-2.46E-211	-1.377E-23	-8.189E-15	9.313E-204	2.754E-204	-5.339E-19	
121	79	66	11	-289	0	0	-1.631E-23	4.819E-213	9.593E-211	-1.631E-23	-8.189E-15	9.313E-204	2.754E-204	-5.339E-19	
122	83	66	11	-289	0	0	-1.631E-23	4.819E-213	9.593E-211	-1.631E-23	-9.494E-15	-3.63E-203	-1.07E-203	-6.189E-19	
123	83	71	12	-288	0	0	-1.926E-23	-1.88E-212	-3.73E-210	-1.926E-23	-9.494E-15	-3.63E-203	-1.07E-203	-6.189E-19	
124	87	71	12	-288	0	0	-1.926E-23	-1.88E-212	-3.73E-210	-1.926E-23	-1.103E-14	1.413E-202	4.177E-203	-7.139E-19	
125	87	72	13	-287	0	0	-2.248E-23	7.898E-212	1.454E-209	-2.248E-23	-1.103E-14	1.413E-202	4.177E-203	-7.139E-19	
126	91	72	13	-287	0	0	-2.248E-23	7.898E-212	1.454E-209	-2.248E-23	-1.285E-14	-5.5E-202	-1.63E-202	-8.376E-19	
127	91	77	14	-286	0	0	-2.647E-23	-2.85E-211	-5.64E-209	-2.647E-23	-1.285E-14	-5.5E-202	-1.63E-202	-8.376E-19	
128	95	77	14	-286	0	0	-2.647E-23	-2.85E-211	-5.64E-209	-2.647E-23	-1.498E-14	2.143E-201	6.394E-202	-9.767E-19	
129	95	79	15	-285	0	0	-3.132E-23	1.109E-210	2.205E-208	-3.132E-23	-1.498E-14	2.143E-201	6.394E-202	-9.767E-19	
130	99	79	15	-285	0	0	-3.132E-23	1.109E-210	2.205E-208	-3.132E-23	-1.749E-14	-8.34E-201	-2.47E-201	-1.14E-18	
131	99	83	16	-284	0	0	-3.676E-23	-4.32E-210	-8.59E-208	-3.676E-23	-1.749E-14	-8.34E-201	-2.47E-201	-1.14E-18	
132	104	83	16	-284	0	0	-3.676E-23	-4.32E-210	-8.59E-208	-3.676E-23	-2.043E-14	3.25E-200	9.61E-201	-1.332E-18	
133	104	84	17	-283	0	0	-4.309E-23	1.682E-209	3.344E-207	-4.309E-23	-2.043E-14	3.25E-200	9.61E-201	-1.332E-18	
134	107	84	17	-283	0	0	-4.309E-23	1.682E-209	3.344E-207	-4.309E-23	-2.388E-14	-1.27E-199	-3.74E-200	-1.557E-18	
135	107	87	18	-282	0	0	-5.05E-23	-6.55E-209	-1.3E-206	-5.05E-23	-2.388E-14	-1.27E-199	-3.74E-200	-1.557E-18	
136	112	87	18	-282	0	0	-5.05E-23	-6.55E-209	-1.3E-206	-5.05E-23	-2.792E-14	4.93E-199	1.498E-199	-1.92E-18	
137	112	91	19	-281	0	0	-5.917E-23	2.551E-208	5.072E-206	-5.917E-23	-2.792E-14	4.93E-199	1.498E-199	-1.92E-18	
138	116	91	19	-281	0	0	-5.917E-23	2.551E-208	5.072E-206	-5.917E-23	-3.265E-14	-1.92E-198	-5.68E-199	-1.129E-18	
139	116	94	20	-280	0	0	-6.931E-23	-9.93E-208	-1.98E-205	-6.931E-23	-3.265E-14	-1.92E-198	-5.68E-199	-1.129E-18	
140	119	94	20	-280	0	0	-6.931E-23	-9.93E-208	-1.98E-205	-6.931E-23	-3.819E-14	7.477E-198	2.211E-198	-2.49E-18	
141	119	96	21	-279	0	0	-8.114E-23	3.869E-207	7.694E-205	-8.114E-23	-3.819E-14	7.477E-198	2.211E-198	-2.49E-18	
142	123	96	21	-279	0	0	-8.114E-23	3.869E-207	7.694E-205	-8.114E-23	-4.469E-14	-2.91E-197	-8.61E-198	-2.913E-18	
143	123	99	22	-278	0	0	-9.504E-23	-1.51E-206	-3E-204	-9.504E-23	-4.469E-14	-2.91E-197	-8.61E-198	-2.913E-18	

Figure 65: Track Worksheet Tabulated Output for Temperature Only Results of Analysis, Increment 1 (3 of 3)

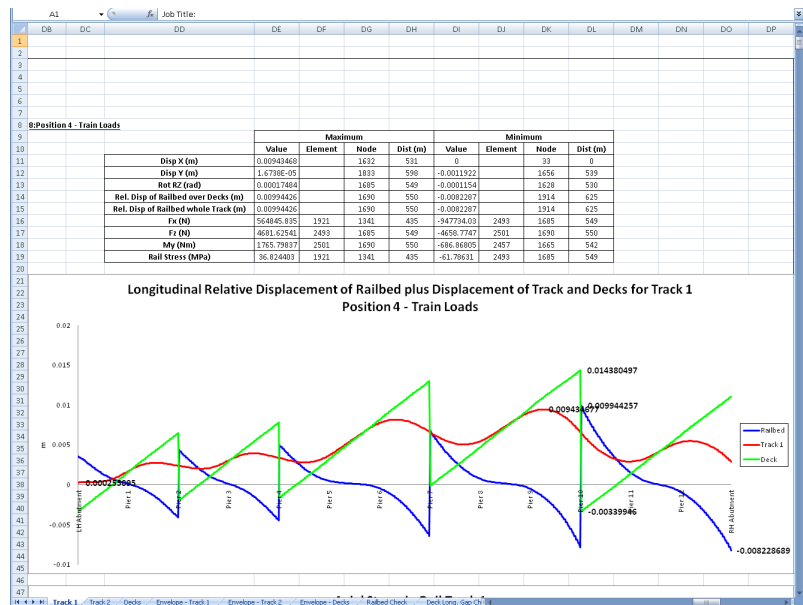


Figure 66: Track Worksheet Summary and Railbed Graph for Temperature and Trainset Results of Analysis, Increment 2 (1 of 3)

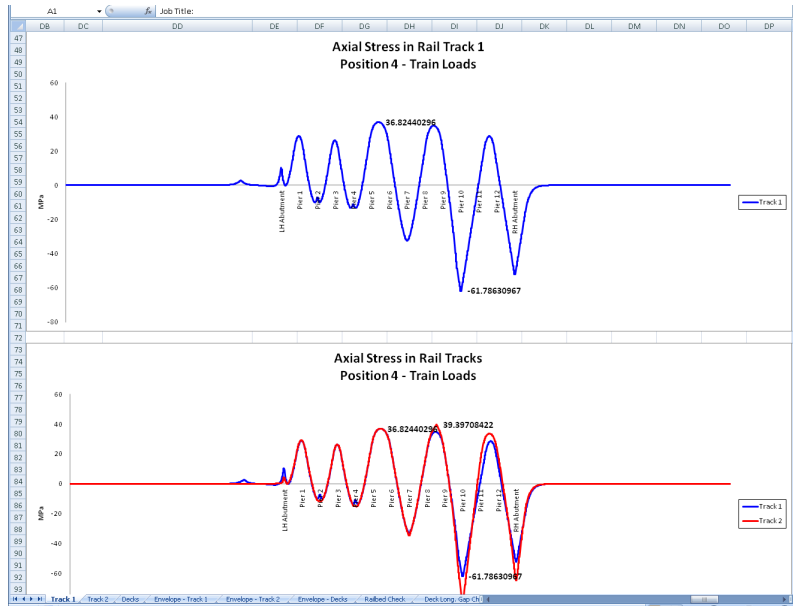


Figure 67: Track Worksheet Rail Stress Graphs for Temperature and Trainset Results of Analysis, Increment 2 (2 of 3)

A1		Job Title													
DB	DC	DD	DE	DF	DG	DH	DI	DJ	DK	DL	DM	DN	DO	DP	
Element	Node	Abutment / Pier	Distance (m)	X (m)	Y (m)	Z (m)	Disp X (m)	Disp Y (m)	Rot RZ (rad)	Rel. Disp of Railbed (m)	Fx (kN)	Fy (kN)	My (Nm)	Rail Stress (MPa)	
99	100	39	33	0	-300	0	0	0	0	1.9999E-12	-9.02E-175	-2.34E-175	1.3037E-16		
101	39	38	1	-299	0	0	6.2088E-22	-7.43E-184	-9.02E-182	6.2088E-22	1.9999E-12	-9.02E-175	-2.34E-175	1.3037E-16	
102	44	38	1	-299	0	0	6.2088E-22	-7.43E-184	-9.02E-182	6.2088E-22	2.0495E-12	3.641E-174	1.095E-174	1.3616E-16	
103	44	39	2	-298	0	0	1.2571E-21	1.971E-189	3.752E-181	1.2571E-21	2.0495E-12	3.641E-174	1.095E-174	1.3616E-16	
104	48	39	2	-298	0	0	1.2571E-21	1.971E-189	3.752E-181	1.2571E-21	2.15E-12	-1.40E-179	-4.22E-174	1.401E-16	
105	48	43	3	-297	0	0	1.9246E-21	-7.38E-180	-1.47E-180	1.9246E-21	2.15E-12	-1.40E-179	-4.22E-174	1.401E-16	
106	51	43	3	-297	0	0	1.9246E-21	-7.38E-180	-1.47E-180	1.9246E-21	2.304E-12	5.553E-173	1.642E-173	1.5021E-16	
107	51	46	4	-296	0	0	2.6398E-21	2.078E-182	5.713E-180	2.6398E-21	2.304E-12	5.553E-173	1.642E-173	1.5021E-16	
108	56	46	4	-296	0	0	2.6398E-21	2.078E-182	5.713E-180	2.6398E-21	2.5152E-12	-2.14E-172	-6.39E-173	1.639E-16	
109	56	49	5	-295	0	0	3.4206E-21	-1.12E-181	-2.23E-179	3.4206E-21	2.5152E-12	-2.14E-172	-6.39E-173	1.639E-16	
110	59	49	5	-295	0	0	3.4206E-21	-1.12E-181	-2.23E-179	3.4206E-21	2.7888E-12	8.422E-172	2.49E-172	1.8101E-16	
111	59	52	6	-294	0	0	4.2864E-21	4.357E-181	8.666E-179	4.2864E-21	2.7888E-12	8.422E-172	2.49E-172	1.8101E-16	
112	63	52	6	-294	0	0	4.2864E-21	4.357E-181	8.666E-179	4.2864E-21	3.1318E-12	-3.20E-171	-9.7E-172	2.041E-16	
113	63	55	7	-293	0	0	5.2587E-21	-1.7E-180	-3.97E-178	5.2587E-21	3.1318E-12	-3.20E-171	-9.7E-172	2.041E-16	
114	67	55	7	-293	0	0	5.2587E-21	-1.7E-180	-3.97E-178	5.2587E-21	3.5524E-12	1.277E-170	3.777E-171	2.314E-16	
115	67	58	8	-292	0	0	6.3615E-21	6.609E-180	1.314E-177	6.3615E-21	3.5524E-12	1.277E-170	3.777E-171	2.314E-16	
116	71	58	8	-292	0	0	6.3615E-21	6.609E-180	1.314E-177	6.3615E-21	4.0634E-12	-4.90E-170	-1.47E-170	2.6478E-16	
117	71	62	9	-291	0	0	7.6224E-21	-2.57E-179	-5.12E-177	7.6224E-21	4.0634E-12	-4.90E-170	-1.47E-170	2.6478E-16	
118	76	62	9	-291	0	0	7.6224E-21	-2.57E-179	-5.12E-177	7.6224E-21	4.6712E-12	1.938E-169	5.729E-170	3.045E-16	
119	76	65	10	-290	0	0	9.0725E-21	1.002E-178	1.994E-176	9.0725E-21	4.6712E-12	1.938E-169	5.729E-170	3.045E-16	
120	79	65	10	-290	0	0	9.0725E-21	1.002E-178	1.994E-176	9.0725E-21	5.397E-12	-7.55E-169	-2.23E-169	3.5185E-16	
121	79	66	11	-289	0	0	1.0748E-20	-3.9E-178	-7.76E-176	1.0748E-20	5.397E-12	-7.55E-169	-2.23E-169	3.5185E-16	
122	83	66	11	-289	0	0	1.0748E-20	-3.9E-178	-7.76E-176	1.0748E-20	6.250E-12	2.939E-168	8.63E-169	4.079E-16	
123	83	71	12	-288	0	0	1.269E-20	1.921E-177	3.024E-175	1.269E-20	6.250E-12	2.939E-168	8.63E-169	4.079E-16	
124	87	71	12	-288	0	0	1.269E-20	1.921E-177	3.024E-175	1.269E-20	7.272E-12	-1.14E-167	-3.98E-168	4.7409E-16	
125	87	72	13	-287	0	0	1.4948E-20	-5.92E-177	-1.18E-174	1.4948E-20	7.272E-12	-1.14E-167	-3.98E-168	4.7409E-16	
126	91	72	13	-287	0	0	1.4948E-20	-5.92E-177	-1.18E-174	1.4948E-20	8.4679E-12	4.698E-167	1.318E-167	5.5205E-16	
127	91	77	14	-286	0	0	1.7577E-20	2.306E-176	4.50E-174	1.7577E-20	8.4679E-12	4.698E-167	1.318E-167	5.5205E-16	
128	95	77	14	-286	0	0	1.7577E-20	2.306E-176	4.50E-174	1.7577E-20	9.874E-12	-1.74E-166	-5.13E-167	6.4372E-16	
129	95	79	15	-285	0	0	2.0642E-20	-8.98E-176	-1.79E-173	2.0642E-20	9.874E-12	-1.74E-166	-5.13E-167	6.4372E-16	
130	99	79	15	-285	0	0	2.0642E-20	-8.98E-176	-1.79E-173	2.0642E-20	1.1525E-11	6.761E-166	1.999E-166	7.5338E-16	
131	99	83	16	-284	0	0	2.422E-20	3.498E-175	6.95E-173	2.422E-20	1.1525E-11	6.761E-166	1.999E-166	7.5338E-16	
132	104	83	16	-284	0	0	2.422E-20	3.498E-175	6.95E-173	2.422E-20	1.3463E-11	-2.63E-165	-7.79E-166	8.777E-16	
133	104	84	17	-283	0	0	2.842E-20	-1.36E-174	-2.71E-172	2.842E-20	1.3463E-11	-2.63E-165	-7.79E-166	8.777E-16	
134	107	84	17	-283	0	0	2.842E-20	-1.36E-174	-2.71E-172	2.842E-20	1.5779E-11	1.024E-164	3.033E-165	1.029E-15	
135	107	87	18	-282	0	0	3.3284E-20	5.306E-174	1.055E-171	3.3284E-20	1.5779E-11	1.024E-164	3.033E-165	1.029E-15	
136	112	87	18	-282	0	0	3.3284E-20	5.306E-174	1.055E-171	3.3284E-20	1.8398E-11	-3.99E-164	-1.18E-164	1.1994E-15	
137	112	91	19	-281	0	0	3.8996E-20	-2.07E-173	-4.11E-171	3.8996E-20	1.8398E-11	-3.99E-164	-1.18E-164	1.1994E-15	
138	116	91	19	-281	0	0	3.8996E-20	-2.07E-173	-4.11E-171	3.8996E-20	2.1517E-11	1.556E-163	4.44E-164	1.4628E-15	
139	116	94	20	-280	0	0	4.5676E-20	8.048E-173	1.601E-170	4.5676E-20	2.1517E-11	1.556E-163	4.44E-164	1.4628E-15	
140	119	94	20	-280	0	0	4.5676E-20	8.048E-173	1.601E-170	4.5676E-20	2.5171E-11	-6.04E-163	-1.79E-163	1.641E-15	
141	119	96	21	-279	0	0	5.349E-20	-1.13E-172	-6.23E-170	5.349E-20	2.5171E-11	-6.04E-163	-1.79E-163	1.641E-15	
142	123	96	21	-279	0	0	5.349E-20	-1.13E-172	-6.23E-170	5.349E-20	2.9451E-11	2.059E-162	6.977E-163	1.92E-15	
143	123	99	22	-278	0	0	6.6203E-20	1.221E-171	2.402E-169	6.6203E-20	2.9451E-11	2.059E-162	6.977E-163	1.92E-15	

Figure 68: Track Worksheet Tabulated Output for Temperature and Trainset Results of Analysis, Increment 2 (3 of 3)

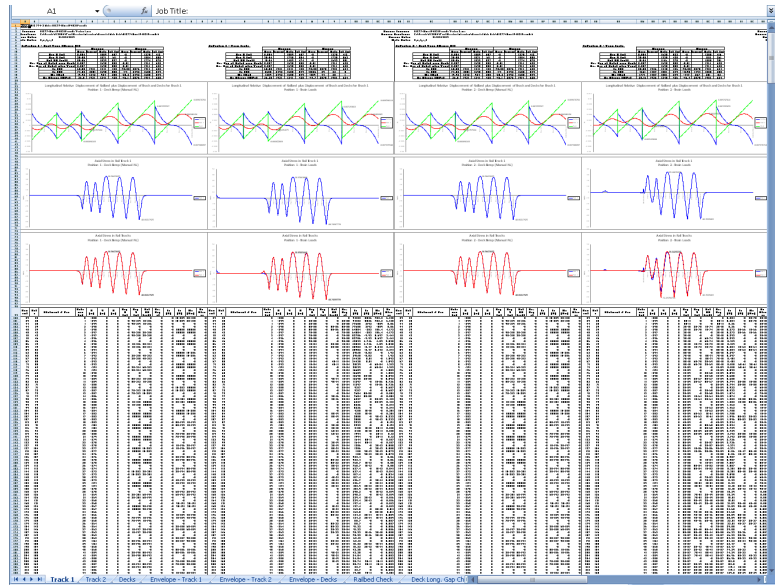


Figure 69: Track Worksheet for Multiple Results Files

If ZLR and/or RLR modelling has been included in the Rail Track Analysis, then an additional legend is included above the “Rail Stress” column of the tabular output in the track worksheets as shown in Figure 70. Within the tabular results the rail stress cells that correspond to regions of track that are within zones of ZLR track will be coloured with the pale blue shading and the regions of track that are within zones of RLR track will be coloured with the pale orange shading.

For the structure that has been modelled in Figure 70 it is possible to visualise where the ZLR track is present in the rail stress chart itself as it is indicated by the constant rail stress of -116.27 MPa stretching from within Deck 6 to Pier 6. The extent of the region of ZLR is indicated within the tabulated results in Figure 71 and Figure 72 which shows that the zone stretches over a range of 310 to 385 m from the start of the left-hand abutment to Pier 6 (610 to 685 m from the start of the track including the left-hand abutment).

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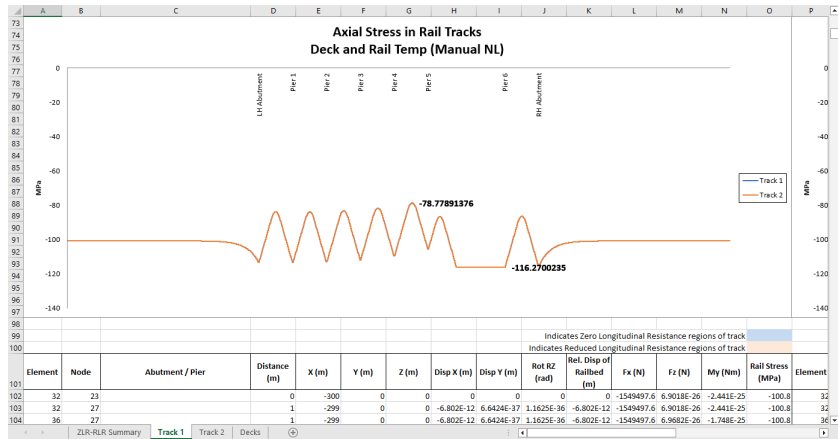


Figure 70: Track Results – Top of Tabular Results for ZLR/RLR Modelling

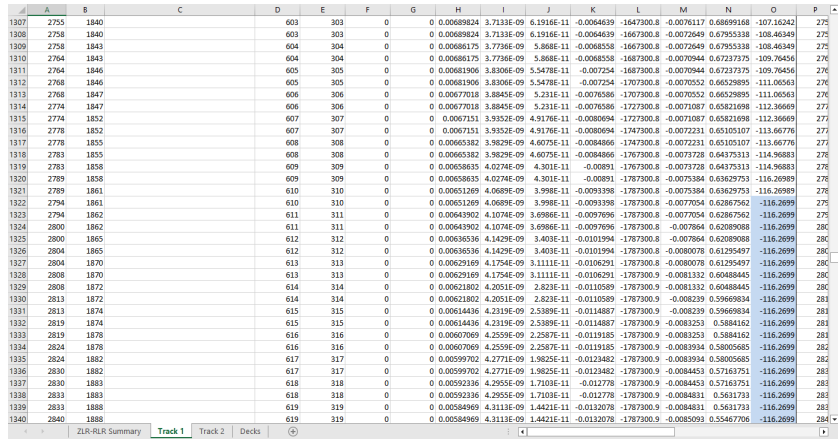


Figure 71: Track Results – Visualisation of Extents of ZLR Track (1 of 2)

J	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P
1454	3124	2058		676	376	0	0	0.00165071	2.0458E-09	-3.446E-11	-0.0377049	-1.787302.5	0.2432565	1.73794737	-116.27	312
1455	3124	2060		677	377	0	0	0.00157704	1.9486E-09	-1.0317E-10	-0.0381347	-1.787302.5	0.2432565	1.73794737	-116.27	312
1456	3130	2060		677	377	0	0	0.00157704	1.9486E-09	-1.0317E-10	-0.0381347	-1.787302.5	0.20793127	1.96354126	-116.27	312
1457	3130	2064		678	378	0	0	0.00150317	1.8425E-09	-1.111E-10	-0.0385645	-1.787302.5	0.20793127	1.96354126	-116.27	311
1458	3134	2064		678	378	0	0	0.00150317	1.8425E-09	-1.111E-10	-0.0385645	-1.787302.5	0.13866622	2.13684	-116.27001	311
1459	3134	2066		679	379	0	0	0.00142971	1.7265E-09	-1.213E-10	-0.0389943	-1.787302.5	0.13866622	2.13684	-116.27001	311
1460	3139	2066		679	379	0	0	0.00142971	1.7265E-09	-1.213E-10	-0.0389943	-1.787302.6	0.02289619	2.21912121	-116.27001	311
1461	3139	2069		680	380	0	0	0.00135604	1.6E-09	-1.318E-10	-0.039424	-1.787302.6	0.02289619	2.21912121	-116.27001	311
1462	3145	2069		680	380	0	0	0.00135604	1.6E-09	-1.318E-10	-0.039424	-1.787302.6	-0.1406457	2.16174643	-116.27001	314
1463	3145	2073		681	381	0	0	0.00128217	1.4628E-09	-1.421E-10	-0.0398538	-1.787302.6	-0.1406457	2.16174643	-116.27001	314
1464	3148	2073		681	381	0	0	0.00128217	1.4628E-09	-1.421E-10	-0.0398538	-1.787302.7	-0.3713914	1.90572785	-116.27001	314
1465	3148	2075		682	382	0	0	0.00120871	1.3157E-09	-1.512E-10	-0.0402836	-1.787302.7	-0.3713914	1.90572785	-116.27001	314
1466	3153	2075		682	382	0	0	0.00120871	1.3157E-09	-1.512E-10	-0.0402836	-1.787302.7	-0.6761449	1.38139588	-116.27001	315
1467	3153	2078		683	383	0	0	0.00113504	1.1604E-09	-1.578E-10	-0.0407134	-1.787302.7	-0.6761449	1.38139588	-116.27002	315
1468	3159	2078		683	383	0	0	0.00113504	1.1604E-09	-1.578E-10	-0.0407134	-1.787302.7	-1.0629839	0.51239527	-116.27002	315
1469	3159	2082		684	384	0	0	0.00106137	1.0001E-09	-1.602E-10	-0.0411431	-1.787302.7	-1.0629839	0.51239527	-116.27002	315
1470	3164	2082		684	384	0	0	0.00106137	1.0001E-09	-1.602E-10	-0.0411431	-1.787302.8	-1.5348087	-0.787501	-116.27002	316
1471	3164	2084 Pier 6		685	385	0	0	0.00098771	8.3995E-10	-1.565E-10	-0.0415729	-1.787302.8	-1.5348087	-0.787501	-116.27002	316
1472	3171	2084		685	385	0	0	0.00098771	8.3995E-10	-1.565E-10	0.00952554	-1.787302.8	-1.4270451	-2.2694279	-116.27002	317
1473	3171	2088		686	386	0	0	0.00091404	6.8717E-10	-1.457E-10	0.00909203	-1.787302.8	-1.4270451	-2.2694279	-116.27002	317
1474	3176	2088		686	386	0	0	0.00091404	6.8717E-10	-1.457E-10	0.00909203	-1.787302.8	-0.8077565	-3.3868287	-114.56986	317
1475	3176	2092		687	387	0	0	0.00084657	5.486E-10	-1.295E-10	0.00866477	-1.787302.8	-0.8077565	-3.3868287	-114.56986	317
1476	3181	2092		687	387	0	0	0.00084657	5.486E-10	-1.295E-10	0.00866477	-1.747302.8	-0.3348128	-3.5581134	-113.66789	318
1477	3181	2094		688	388	0	0	0.00078529	4.2809E-10	-1.107E-10	0.00824375	-1.747302.8	-0.3348128	-3.5581134	-113.66789	318
1478	3186	2094		688	388	0	0	0.00078529	4.2809E-10	-1.107E-10	0.00824375	-1.727302.8	0.0102167	-4.1204114	-112.56682	316
1479	3186	2098		689	389	0	0	0.00073021	3.2722E-10	-9.106E-11	0.00782896	-1.727302.8	0.0102167	-4.1204114	-112.56682	316
1480	3191	2098		689	389	0	0	0.00073021	3.2722E-10	-9.106E-11	0.00782896	-1.707302.8	0.24735625	-3.9916249	-111.06575	315
1481	3191	2100		690	390	0	0	0.00068113	2.4596E-10	-7.206E-11	0.00742042	-1.707302.8	0.24735625	-3.9916249	-111.06575	315
1482	3196	2100		690	390	0	0	0.00068113	2.4596E-10	-7.206E-11	0.00742042	-1.687302.8	0.39658137	-3.6696561	-109.76469	315
1483	3196	2104		691	391	0	0	0.00063864	1.8312E-10	-5.458E-11	0.00701811	-1.687302.8	0.39658137	-3.6696561	-109.76469	315
1484	3202	2104		691	391	0	0	0.00063864	1.8312E-10	-5.458E-11	0.00701811	-1.667302.8	0.47688976	-3.2330205	-108.46362	320
1485	3202	2106		692	392	0	0	0.00060215	1.3681E-10	-4.919E-11	0.00662205	-1.667302.8	0.47688976	-3.2330205	-108.46362	320
1486	3207	2106		692	392	0	0	0.00060215	1.3681E-10	-4.919E-11	0.00662205	-1.647302.8	0.50459103	-2.7423801	-107.16255	320
1487	3207	2109		693	393	0	0	0.00057185	1.0476E-10	-2.613E-11	0.00623223	-1.647302.8	0.50459103	-2.7423801	-107.16255	320

Figure 72: Track Results – Visualisation of Extents of ZLR Track (2 of 2)

If valid basic combinations or envelopes that match the criteria described in “*Post-processing of automatically defined groups*” (page 63) are present in the model then additional results for these will be tabulated into the XLSX worksheets for the tracks. For basic combinations a warning will be added at the top of the extracted results indicating that basic combinations of nonlinear results are not strictly valid. For LUSAS envelopes all quantities other than the longitudinal relative railbed displacements will be extracted for the tracks and the results from LUSAS envelopes will also be excluded from any enveloping carried out.



Note. Longitudinal relative railbed displacements cannot be calculated within the LUSAS envelopes directly because this is a quantity derived from two separate disconnected nodes in the model and requires a knowledge of the geometry of the model. The calculation of the longitudinal relative railbed displacements can only be carried out by the Rail Track Analysis specific post-processing.

Deck Results

A separate worksheet is created for the deck in the model. In this worksheet the displacement and forces / moments in the deck are reported for all of the results files. If only temperature results exist in a results file the post-processing will only generate the output for these (Increment 1 of the nonlinear analysis). If trainset loading is also present in the analyses then for each results file the results for the temperature only (Increment 1 of the nonlinear analysis) and the combined temperature and trainset loading (Increment 2 of the nonlinear analysis) are output for each results file. Figure 73 to Figure 76 show the tabulated and graph output generated for the deck for all of the loading conditions included in the analyses. Figure 77 shows a zoomed out version of the worksheet showing the output for multiple results files. In this figure the temperature only and combined results for more than two results files are illustrated

with the analyses incrementing from left to right and for each, the first column of results and graphs are for the temperature only case and the second column are for the combined case for each analysis.



Note. The tabulated and graphed nodal displacements for the deck are the displacements associated with the top of the slab / the surface where the interaction occurs between the structure and the track, not the displacements at the neutral axis or at the bearings, since this is the nodal line of the main deck mesh to ensure correct longitudinal relative railbed displacement calculations. It is possible to calculate the displacements at these locations if needed – see “Appendix C: Calculation of Deck Displacements at Alternative Locations to Top of Slab / Deck”.

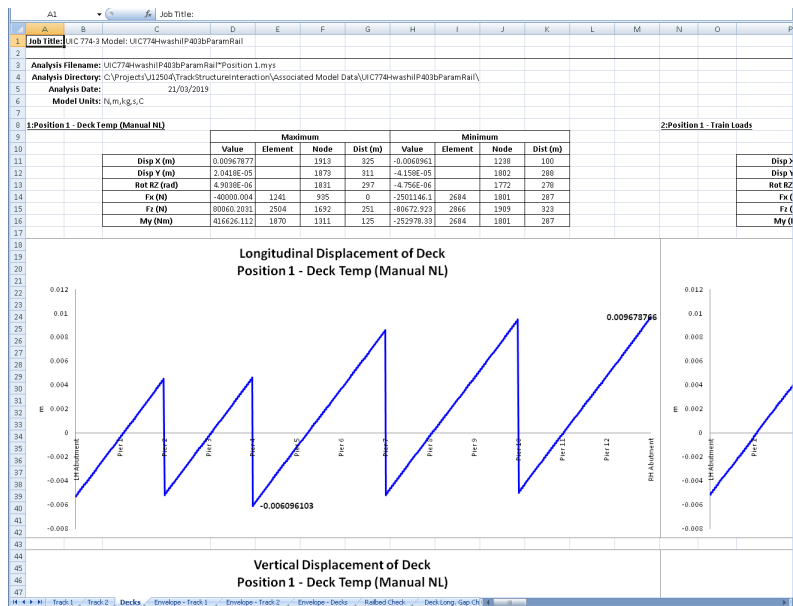


Figure 73: Deck Worksheet Summary and Longitudinal Displacement Graph for Results of Analysis (1 of 4)

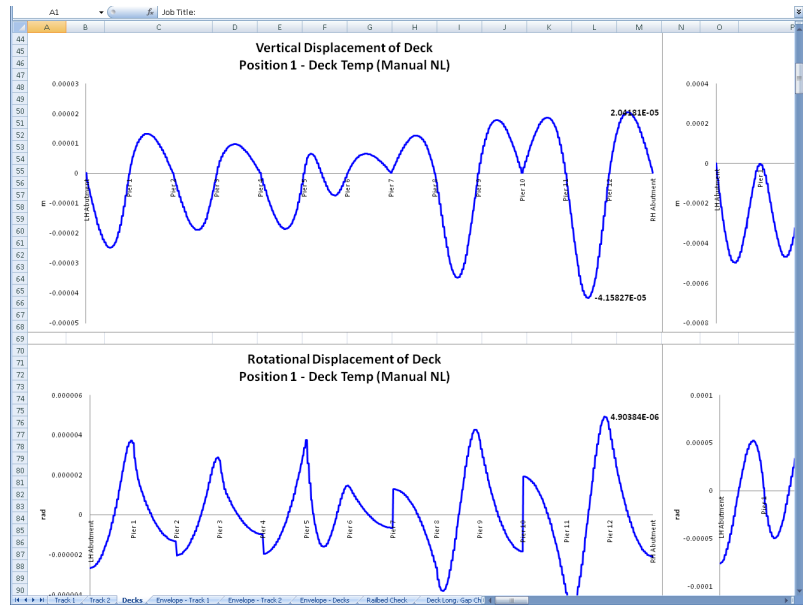


Figure 74: Deck Worksheet Vertical and Rotational Displacement Graphs for Results of Analysis (2 of 4)

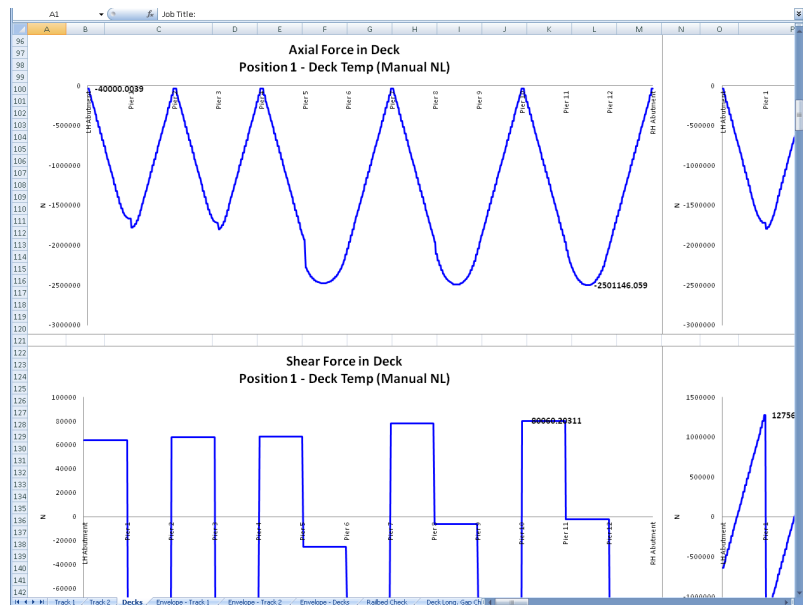


Figure 75: Deck Worksheet Axial and Shear Force Graphs for Results of Analysis (3 of 4)

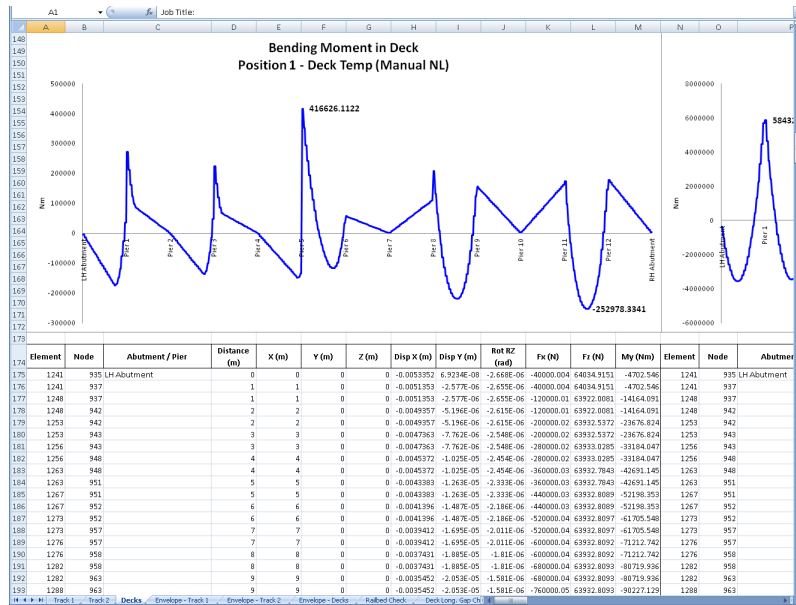


Figure 76: Deck Worksheet Bending Moment Graph and Tabulated Output for Results of Analysis (4 of 4)

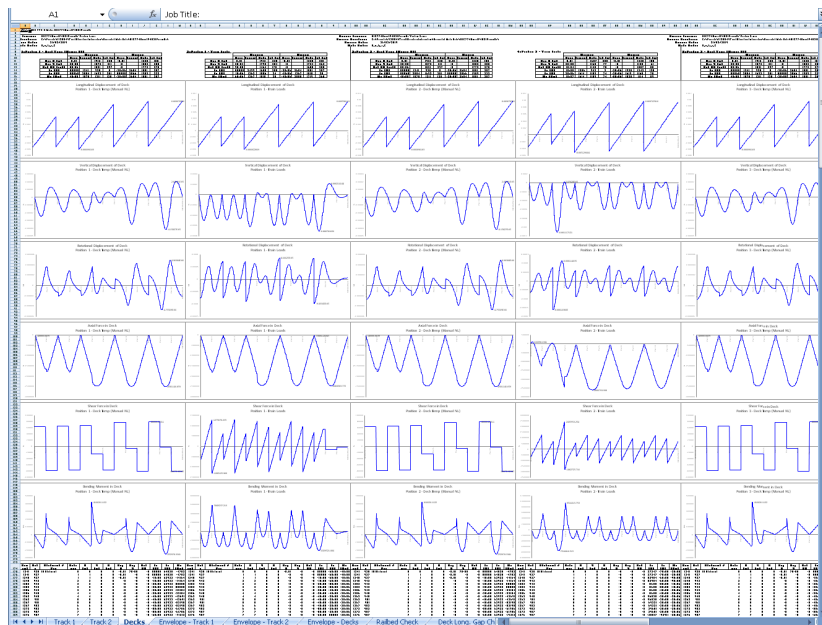


Figure 77: Deck Worksheet for Multiple Results Files

If valid basic combinations or envelopes that match the criteria described in “*Post-processing of automatically defined groups*” (page 63) are present in the model then additional results for these will be tabulated into the XLSX worksheets for the decks. For basic combinations a warning will be added at the top of the extracted results indicating that basic combinations of nonlinear results are not strictly valid.

Additional Results from Enveloping

If more than one results file is loaded, basic combinations are defined in the model that may be post-processed (see the restrictions under the “*Post-processing of automatically defined groups*” section on page 63) and enveloping has been selected then additional envelope results output can be generated by the post-processor in separate worksheets in the XLSX format spreadsheet. These additional worksheets include envelopes of the raw results and summary tables for key results that are required for checking against the UIC774-3 code. The track and deck envelopes produce the same summary tables, graphs and results highlighted in the previous two sections for the following envelopes:

- ☐ **Maximum and minimum envelopes for temperature loading only**
- ☐ **Maximum and minimum envelopes for temperature and trainset rail loading**
- ☐ **Maximum and minimum envelopes for all of the basic combinations defined in the model (if valid basic combinations are present)**
- ☐ **Maximum and minimum envelopes for all configurations (an envelope of all of the above results – temperature only, temperature and trainset, basic combinations)**

The additional UIC774-3 summary tables output by the post-processor are dependent upon the configuration of the model (the number of tracks and the number of decks in the structure) but will include some or all of the following tables:

- ☐ **Longitudinal Relative Displacement of Railbed (Relative Displacement between Rails and Deck)**
- ☐ **Longitudinal Relative Displacement between Ends of Decks (Axial)**
- ☐ **Longitudinal Relative Displacement between Ends of Decks (End Rotations)**
- ☐ **Longitudinal Relative Displacement between Ends of Decks (Total Effects)**
- ☐ **Vertical Relative Displacement between Ends of Decks**
- ☐ **Longitudinal Reactions**
- ☐ **Axial Rail Stress**



Note. The ‘total effect’ longitudinal relative displacement between the ends of the decks is the sum of the axial movement of the deck support position and the movement of the top of the deck from the rotation of the deck about this support position.

Sample tables are shown in the following figures which provide the peak values, the track that the peak is occurring in (if appropriate), the distance from the left end of the structure of the peak and also a description of where the peak is occurring. In all of the worksheets the worst effects are highlighted in bold and blue text to allow the quick determination of which analysis is causing the worst effects for each of the checks that need to be performed.

Check of Longitudinal Relative Displacement of Railbed (Relative Displacement between Rails and Deck)										
Job Title: UC774-3 Model UC774HeadR0Param Analysis (Resource): UC774HeadR0Param Position 1 UC774HeadR0Param Position 10 Model Orientation: Co-Planar/Ortho/Not Tail/Non-Intersection Analysis Date: 2003/01/01 Model Date: N/A/3/0										
Analysis ID	Resource Filename	Track 1			Track 2			Peak Relative Longitudinal Displacement between Rails and Deck (in)	Track Number with Peak Displacement	Distance from Left End of Structure to Peak Displacement
		Loading Type	Distance from Left End of the Model to the Starting Position of the	Distance from Left End of the Model to the Finishing Position of the	Loading Type	Distance from Left End of the Model to the Starting Position of the	Distance from Left End of the Model to the Finishing Position of the			
1	UC774HeadR0Param Position 1tmp	Temperature Only	0	360	Temperature Only	0	360	0.007393287	1	320
2	UC774HeadR0Param Position 2tmp	Braking	0.15	300.25	Accelerating	30.25	400.25	0.00779224	2	320
3	UC774HeadR0Param Position 3tmp	Braking	1.32	291.75	Accelerating	131.75	391.75	0.00737024	3	320
4	UC774HeadR0Param Position 4tmp	Braking	2.5	283.25	Accelerating	248.25	348.25	0.00735824	4	320
5	UC774HeadR0Param Position 5tmp	Braking	3.67	274.75	Accelerating	349.75	349.75	0.00734624	5	320
6	UC774HeadR0Param Position 6tmp	Braking	4.85	266.25	Accelerating	450.75	340.75	0.00733424	6	320
7	UC774HeadR0Param Position 7tmp	Braking	6.02	257.75	Accelerating	551.75	331.75	0.00732224	7	320
8	UC774HeadR0Param Position 8tmp	Braking	7.19	249.25	Accelerating	652.75	322.75	0.00731024	8	320
9	UC774HeadR0Param Position 9tmp	Braking	8.37	240.75	Accelerating	753.75	313.75	0.00729824	9	320
10	UC774HeadR0Param Position 10tmp	Braking	9.54	232.25	Accelerating	854.75	304.75	0.00728624	10	320
11	UC774HeadR0Param Position 11tmp	Braking	10.72	223.75	Accelerating	955.75	295.75	0.00727424	11	320
12	UC774HeadR0Param Position 12tmp	Braking	11.89	215.25	Accelerating	1056.75	286.75	0.00726224	12	320
13	UC774HeadR0Param Position 13tmp	Braking	13.07	206.75	Accelerating	1157.75	277.75	0.00725024	13	320
14	UC774HeadR0Param Position 14tmp	Braking	14.24	198.25	Accelerating	1258.75	268.75	0.00723824	14	320
15	UC774HeadR0Param Position 15tmp	Braking	15.42	189.75	Accelerating	1359.75	259.75	0.00722624	15	320
16	UC774HeadR0Param Position 16tmp	Braking	16.59	181.25	Accelerating	1460.75	250.75	0.00721424	16	320
17	UC774HeadR0Param Position 17tmp	Braking	17.77	172.75	Accelerating	1561.75	241.75	0.00720224	17	320
18	UC774HeadR0Param Position 18tmp	Braking	18.94	164.25	Accelerating	1662.75	232.75	0.00719024	18	320
19	UC774HeadR0Param Position 19tmp	Braking	20.12	155.75	Accelerating	1763.75	223.75	0.00717824	19	320
20	UC774HeadR0Param Position 20tmp	Braking	21.29	147.25	Accelerating	1864.75	214.75	0.00716624	20	320
21	UC774HeadR0Param Position 21tmp	Braking	22.47	138.75	Accelerating	1965.75	205.75	0.00715424	21	320
22	UC774HeadR0Param Position 22tmp	Braking	23.64	130.25	Accelerating	2066.75	196.75	0.00714224	22	320
23	UC774HeadR0Param Position 23tmp	Braking	24.82	121.75	Accelerating	2167.75	187.75	0.00713024	23	320
24	UC774HeadR0Param Position 24tmp	Braking	25.99	113.25	Accelerating	2268.75	178.75	0.00711824	24	320
25	UC774HeadR0Param Position 25tmp	Braking	27.17	104.75	Accelerating	2369.75	169.75	0.00710624	25	320
26	UC774HeadR0Param Position 26tmp	Braking	28.34	96.25	Accelerating	2470.75	160.75	0.00709424	26	320
27	UC774HeadR0Param Position 27tmp	Braking	29.52	87.75	Accelerating	2571.75	151.75	0.00708224	27	320
28	UC774HeadR0Param Position 28tmp	Braking	30.69	79.25	Accelerating	2672.75	142.75	0.00707024	28	320
29	UC774HeadR0Param Position 29tmp	Braking	31.87	70.75	Accelerating	2773.75	133.75	0.00705824	29	320
30	UC774HeadR0Param Position 30tmp	Braking	33.04	62.25	Accelerating	2874.75	124.75	0.00704624	30	320
31	UC774HeadR0Param Position 31tmp	Braking	34.22	53.75	Accelerating	2975.75	115.75	0.00703424	31	320
32	UC774HeadR0Param Position 32tmp	Braking	35.39	45.25	Accelerating	3076.75	106.75	0.00702224	32	320
33	UC774HeadR0Param Position 33tmp	Braking	36.57	36.75	Accelerating	3177.75	97.75	0.00701024	33	320
34	UC774HeadR0Param Position 34tmp	Braking	37.74	28.25	Accelerating	3278.75	88.75	0.00699824	34	320
35	UC774HeadR0Param Position 35tmp	Braking	38.92	19.75	Accelerating	3379.75	79.75	0.00698624	35	320
36	UC774HeadR0Param Position 36tmp	Braking	40.09	11.25	Accelerating	3480.75	70.75	0.00697424	36	320
37	UC774HeadR0Param Position 37tmp	Braking	41.27	2.75	Accelerating	3581.75	61.75	0.00696224	37	320
38	UC774HeadR0Param Position 38tmp	Braking	42.44	-6.75	Accelerating	3682.75	52.75	0.00695024	38	320
39	UC774HeadR0Param Position 39tmp	Braking	43.62	-15.25	Accelerating	3783.75	43.75	0.00693824	39	320
40	UC774HeadR0Param Position 40tmp	Braking	44.79	-23.75	Accelerating	3884.75	34.75	0.00692624	40	320
41	UC774HeadR0Param Position 41tmp	Braking	45.97	-32.25	Accelerating	3985.75	25.75	0.00691424	41	320
42	UC774HeadR0Param Position 42tmp	Braking	47.14	-40.75	Accelerating	4086.75	16.75	0.00690224	42	320
43	UC774HeadR0Param Position 43tmp	Braking	48.32	-49.25	Accelerating	4187.75	7.75	0.00689024	43	320
44	UC774HeadR0Param Position 44tmp	Braking	49.49	-57.75	Accelerating	4288.75	-1.75	0.00687824	44	320
45	UC774HeadR0Param Position 45tmp	Braking	50.67	-66.25	Accelerating	4389.75	-10.75	0.00686624	45	320
46	UC774HeadR0Param Position 46tmp	Braking	51.84	-74.75	Accelerating	4490.75	-19.75	0.00685424	46	320
47	UC774HeadR0Param Position 47tmp	Braking	53.02	-83.25	Accelerating	4591.75	-28.75	0.00684224	47	320
48	UC774HeadR0Param Position 48tmp	Braking	54.19	-91.75	Accelerating	4692.75	-37.75	0.00683024	48	320
49	UC774HeadR0Param Position 49tmp	Braking	55.37	-100.25	Accelerating	4793.75	-46.75	0.00681824	49	320
50	UC774HeadR0Param Position 50tmp	Braking	56.54	-108.75	Accelerating	4894.75	-55.75	0.00680624	50	320
51	UC774HeadR0Param Position 51tmp	Braking	57.72	-117.25	Accelerating	4995.75	-64.75	0.00679424	51	320
52	UC774HeadR0Param Position 52tmp	Braking	58.89	-125.75	Accelerating	5096.75	-73.75	0.00678224	52	320
53	UC774HeadR0Param Position 53tmp	Braking	60.07	-134.25	Accelerating	5197.75	-82.75	0.00677024	53	320
54	UC774HeadR0Param Position 54tmp	Braking	61.24	-142.75	Accelerating	5298.75	-91.75	0.00675824	54	320
55	UC774HeadR0Param Position 55tmp	Braking	62.42	-151.25	Accelerating	5399.75	-100.75	0.00674624	55	320
56	UC774HeadR0Param Position 56tmp	Braking	63.59	-159.75	Accelerating	5500.75	-109.75	0.00673424	56	320
57	UC774HeadR0Param Position 57tmp	Braking	64.77	-168.25	Accelerating	5601.75	-118.75	0.00672224	57	320
58	UC774HeadR0Param Position 58tmp	Braking	65.94	-176.75	Accelerating	5702.75	-127.75	0.00671024	58	320
59	UC774HeadR0Param Position 59tmp	Braking	67.12	-185.25	Accelerating	5803.75	-136.75	0.00669824	59	320
60	UC774HeadR0Param Position 60tmp	Braking	68.29	-193.75	Accelerating	5904.75	-145.75	0.00668624	60	320
61	UC774HeadR0Param Position 61tmp	Braking	69.47	-202.25	Accelerating	6005.75	-154.75	0.00667424	61	320
62	UC774HeadR0Param Position 62tmp	Braking	70.64	-210.75	Accelerating	6106.75	-163.75	0.00666224	62	320
63	UC774HeadR0Param Position 63tmp	Braking	71.82	-219.25	Accelerating	6207.75	-172.75	0.00665024	63	320
64	UC774HeadR0Param Position 64tmp	Braking	72.99	-227.75	Accelerating	6308.75	-181.75	0.00663824	64	320
65	UC774HeadR0Param Position 65tmp	Braking	74.17	-236.25	Accelerating	6409.75	-190.75	0.00662624	65	320
66	UC774HeadR0Param Position 66tmp	Braking	75.34	-244.75	Accelerating	6510.75	-199.75	0.00661424	66	320
67	UC774HeadR0Param Position 67tmp	Braking	76.52	-253.25	Accelerating	6611.75	-208.75	0.00660224	67	320
68	UC774HeadR0Param Position 68tmp	Braking	77.69	-261.75	Accelerating	6712.75	-217.75	0.00659024	68	320
69	UC774HeadR0Param Position 69tmp	Braking	78.87	-270.25	Accelerating	6813.75	-226.75	0.00657824	69	320
70	UC774HeadR0Param Position 70tmp	Braking	80.04	-278.75	Accelerating	6914.75	-235.75	0.00656624	70	320
71	UC774HeadR0Param Position 71tmp	Braking	81.22	-287.25	Accelerating	7015.75	-244.75	0.00655424	71	320
72	UC774HeadR0Param Position 72tmp	Braking	82.39	-295.75	Accelerating	7116.75	-253.75	0.00654224	72	320
73	UC774HeadR0Param Position 73tmp	Braking	83.57	-304.25	Accelerating	7217.75	-262.75	0.00653024	73	320
74	UC774HeadR0Param Position 74tmp	Braking	84.74	-312.75	Accelerating	7318.75	-271.75	0.00651824	74	320
75	UC774HeadR0Param Position 75tmp	Braking	85.92	-321.25	Accelerating	7419.75	-280.75	0.00650624	75	320
76	UC774HeadR0Param Position 76tmp	Braking	87.09	-329.75	Accelerating	7520.75	-289.75	0.00649424	76	320
77	UC774HeadR0Param Position 77tmp	Braking	88.27	-338.25	Accelerating	7621.75	-298.75	0.00648224	77	320
78	UC774HeadR0Param Position 78tmp	Braking	89.44	-346.75	Accelerating	7722.75	-307.75	0.00647024	78	320
79	UC774HeadR0Param Position 79tmp	Braking	90.62	-355.25	Accelerating	7823.75	-316.75	0.00645824	79	320
80	UC774HeadR0Param Position 80tmp	Braking	91.79	-363.75	Accelerating	7924.75	-325.75	0.00644624	80	320
81	UC774HeadR0Param Position 81tmp	Braking	92.97	-372.25	Accelerating	8025.75	-334.75	0.00643424	81	320
82	UC774HeadR0Param Position 82tmp	Braking	94.14	-380.75	Accelerating	8126.75	-343.75	0.00642224	82	320
83	UC774HeadR0Param Position 83tmp	Braking	95.32	-389.25	Accelerating	8227.75	-352.75	0.00641024	83	320
84	UC774HeadR0Param Position 84tmp	Braking	96.49	-397.75	Accelerating	8328.75	-361.75	0.00639824	84	320
85	UC774HeadR0Param Position 85tmp	Braking	97.67	-406.25	Accelerating	8429.75	-370.75	0.00638624	85	320
86	UC774HeadR0Param Position 86tmp	Braking	98.84	-414.75	Accelerating	8530.75	-379.75	0.00637424	86	320
87	UC774HeadR0Param Position 87tmp	Braking	100.02	-423.25	Accelerating	8631.75	-388.75	0.00636224	87	320
88	UC774HeadR0Param Position 88tmp	Braking	101.19	-431.75	Accelerating	8732.75	-397.75	0.00635024	88	320
89	UC774HeadR0Param Position 89tmp	Braking	102.37	-440.25	Accelerating	8833.75	-406.75	0.00633824	89	320
90	UC774HeadR0Param Position 90tmp	Braking	103.54	-448.75	Accelerating	8934.75	-415.75	0.00632624	90	320
91	UC774HeadR0Param Position 91tmp	Braking	104.72	-457.25	Accelerating	9035.75	-424.75	0.00631424	91	320
92	UC774HeadR0Param Position 92tmp	Braking	105.89	-465.75	Accelerating	9136.75	-433.75	0.00630224	92	320
93	UC774HeadR0Param Position 93tmp	Braking	107.07	-474.25	Accelerating	9237.75	-442.75	0.00629024	93	320
94	UC774HeadR0Param Position 94tmp	Braking	108.24	-482.75	Accelerating	9338.75	-451.75	0.00627824	94	320
95	UC774HeadR0Param Position 95tmp	Braking	109.42	-491.25	Accelerating	9439.75	-460.75	0.00626624	95	320
96	UC774HeadR0Param Position 96tmp	Braking	110.59	-499.75	Accelerating	9540.75	-469.75	0.00625424	96	320
97	UC774HeadR0Param Position 97tmp	Braking	111.77	-508.25	Accelerating	9641.75	-478.75	0	97	320

**Figure 79: Longitudinal Deck End Displacement due to Axial Effects Check Worksheet
for Multiple Results Files**

**Figure 80: Longitudinal Deck End Displacement due to End Rotation Effects Check
Worksheet for Multiple Results Files**

Rail Track Analysis User Manual

Check of Longitudinal Relative Displacement between Ends of Decks (Total Effects)													
Job Title: UC7-17-Hsct UC774-wsl029-Param Analysis Pattern: UC774-wsl029-Param Train 1 - UC774-wsl029-Param Train 51 Component: C-Programa125047-wsl029-Param Train 51 Model: UC774-wsl029-Param Train 51 Model User: N/A;G;C													
Analysis ID	Element's Filename	Track 1			Track 2			Peak Relative Longitudinal Displacement of Ends of Decks, Position	Location Number / Location Coordinates of Decks with				
		Loading Type	Distance from Left End of the Deck to the Starting	Distance from Left End of the Deck to the Finishing	Loading Type	Distance from Left End of the Deck to the Starting	Distance from Left End of the Deck to the Finishing						
1	UC774-wsl029-Param Train 1.mst	Temperature Dbl	0	300	Temperature Dbl	300	600	-0.01642E+00	1				
2	UC774-wsl029-Param Train 2.mst	Damping	306	302	Damping	306	602	-0.00344E+00	2				
3	UC774-wsl029-Param Train 3.mst	Damping	315	312	Damping	306	606	-0.00444E+00	3				
4	UC774-wsl029-Param Train 4.mst	Damping	318	315	Damping	318	609	-0.00444E+00	4				
5	UC774-wsl029-Param Train 5.mst	Damping	325	322	Damping	318	612	-0.00444E+00	5				
6	UC774-wsl029-Param Train 6.mst	Damping	332	329	Damping	318	615	-0.00444E+00	6				
7	UC774-wsl029-Param Train 7.mst	Damping	337	334	Damping	318	618	-0.00444E+00	7				
8	UC774-wsl029-Param Train 8.mst	Damping	343	340	Damping	318	622	-0.00444E+00	8				
9	UC774-wsl029-Param Train 9.mst	Damping	350	347	Damping	318	626	-0.00444E+00	9				
10	UC774-wsl029-Param Train 10.mst	Damping	356	353	Damping	318	630	-0.00444E+00	10				
11	UC774-wsl029-Param Train 11.mst	Damping	363	360	Damping	318	634	-0.00444E+00	11				
12	UC774-wsl029-Param Train 12.mst	Damping	369	366	Damping	318	638	-0.00444E+00	12				
13	UC774-wsl029-Param Train 13.mst	Damping	375	372	Damping	318	642	-0.00444E+00	13				
14	UC774-wsl029-Param Train 14.mst	Damping	381	378	Damping	318	646	-0.00444E+00	14				
15	UC774-wsl029-Param Train 15.mst	Damping	387	384	Damping	318	650	-0.00444E+00	15				
16	UC774-wsl029-Param Train 16.mst	Damping	393	390	Damping	318	654	-0.00444E+00	16				
17	UC774-wsl029-Param Train 17.mst	Damping	399	396	Damping	318	658	-0.00444E+00	17				
18	UC774-wsl029-Param Train 18.mst	Damping	405	402	Damping	318	662	-0.00444E+00	18				
19	UC774-wsl029-Param Train 19.mst	Damping	411	408	Damping	318	666	-0.00444E+00	19				
20	UC774-wsl029-Param Train 20.mst	Damping	417	414	Damping	318	670	-0.00444E+00	20				
21	UC774-wsl029-Param Train 21.mst	Damping	423	420	Damping	318	674	-0.00444E+00	21				
22	UC774-wsl029-Param Train 22.mst	Damping	429	426	Damping	318	678	-0.00444E+00	22				
23	UC774-wsl029-Param Train 23.mst	Damping	435	432	Damping	318	682	-0.00444E+00	23				
24	UC774-wsl029-Param Train 24.mst	Damping	441	438	Damping	318	686	-0.00444E+00	24				
25	UC774-wsl029-Param Train 25.mst	Damping	447	444	Damping	318	690	-0.00444E+00	25				
26	UC774-wsl029-Param Train 26.mst	Damping	453	450	Damping	318	694	-0.00444E+00	26				
27	UC774-wsl029-Param Train 27.mst	Damping	459	456	Damping	318	698	-0.00444E+00	27				
28	UC774-wsl029-Param Train 28.mst	Damping	465	462	Damping	318	702	-0.00444E+00	28				
29	UC774-wsl029-Param Train 29.mst	Damping	471	468	Damping	318	706	-0.00444E+00	29				
30	UC774-wsl029-Param Train 30.mst	Damping	477	474	Damping	318	710	-0.00444E+00	30				
31	UC774-wsl029-Param Train 31.mst	Damping	483	480	Damping	318	714	-0.00444E+00	31				
32	UC774-wsl029-Param Train 32.mst	Damping	489	486	Damping	318	718	-0.00444E+00	32				
33	UC774-wsl029-Param Train 33.mst	Damping	495	492	Damping	318	722	-0.00444E+00	33				
34	UC774-wsl029-Param Train 34.mst	Damping	501	498	Damping	318	726	-0.00444E+00	34				
35	UC774-wsl029-Param Train 35.mst	Damping	507	504	Damping	318	730	-0.00444E+00	35				
36	UC774-wsl029-Param Train 36.mst	Damping	513	510	Damping	318	734	-0.00444E+00	36				
37	UC774-wsl029-Param Train 37.mst	Damping	519	516	Damping	318	738	-0.00444E+00	37				
38	UC774-wsl029-Param Train 38.mst	Damping	525	522	Damping	318	742	-0.00444E+00	38				
39	UC774-wsl029-Param Train 39.mst	Damping	531	528	Damping	318	746	-0.00444E+00	39				
40	UC774-wsl029-Param Train 40.mst	Damping	537	534	Damping	318	750	-0.00444E+00	40				
41	UC774-wsl029-Param Train 41.mst	Damping	543	540	Damping	318	754	-0.00444E+00	41				
42	UC774-wsl029-Param Train 42.mst	Damping	549	546	Damping	318	758	-0.00444E+00	42				
43	UC774-wsl029-Param Train 43.mst	Damping	555	552	Damping	318	762	-0.00444E+00	43				
44	UC774-wsl029-Param Train 44.mst	Damping	561	558	Damping	318	766	-0.00444E+00	44				
45	UC774-wsl029-Param Train 45.mst	Damping	567	564	Damping	318	770	-0.00444E+00	45				
46	UC774-wsl029-Param Train 46.mst	Damping	573	570	Damping	318	774	-0.00444E+00	46				
47	UC774-wsl029-Param Train 47.mst	Damping	579	576	Damping	318	778	-0.00444E+00	47				
48	UC774-wsl029-Param Train 48.mst	Damping	585	582	Damping	318	782	-0.00444E+00	48				
49	UC774-wsl029-Param Train 49.mst	Damping	591	588	Damping	318	786	-0.00444E+00	49				
50	UC774-wsl029-Param Train 50.mst	Damping	597	594	Damping	318	790	-0.00444E+00	50				
51	UC774-wsl029-Param Train 51.mst	Damping	603	600	Damping	318	794	-0.00444E+00	51				
52	UC774-wsl029-Param Train 52.mst	Damping	609	606	Damping	318	798	-0.00444E+00	52				
53	UC774-wsl029-Param Train 53.mst	Damping	615	612	Damping	318	802	-0.00444E+00	53				
54	UC774-wsl029-Param Train 54.mst	Damping	621	618	Damping	318	806	-0.00444E+00	54				
55	UC774-wsl029-Param Train 55.mst	Damping	627	624	Damping	318	810	-0.00444E+00	55				
56	UC774-wsl029-Param Train 56.mst	Damping	633	630	Damping	318	814	-0.00444E+00	56				
57	UC774-wsl029-Param Train 57.mst	Damping	639	636	Damping	318	818	-0.00444E+00	57				
58	UC774-wsl029-Param Train 58.mst	Damping	645	642	Damping	318	822	-0.00444E+00	58				
59	UC774-wsl029-Param Train 59.mst	Damping	651	648	Damping	318	826	-0.00444E+00	59				
60	UC774-wsl029-Param Train 60.mst	Damping	657	654	Damping	318	830	-0.00444E+00	60				

Figure 81: Longitudinal Deck End Displacement due to Total Effects Check Worksheet for Multiple Results Files

Check of Vertical Relative Displacement between Ends of Decks

Job Title	UC774-M364 UC774-M364EParam
Analysis Element	UC774-M364EParam 1 - UC774-M364EParam Position 50
Model Definition	Project 12/20/2014 Model Construction
Analysis Dates	0000007 - 0000020
Model Units	N/A,N/C

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Figure 82: Vertical Deck End Displacement Check Worksheet for Multiple Results Files

Rail Track Analysis Results Spreadsheet

Check of Longitudinal Reactions									
Job Title: UC 774-3 Model UC774hnd0 Param Analysis Filename: UC774hnd0ParamPosition 1 Model Directory: C:\Program Files\ESRI\RailSim\Simulation Analysis Date: 28/03/2019 Model User: Tom J.C.									
Analysis ID	Results Filename	Loading Type	Distance from Left End of the Model to the Start of the Loading	Distance from Left End of the Model to the End of the Loading	Loading Type	Distance from Left End of the Model to the Start of the Loading	Distance from Left End of the Model to the End of the Loading	Peak Longitudinal Reaction (N)	Abutment / Pier Number with Peak Reaction
1	UC774hnd0ParamPosition 1.mst	Temperature Only	0	300	Temperature Only	300	600	30043.4137	Per 5
2	UC774hnd0ParamPosition 1.mst	Braking	6.25	308.25	Accelerating	303.25	603.25	24493.4462	Per 5
3	UC774hnd0ParamPosition 1.mst	Braking	12.5	316.5	Accelerating	306.5	606.5	22993.3948	Per 5
4	UC774hnd0ParamPosition 1.mst	Braking	18.75	318.75	Accelerating	309.75	609.75	20871.9438	Per 1
5	UC774hnd0ParamPosition 1.mst	Braking	25	325	Accelerating	315	615	20672.9836	Per 1
6	UC774hnd0ParamPosition 1.mst	Braking	31.25	331.25	Accelerating	318.25	618.25	23772.7663	Per 1
7	UC774hnd0ParamPosition 1.mst	Braking	37.5	337.5	Accelerating	321.5	621.5	23520.3019	Per 1
8	UC774hnd0ParamPosition 1.mst	Braking	43.75	343.75	Accelerating	322.75	622.75	23708.8442	Per 1
9	UC774hnd0ParamPosition 1.mst	Braking	50	350	Accelerating	328	628	23768.0385	Per 1
10	UC774hnd0ParamPosition 1.mst	Braking	56.25	356.25	Accelerating	329.25	629.25	23955.9487	Per 1
11	UC774hnd0ParamPosition 1.mst	Braking	62.5	362.5	Accelerating	332.5	632.5	23850.4385	Per 1
12	UC774hnd0ParamPosition 1.mst	Braking	68.75	368.75	Accelerating	335.75	635.75	24503.8493	Per 3
13	UC774hnd0ParamPosition 1.mst	Braking	75	375	Accelerating	338	638	24768.0385	Per 3
14	UC774hnd0ParamPosition 1.mst	Braking	81.25	381.25	Accelerating	342.25	642.25	23923.8377	Per 3
15	UC774hnd0ParamPosition 1.mst	Braking	87.5	387.5	Accelerating	345.5	645.5	24454.4571	Per 3
16	UC774hnd0ParamPosition 1.mst	Braking	93.75	393.75	Accelerating	348.75	648.75	207463.8858	Per 3
17	UC774hnd0ParamPosition 1.mst	Braking	100	400	Accelerating	352	652	20344.4571	Per 3
18	UC774hnd0ParamPosition 1.mst	Braking	106.25	406.25	Accelerating	355.25	655.25	20814.7352	Per 3
19	UC774hnd0ParamPosition 1.mst	Braking	112.5	412.5	Accelerating	358.5	658.5	20481.3752	Per 3
20	UC774hnd0ParamPosition 1.mst	Braking	118.75	418.75	Accelerating	361.75	661.75	21003.329	Per 3
21	UC774hnd0ParamPosition 1.mst	Braking	125	425	Accelerating	365	665	20340.0385	Per 3
22	UC774hnd0ParamPosition 1.mst	Braking	131.25	431.25	Accelerating	368.25	668.25	20496.2598	Per 3
23	UC774hnd0ParamPosition 1.mst	Braking	137.5	437.5	Accelerating	371.5	671.5	21151.4385	Per 3
24	UC774hnd0ParamPosition 1.mst	Braking	143.75	443.75	Accelerating	374.75	674.75	21771.5242	Per 3
25	UC774hnd0ParamPosition 1.mst	Braking	150	450	Accelerating	378	678	20672.9836	Per 3
26	UC774hnd0ParamPosition 1.mst	Braking	156.25	456.25	Accelerating	381.25	681.25	20496.2598	Per 3
27	UC774hnd0ParamPosition 1.mst	Braking	162.5	462.5	Accelerating	384.5	684.5	21151.4385	Per 3
28	UC774hnd0ParamPosition 1.mst	Braking	168.75	468.75	Accelerating	387.75	687.75	21230.8177	Per 3
29	UC774hnd0ParamPosition 1.mst	Braking	175	475	Accelerating	391	691	20340.0385	Per 3
30	UC774hnd0ParamPosition 1.mst	Braking	181.25	481.25	Accelerating	394.25	694.25	20346.9598	Per 3
31	UC774hnd0ParamPosition 1.mst	Braking	187.5	487.5	Accelerating	397.5	697.5	20375.8571	Per 3
32	UC774hnd0ParamPosition 1.mst	Braking	193.75	493.75	Accelerating	400.75	700.75	20479.554	Per 3
33	UC774hnd0ParamPosition 1.mst	Braking	200	500	Accelerating	404	704	20340.0385	Per 3
34	UC774hnd0ParamPosition 1.mst	Braking	206.25	506.25	Accelerating	407.25	707.25	20397.2598	Per 3
35	UC774hnd0ParamPosition 1.mst	Braking	212.5	512.5	Accelerating	410.5	710.5	21151.4385	Per 3
36	UC774hnd0ParamPosition 1.mst	Braking	218.75	518.75	Accelerating	413.75	713.75	21721.5242	Per 3
37	UC774hnd0ParamPosition 1.mst	Braking	225	525	Accelerating	417	717	20672.9836	Per 3
38	UC774hnd0ParamPosition 1.mst	Braking	231.25	531.25	Accelerating	420.25	720.25	21371.804	Per 3
39	UC774hnd0ParamPosition 1.mst	Braking	237.5	537.5	Accelerating	423.5	723.5	21151.4385	Per 3
40	UC774hnd0ParamPosition 1.mst	Braking	243.75	543.75	Accelerating	426.75	726.75	20047.478	Per 3
41	UC774hnd0ParamPosition 1.mst	Braking	250	550	Accelerating	430	730	20340.0385	Per 3
42	UC774hnd0ParamPosition 1.mst	Braking	256.25	556.25	Accelerating	433.25	733.25	20714.7352	Per 3
43	UC774hnd0ParamPosition 1.mst	Braking	262.5	562.5	Accelerating	436.5	736.5	20340.0385	Per 3
44	UC774hnd0ParamPosition 1.mst	Braking	268.75	568.75	Accelerating	439.75	739.75	20703.029	Per 3
45	UC774hnd0ParamPosition 1.mst	Braking	275	575	Accelerating	443	743	20340.0385	Per 3
46	UC774hnd0ParamPosition 1.mst	Braking	281.25	581.25	Accelerating	446.25	746.25	21230.8177	Per 3
47	UC774hnd0ParamPosition 1.mst	Braking	287.5	587.5	Accelerating	449.5	749.5	21151.4385	Per 3
48	UC774hnd0ParamPosition 1.mst	Braking	293.75	593.75	Accelerating	452.75	752.75	21179.57	Per 3
49	UC774hnd0ParamPosition 1.mst	Braking	300	600	Accelerating	456	756	20340.0385	Per 3
50	UC774hnd0ParamPosition 1.mst	Braking	306.25	606.25	Accelerating	459.25	759.25	21470.9877	Per 3
51	UC774hnd0ParamPosition 1.mst	Braking	312.5	612.5	Accelerating	462.5	762.5	21151.4385	Per 3
52	UC774hnd0ParamPosition 1.mst	Braking	318.75	618.75	Accelerating	465.75	765.75	21249.272	Per 3
53	UC774hnd0ParamPosition 1.mst	Braking	325	625	Accelerating	469	769	20340.0385	Per 3
54	UC774hnd0ParamPosition 1.mst	Braking	331.25	631.25	Accelerating	472.25	772.25	21502.108	Per 3
55	UC774hnd0ParamPosition 1.mst	Braking	337.5	637.5	Accelerating	475.5	775.5	21151.4385	Per 3
56	UC774hnd0ParamPosition 1.mst	Braking	343.75	643.75	Accelerating	478.75	778.75	21748.68	Per 3
57	UC774hnd0ParamPosition 1.mst	Braking	400	700	Accelerating	480	780	21502.108	Per 3
58	UC774hnd0ParamPosition 1.mst	Braking	356.25	656.25	Accelerating	476.25	766.25	21546.535	Per 3

Figure 83: Longitudinal Reaction Check Worksheet for Multiple Results Files

Check of Axial Rail Stress									
Job Title: UC 774-3 Model UC774hnd0 Param Analysis Filename: UC774hnd0ParamPosition 1 Model Directory: C:\Program Files\ESRI\RailSim\Simulation Analysis Date: 28/03/2019 Model User: Tom J.C.									
Analysis ID	Results Filename	Loading Type	Distance from Left End of the Model to the Start of the Loading m	Distance from Left End of the Model to the End of the Loading m	Loading Type	Distance from Left End of the Model to the Start of the Loading m	Distance from Left End of the Model to the End of the Loading m	Peak Longitudinal Reaction (N)	Abutment / Pier Number with Peak Reaction
1	UC774hnd0ParamPosition 1.mst	Temperature Only	0	300	Temperature Only	300	600	30043.4137	Per 5
2	UC774hnd0ParamPosition 1.mst	Braking	6.25	308.25	Accelerating	303.25	603.25	24493.4462	Per 5
3	UC774hnd0ParamPosition 1.mst	Braking	12.5	316.5	Accelerating	306.5	606.5	22993.3948	Per 5
4	UC774hnd0ParamPosition 1.mst	Braking	18.75	318.75	Accelerating	309.75	609.75	20871.9438	Per 1
5	UC774hnd0ParamPosition 1.mst	Braking	25	325	Accelerating	315	615	20672.9836	Per 1
6	UC774hnd0ParamPosition 1.mst	Braking	31.25	331.25	Accelerating	318.25	618.25	23772.7663	Per 1
7	UC774hnd0ParamPosition 1.mst	Braking	37.5	337.5	Accelerating	321.5	621.5	23520.3019	Per 1
8	UC774hnd0ParamPosition 1.mst	Braking	43.75	343.75	Accelerating	322.75	622.75	23708.8442	Per 1
9	UC774hnd0ParamPosition 1.mst	Braking	50	350	Accelerating	328	628	23768.0385	Per 1
10	UC774hnd0ParamPosition 1.mst	Braking	56.25	356.25	Accelerating	329.25	629.25	23955.9487	Per 1
11	UC774hnd0ParamPosition 1.mst	Braking	62.5	362.5	Accelerating	332.5	632.5	23850.4385	Per 1
12	UC774hnd0ParamPosition 1.mst	Braking	68.75	368.75	Accelerating	335.75	635.75	24503.8493	Per 3
13	UC774hnd0ParamPosition 1.mst	Braking	75	375	Accelerating	338	638	24768.0385	Per 3
14	UC774hnd0ParamPosition 1.mst	Braking	81.25	381.25	Accelerating	342.25	642.25	23923.8377	Per 3
15	UC774hnd0ParamPosition 1.mst	Braking	87.5	387.5	Accelerating	345.5	645.5	24454.4571	Per 3
16	UC774hnd0ParamPosition 1.mst	Braking	93.75	393.75	Accelerating	348.75	648.75	207463.8858	Per 3
17	UC774hnd0ParamPosition 1.mst	Braking	100	400	Accelerating	352	652	20344.4571	Per 3
18	UC774hnd0ParamPosition 1.mst	Braking	106.25	406.25	Accelerating	355.25	655.25	20814.7352	Per 3
19	UC774hnd0ParamPosition 1.mst	Braking	112.5	412.5	Accelerating	358.5	658.5	20481.3752	Per 3
20	UC774hnd0ParamPosition 1.mst	Braking	118.75	418.75	Accelerating	361.75	661.75	21003.329	Per 3
21	UC774hnd0ParamPosition 1.mst	Braking	125	425	Accelerating	365	665	20340.0385	Per 3
22	UC774hnd0ParamPosition 1.mst	Braking	131.25	431.25	Accelerating	368.25	668.25	20496.2598	Per 3
23	UC774hnd0ParamPosition 1.mst	Braking	137.5	437.5	Accelerating	371.5	671.5	21151.4385	Per 3
24	UC774hnd0ParamPosition 1.mst	Braking	143.75	443.75	Accelerating	374.75	674.75	21771.5242	Per 3
25	UC774hnd0ParamPosition 1.mst	Braking	150	450	Accelerating	378	678	20672.9836	Per 3
26	UC774hnd0ParamPosition 1.mst	Braking	156.25	456.25	Accelerating	381.25	681.25	20496.2598	Per 3
27	UC774hnd0ParamPosition 1.mst	Braking	162.5	462.5	Accelerating	384.5	684.5	21151.4385	Per 3
28	UC774hnd0ParamPosition 1.mst	Braking	168.75	468.75	Accelerating	387.75	687.75	21230.8177	Per 3
29	UC774hnd0ParamPosition 1.mst	Braking	175	475	Accelerating	391	691	20340.0385	Per 3
30	UC774hnd0ParamPosition 1.mst	Braking	181.25	481.25	Accelerating	394.25	694.25	20346.9598	Per 3
31	UC774hnd0ParamPosition 1.mst	Braking	187.5	487.5	Accelerating	397.5	697.5	20375.8571	Per 3
32	UC774hnd0ParamPosition 1.mst	Braking	193.75	493.75	Accelerating	400.75	700.75	20479.554	Per 3
33	UC774hnd0ParamPosition 1.mst	Braking	200	500	Accelerating	404	704	20340.0385	Per 3
34	UC774hnd0ParamPosition 1.mst	Braking	206.25	506.25	Accelerating	407.25	707.25	20397.2598	Per 3
35	UC774hnd0ParamPosition 1.mst	Braking	212.5	512.5	Accelerating	410.5	710.5	21151.4385	Per 3
36	UC774hnd0ParamPosition 1.mst	Braking	218.75	518.75	Accelerating	413.75	713.75	21721.5242	Per 3
37	UC774hnd0ParamPosition 1.mst	Braking	225	525	Accelerating	417	717	20672.9836	Per 3
38	UC774hnd0ParamPosition 1.mst	Braking	231.25	531.25	Accelerating	420.25	720.25	21371.804	Per 3
39	UC774hnd0ParamPosition 1.mst	Braking	237.5	537.5	Accelerating	423.5	723.5	21151.4385	Per 3
40	UC774hnd0ParamPosition 1.mst	Braking	243.75	543.75	Accelerating	426.75	726.75	20047.478	Per 3
41	UC774hnd0ParamPosition 1.mst	Braking	250	550	Accelerating	430	730	20340.0385	Per 3
42	UC774hnd0ParamPosition 1.mst	Braking	256.25	556.25	Accelerating	433.25	733.25	20714.7352	Per 3
43	UC774hnd0ParamPosition 1.mst	Braking	262.5	562.5	Accelerating	436.5	736.5	20340.0385	Per 3
44	UC774hnd0ParamPosition 1.mst	Braking	268.75	568.75	Accelerating	439.75	739.75	20703.029	Per 3
45	UC774hnd0ParamPosition 1.mst	Braking	275	575	Accelerating	443	743	20340.0385	Per 3
46	UC774hnd0ParamPosition 1.mst	Braking	281.25	581.25	Accelerating	446.25	746.25	21230.8177	Per 3
47	UC774hnd0ParamPosition 1.mst	Braking	287.5	587.5	Accelerating	449.5	749.5	21151.4385	Per 3
48	UC774hnd0ParamPosition 1.mst	Braking	293.75	593.75	Accelerating	452.75	752.75	21179.57	Per 3
49	UC774hnd0ParamPosition 1.mst	Braking	300	600	Accelerating	456	756	20340.0385	Per 3
50	UC774hnd0ParamPosition 1.mst	Braking	306.25	606.25	Accelerating	459.25	759.25	20346.9598	Per 3
51	UC774hnd0ParamPosition 1.mst	Braking	312.5	612.5	Accelerating	462.5	762.5	20375.8571	Per 3
52	UC774hnd0ParamPosition 1.mst	Braking	318.75	618.75	Accelerating	465.75	765.75	20479.554	Per 3
53	UC774hnd0ParamPosition 1.mst	Braking	325	625	Accelerating	469	769	20340.0385	Per 3
54	UC774hnd0ParamPosition 1.mst	Braking	331.25	631.25	Accelerating	472.25	772.25	20346.9598	Per 3
55	UC774hnd0ParamPosition 1.mst	Braking	337.5	637.5	Accelerating	475.5	775.5	20375.8571	Per 3
56	UC774hnd0ParamPosition 1.mst	Braking	343.75	643.75	Accelerating	478.75	778.75	20479.554	Per 3
57	UC774hnd0ParamPosition 1.mst	Braking	350	650	Accelerating	482	782	20340.0385	Per 3
58	UC774hnd0ParamPosition 1.mst	Braking	356.25	656.25	Accelerating	485.25	785.25	20346.9598	Per 3
59	UC774hnd0ParamPosition 1.mst	Braking	362.5	662.5	Accelerating	488.5	788.5	20375.8571	Per 3
60	UC774hnd0ParamPosition 1.mst	Braking	368.75	668.75	Accelerating	491.75	791.75	20479.554	Per 3
61	UC774hnd0ParamPosition 1.mst	Braking	375	675	Accelerating	495	795	20340.0385	Per 3
62	UC774hnd0ParamPosition 1.mst	Braking	381.25	681.25	Accelerating	498.25	798.25	20346.9598	Per 3
63	UC774hnd0ParamPosition 1.mst	Braking	387.5	687.5	Accelerating	501.5	801.5	20375.8571	Per 3
64	UC774hnd0ParamPosition 1.mst	Braking	393.75	693.75	Accelerating	504.75	804.75	20479.554	Per 3
65	UC774hnd0ParamPosition 1.mst	Braking	400	700	Accelerating	508	808	20340.0385	Per 3
66	UC774hnd0ParamPosition 1.mst	Braking	406.25	706.25	Accelerating	511.25	811.25	20346.9598	Per 3
67	UC774hnd0ParamPosition 1.mst	Braking	412.5	712.5	Accelerating	514.5	814.5	20375.8571	Per 3
68	UC774hnd0ParamPosition 1.mst	Braking	418.75	718.75	Accelerating	517.75	817.75	20479.554	Per 3
69	UC774hnd0ParamPosition 1.mst	Braking	425	725	Accelerating	521	821	20340.0385	Per 3
70	UC774hnd0ParamPosition 1.mst	Braking	431.25	731.25	Accelerating	524.25	824.25	20346.9598	Per 3
71	UC774hnd0ParamPosition 1.mst	Braking	437.5	737.5	Accelerating	527.5	827.5	20375.8571	Per 3
72	UC774hnd0ParamPosition 1.mst	Braking	443.75	743.75	Accelerating	530.75	830.75	20479.554	Per 3
73	UC774hnd0ParamPosition 1.mst	Braking	450	750	Accelerating	534	834	20340.0385	Per 3
74	UC774hnd0ParamPosition 1.mst	Braking	456.25	756.25	Accelerating	537.25	837.25	20346.9598	Per 3
75	UC774hnd0ParamPosition 1.mst	Braking	462.5	762.5	Accelerating	540.5	840.5	20375.8571	Per 3
76	UC774hnd0ParamPosition 1.mst	Braking	468.75	768.75	Accelerating	543.75	843.75	20479.554	Per 3
77	UC774hnd0ParamPosition 1.mst	Braking	475	775	Accelerating	547	847	20340.0385	Per 3
78	UC774hnd0ParamPosition 1.mst	Braking	481.25	781.25	Accelerating	550.25	850.25	20346.9598	Per 3
79	UC774hnd0ParamPosition 1.mst	Braking	487.5	787.5	Accelerating	553.5	853.5	20375.8571	Per 3
80	UC774hnd0ParamPosition 1.mst	Braking	493.75	793.75	Accelerating	556.75	856.75	20479.554	Per 3
81	UC774hnd0ParamPosition 1.mst	Braking	500	800	Accelerating	560	860	20340.0385	Per 3
82	UC774hnd0ParamPosition 1.mst	Braking	506.25	806.25	Accelerating	563.25	863.25	20346.9598	Per 3
83	UC774hnd0ParamPosition 1.mst	Braking	512.5	812.5	Accelerating	566.5	866.5	20375.8571	Per 3
84	UC774hnd0ParamPosition 1.mst	Braking	518.75	818.75	Accelerating	569.75	869.75	20479.554	Per 3
85	UC774hnd0ParamPosition 1.mst	Braking	525	825	Accelerating	573	873	20340.0385	Per 3
86	UC774hnd0ParamPosition 1.mst	Braking	531.25	831.25	Accelerating	576.25	876.25	20346.9598	Per 3
87	UC774hnd0ParamPosition 1.mst	Braking	537.5	837.5	Accelerating	579.5	879.5	20375.8571	Per 3
88	UC774hnd0ParamPosition 1.mst	Braking	543.75	843.75	Accelerating	582.75	882.75	20479.554	Per 3
89	UC774hnd0ParamPosition 1.mst	Braking	550	850	Accelerating	586	886	20340.0385	Per 3
90	UC774hnd0ParamPosition 1.mst	Braking	556.25	856.25	Accelerating	589.25	889.25	20346.9598	Per 3
91	UC774hnd0ParamPosition 1.mst	Braking	562.5	862.5	Accelerating	592.5	892.5	20375.8571	Per 3
92	UC774hnd0ParamPosition 1.mst	Braking	568.75	868.75	Accelerating	595.75	895.75	20479.554	Per 3
93	UC774hnd0ParamPosition 1.mst	Braking	575	875	Accelerating	599	899	20340.0385	Per 3
94	UC774hnd0ParamPosition 1.mst	Braking	581.25	881.25	Accelerating	602.25	902.25	20346.9598	Per 3
95	UC774hnd0ParamPosition 1.mst	Braking	587.5	887.5	Accelerating	605.5	905.5	20375.8571	Per 3
96	UC774hnd0ParamPosition 1.mst	Braking	593.75	893.75	Accelerating	608.75	908.75	20479.554	Per 3
97	UC774hnd0ParamPosition 1.mst	Braking	600	900	Accelerating	612	912	20340.0385	Per 3
98	UC774hnd0ParamPosition 1.mst	Braking	606.25	906.25	Accelerating	615.25	915.25	20346.9598	Per 3
99	UC774hnd0ParamPosition 1.mst	Braking	612.5	912.5	Accelerating	618.5	918.5	20375.8571	Per 3
100	UC774hnd0ParamPosition 1.mst	Braking	618.75	918.75	Accelerating	621.75	921.75	20479.554	Per 3
101	UC774hnd0ParamPosition 1.mst	Braking	625	925	Accelerating	625	925	20340.0385	Per 3
102	UC774hnd0ParamPosition 1.mst	Braking	631.25	931.25	Accelerating	628.25	931.25	20346.9598	Per 3
103	UC774hnd0ParamPosition 1.mst	Braking	637.5	937.5	Accelerating	631.5	937.5	20375.8571	Per 3
104	UC774hnd0ParamPosition 1.mst	Braking	643.75	943.75	Accelerating	634.75	943.75	20479.554	Per 3
105	UC774hnd0ParamPosition 1.mst	Braking	650	950	Accelerating	638	950	20340.0385	Per 3
106	UC774hnd0ParamPosition 1.mst	Braking	656.25	956.25	Accelerating	641.25	956.25	20346.9598	Per 3
107	UC774hnd0ParamPosition 1.mst	Braking	662.5	962.5	Accelerating	644.5	962.5	20375.8571	Per 3
108	UC774hnd0ParamPosition 1.mst	Braking	668.75	968.75	Accelerating	647.75	968.75	20479.554	Per 3
109	UC774hnd0ParamPosition 1.mst	Braking	675	975	Accelerating	651	975	20340.0385	Per 3
110	UC774hnd0ParamPosition 1.mst	Braking	681.25	981.25	Accelerating	654.25	981.25	20346.9598	Per 3
111	UC774hnd0ParamPosition 1.mst	Braking	687.5	987.5	Accelerating	657.5	987.5	20375.8571	Per 3
112	UC774hnd0ParamPosition 1.mst	Braking	693.75	993.75	Accelerating	660.75	993.75	20479.554	Per 3
113	UC774hnd0ParamPosition 1.mst	Braking	700	1000	Accelerating	664	1000	20340.0385	Per 3
114	UC774hnd0ParamPosition 1.mst	Braking	706.25	1006.25	Accelerating	667.25	1006.25	20346.9598	Per 3
115	UC774hnd0ParamPosition 1.mst	Braking	712.5	1012.5	Accelerating	670.5	1012.5		

If valid basic combinations or envelopes that match the criteria described in “*Post-processing of automatically defined groups*” (page 63) are present in the model then additional results for these will be tabulated into the XLSX spreadsheet summary worksheets underneath the results for the temperature only and combined temperature and trainset rail loading results. A separate set of the peak results within these basic combinations will be highlighted in bold blue text as illustrated in the figures below for the longitudinal relative railbed displacement and longitudinal reaction results for a model that includes valid basic combinations.

Check of Longitudinal Relative Displacement of Railbed (Relative Displacement between Rails and Deck)												
Job Title: UC 774-3 Model UC774HeadP403ParamRail Analysis Filename: UC774HeadP403ParamRail-BasicCombi-Position 1--> UC774HeadP403ParamRail-BasicCombi-Position 5 Model Directory: C:\ProgramData\RailTrack\StructureInteraction Analysis Date: 28/03/2019 --> 28/03/2019 Model Units: N/mm,kg,C												
Analysis ID	Results Filename / Combination Name	Track 1		Track 2		Peak Relative Longitudinal Displacement between Rail and Deck (mm)		Track Number with Peak Displacement		Distance from Left End of Structure for Peak Displacement		Description of peak location
		Loading Type	Distance from Left End of the Model to the Starting Position of the	Distance from Left End of the Model to the Finishing Position of the	Loading Type	Distance from Left End of the Model to the Starting Position of the	Distance from Left End of the Model to the Finishing Position of the					
1	UC774HeadP403ParamRail-BasicCombi-Position 1.mys	Temperature Only			Temperature Only	270	570	0.00732054	2	325	Rail Abutment	
2	UC774HeadP403ParamRail-BasicCombi-Position 1.mys	Baking	0	300	Accelerating	351.25	651.25	0.00732054	2	325	Rail Abutment	
3	UC774HeadP403ParamRail-BasicCombi-Position 2.mys	Baking	0	300	Accelerating	351.25	651.25	0.00732054	2	325	Rail Abutment	
4	UC774HeadP403ParamRail-BasicCombi-Position 3.mys	Baking	0	300	Accelerating	351.25	651.25	0.00732054	2	325	Rail Abutment	
5	UC774HeadP403ParamRail-BasicCombi-Position 4.mys	Baking	243.75	543.75	Accelerating	513.75	813.75	0.00971488	1	294	Pier 7	
6	UC774HeadP403ParamRail-BasicCombi-Position 5.mys	Baking	325	625	Accelerating	695	995	0.00971488	2	325	Rail Abutment	
7	Basic Combination Position including Self Weight							0.00732054	2	325	Rail Abutment	
8	Basic Combination Position 2 including Self Weight							0.00732054	2	325	Rail Abutment	
9	Basic Combination Position 3 including Self Weight							0.00732054	2	325	Rail Abutment	
10	Basic Combination Position 4 including Self Weight							0.00971488	1	294	Pier 7	
11	Basic Combination Position 5 including Self Weight							0.00971488	2	325	Rail Abutment	
Warning: Basic combinations of nonlinear results are not strictly valid and should be used with caution												

Figure 85: Longitudinal Relative Railbed Displacement Check Worksheet for Rail Track Analysis Results and Basic Combinations of these Results

Check of Longitudinal Reactions												
Job Title: UC 774-3 Model UC774HeadP403ParamRail Analysis Filename: UC774HeadP403ParamRail-Position 1--> UC774HeadP403ParamRail-BasicCombi-Position 5 Model Directory: C:\ProgramData\RailTrack\StructureInteraction Analysis Date: 28/03/2019 --> 28/03/2019 Model Units: N/mm,kg,C												
Analysis ID	Results Filename / Combination Name	Track 1		Track 2		Peak Longitudinal Reaction (N)		Abutment / Pier Number / Pier Reaction				
		Loading Type	Distance from Left End of the Model to the Starting Position	Distance from Left End of the Model to the Finishing Position	Loading Type	Distance from Left End of the Model to the Starting Position	Distance from Left End of the Model to the Finishing Position					
1	UC774HeadP403ParamRail-BasicCombi-Position 1.mys	Temperature Only			Temperature Only	270	570	302463.4131	Pier 5			
2	UC774HeadP403ParamRail-BasicCombi-Position 1.mys	Baking	0	300	Accelerating	351.25	651.25	-464507.2753	Pier 3			
3	UC774HeadP403ParamRail-BasicCombi-Position 2.mys	Baking	0	300	Accelerating	351.25	651.25	-464507.2753	Pier 3			
4	UC774HeadP403ParamRail-BasicCombi-Position 3.mys	Baking	0	300	Accelerating	351.25	651.25	-464507.2753	Pier 3			
5	UC774HeadP403ParamRail-BasicCombi-Position 4.mys	Baking	243.75	543.75	Accelerating	513.75	813.75	1001842.32	Pier 8			
6	UC774HeadP403ParamRail-BasicCombi-Position 5.mys	Baking	325	625	Accelerating	695	995	-119339.888	Pier 11			
7	Basic Combination Position including Self Weight							262574.6646	Pier 5			
8	Basic Combination Position 2 including Self Weight							-643660.8864	Pier 3			
9	Basic Combination Position 3 including Self Weight							-638174.2286	Pier 3			
10	Basic Combination Position 4 including Self Weight							-1214112.788	Pier 8			
11	Basic Combination Position 5 including Self Weight							-159972.026	Pier 11			
Warning: Basic combinations of nonlinear results are not strictly valid and should be used with caution												

Figure 86: Longitudinal Reaction Check Worksheet for Rail Track Analysis Results and Basic Combinations of these Results

Performing Post-Processing without Charting

For a large Rail Track Analysis that may have included detailed modelling or possibly a greater number of tracks / Train Loading Groups / trainset positions per Train Loading Group there are some circumstances when the post-processing can be unsuccessful or the results spreadsheet can fail to load into the spreadsheet application you are using to view the XLSX spreadsheet, resulting in an error message being shown. If this occurs it may be possible to post-process the whole Rail Track Analysis by disabling the charting in the post-processing.

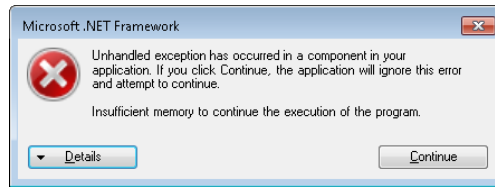


Figure 87: Insufficient Memory to Complete the Post-Processing

The post-processing provides the option to turn off all of the charting on the main dialog as highlighted in the figure that follows. When this option is turned off the output from the post-processing will be identical to the full post-processing but the only difference will be the omission of the charts in the separate worksheets for the tracks and the decks. The whole (or part – see next section) analysis can therefore be post-processed first with all of the enveloping and peak checking carried out, after which these spreadsheets can be inspected.

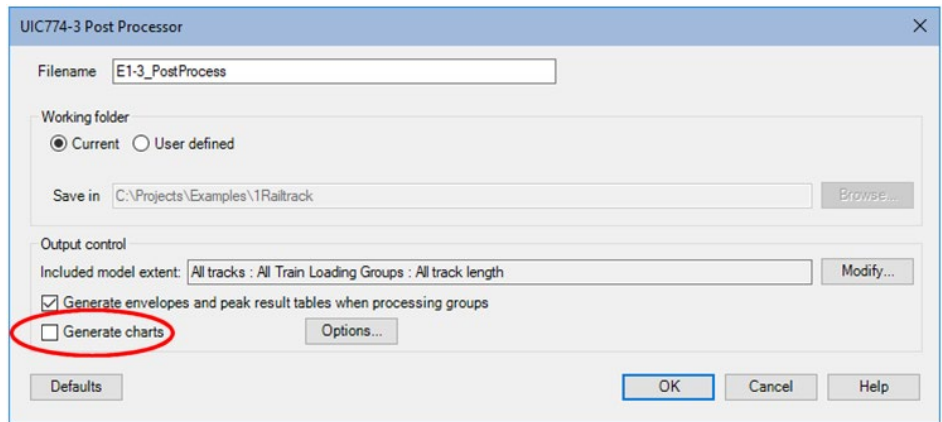


Figure 88: Disabling the Charting for the Post-Processing

Any aspects of the structure/analysis that warrant more detailed investigations can then be post-processed to separate spreadsheets with the charting turned back on but using the **Modify Included Output** dialog to target which tracks / Train Loading Groups / rail track extent and the **Chart Options** dialog to choose which charts are required – see “*Performing Post-Processing with Selective Output*” below.

Performing Post-processing with Selective Output

Targeted results output for the Rail Track Analysis can be obtained for the post-processing if a reduced set of tracks/Train Loading Groups/extent of railtrack are to be post-processed. This may be because of a need to investigate specific aspects of the track-structure interaction model more closely without all of the other effects or it could be because it was impossible to post-process the whole analysis into a single

spreadsheet (the spreadsheet was too large to write, or the application being used to view the spreadsheet was unable to load/view it).

The post-processor allows the full control of the tracks, Train Loading Groups and extent of the railtrack that are to be included in the results post-processing through the **Modify Included Output** dialog shown in the figure below (accessed by clicking on the **Modify...** button on the main post-processing dialog). In combination with the **Generate Charts** option (and the selection of which charts to create) this allows the creation of any results spreadsheets for track-structure interaction locations of interest.

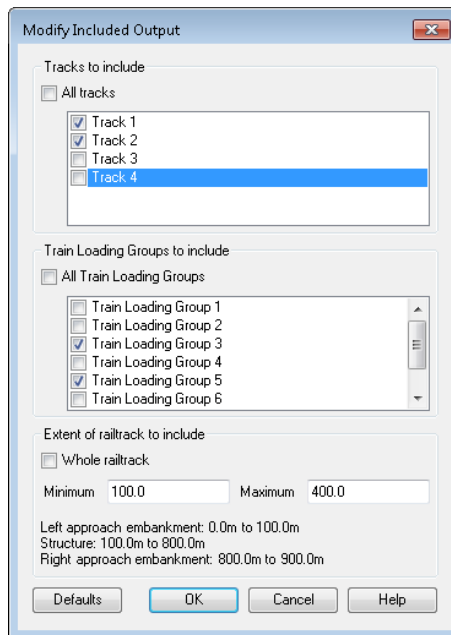


Figure 89: Modify Included Output Dialog with Selective Output for Rail Track Model with 4 Tracks, 8 Train Loading Groups and a 0.7 km Viaduct

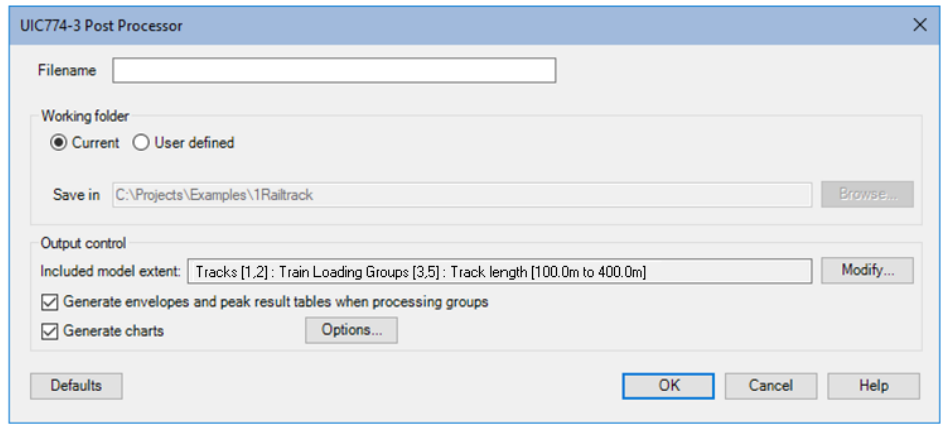


Figure 90: Associated Post-Processing Dialog Showing Selection Output for Rail Track Model with 4 Tracks, 8 Train Loading Groups and a 0.7 km Viaduct

For the viaduct being post-processed above the chosen input in the dialog will create the individual spreadsheets for the selective output as normal. These will, in addition to the data and charts, contain some warnings within the worksheets for the tracks, decks and the peak quantities as a reminder that it is possible for a more onerous result to be present for a different track / Train Loading Group or trainset position / within a different rail track extent if the selection within the current results spreadsheet has not included the worst effects.



Note. If for some reason a spreadsheet file is not produced due to insufficient memory post-processing of the whole model without charts is recommended as a first step if selected output is being used, this way the peak results for the whole analysis are obtained prior to carrying out selective post-processing.



Caution. If selective output is being used when it has not previously failed it is still recommended that the whole model (or at absolute minimum the left abutment to the right abutment) is post-processed without charts as a first step to ensure that the peak results and their locations are known prior to carrying out selective post-processing.

Figure 91 shows the results worksheet created for track 1 of the model. Clearly visible at the top of the worksheet is the following warning highlighted in red:

Warning: Only selected Train Loading Groups and track length (100.0m to 400.0m) were included in the results. Exclusion of results could lead to peak behaviours being missed and more critical conditions being excluded from the design process

The same message will also be repeated at the top of the results worksheets for track 2 and the decks along with the associated envelope worksheets if this option has been selected. The exact message reflects the choices within the **Modify Included Output** dialog.

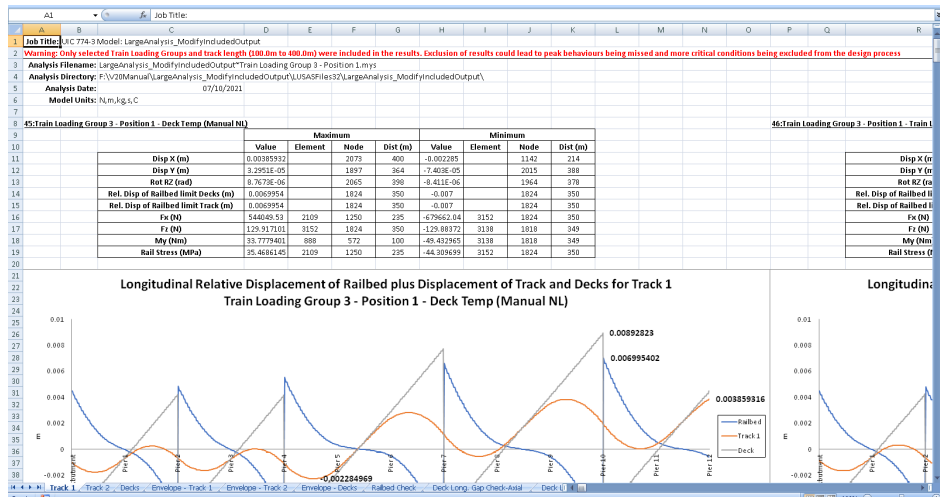


Figure 91: Selective Rail Track Extents Results for Track 1

Figure 92 to Figure 94 show the peak result table worksheet for the longitudinal relative railbed displacement. In the table only loadings applied to the tracks chosen for post-processing are output and therefore only tracks 1 and 2 are tabulated, tracks 3 and 4 have been omitted. The peak longitudinal relative railbed displacements reported in the table will also only come from tracks 1 and 2. Furthermore, only Train Loading Groups 3 and 5 were chosen for post-processing and are output in the table, Train Loading Groups 1, 2, 4 and 6 to 8 have been omitted. Finally, the selection of the rail track extent to only be from 100 m (the left-hand abutment) to 400 m means that the full length of the rail track has not been considered for the determination of the peak longitudinal relative railbed displacement which could mean that the peak value might occur outside the extent that has been chosen. As a result of the restriction of the post-processing to the limited tracks / Train Loading Groups / rail track extent the post-processor has issued the warnings underneath the table shown in Figure 94 and repeated below:

Warning: Only selected tracks were included in the enveloping and the table above. Exclusion of tracks could result in peak behaviours in tracks being missed and more critical conditions being excluded from the design process.

Warning: Only selected Train Loading Groups were included in the main results, enveloping and the table above. Exclusion of Train Loading Groups could result in peak behaviours from excluded results being missed and more critical conditions being excluded from the design process.

Warning: Only selected track length (100.0m to 400.0m) was included in the enveloping and the table above. Exclusion of track length could result in peak behaviours in tracks being missed and more critical conditions being excluded from the design process.

The same messages will also be repeated at the bottom of the peak results worksheet for axial rail stress since the choice of tracks / Train Loading Groups / rail track extent will have an identical effect on the extent of the tabular output for the axial rail stress. The exact messages reported reflect the choices within the **Modify Included Output** dialog.

Check of Longitudinal Relative Displacement of Railbed (Relative Displacement between Rails and Deck)					
Job Title: UIC 774-3 Model: LargeAnalysis_ModifyIncludedOutput Analysis Filename: LargeAnalysis_ModifyIncludedOutput*Train Loading Group 1 - Position 1 --> LargeAnalysis_ModifyIncludedOutput*Train Loading Group 8 - Position 11 Model Directory: F:\V20Manual\LargeAnalysis_ModifyIncludedOutput Analysis Date: 07/10/2021 --> 07/10/2021 Model Units: N,m,kg,s,C					
Analysis ID	Results Filename	Loading Type	Track1		Distance from the Mode Finishing Pos the Load
			Distance from Left End of the Model to the Starting Position of the Loading (m)	Distance from the Mode Finishing Pos the Load	
23	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 1.mys	Temperature Only			
23	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 1.mys	Braking	-200		
24	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 2.mys	Braking	-130		
25	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 3.mys	Braking	-60		
26	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 4.mys	Braking	10		
27	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 5.mys	Braking	80		
28	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 6.mys	Braking	150		
29	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 7.mys	Braking	220		
30	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 8.mys	Braking	290		
31	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 9.mys	Braking	360		
32	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 10.mys	Braking	430		
33	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 11.mys	Braking	500		
45	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 1.mys	Braking	-200		
46	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 2.mys	Braking	-130		
47	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 3.mys	Braking	-60		
48	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 4.mys	Braking	10		
49	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 5.mys	Braking	80		
50	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 6.mys	Braking	150		
51	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 7.mys	Braking	220		
52	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 8.mys	Braking	290		
53	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 9.mys	Braking	360		
54	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 10.mys	Braking	430		
55	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 11.mys	Braking	500		

Figure 92: Longitudinal Relative Railbed Displacement Results for Tracks 1 and 2, Train Loading Groups 3 and 5, Rail Track Extent 100m to 400m (1 of 3)

tracks 1 and 2 are tabulated, tracks 3 and 4 have been omitted. It should be noted though that tracks 3 and 4 were still included within the analysis so any loading that was applied to them would have still been included in the track-structure-interaction analysis – the information is simply not being reported here because the tracks are excluded from the post-processing.

For the post-processing only Train Loading Groups 3 and 5 were chosen for post-processing and are output in the table, Train Loading Groups 1, 2, 4 and 6 to 8 have been omitted. The restriction of the rail track extent has no effect on the calculation of the displacements between the ends of decks since these calculations do not relate to the track, any modification of the rail track extent is therefore ignored in the **Modify Included Output** dialog.

As a result of any restriction of the post-processing the post-processor has issued the following message and warning below the table:

Note: Selected tracks were included in the enveloping and only these are listed in the table above. The effects of loading on excluded tracks is still considered in the model and all results reported in this table relate to the structure only.

Warning: Only selected Train Loading Groups were included in the main results, enveloping and the table above. Exclusion of Train Loading Groups could result in peak behaviours from excluded results being missed and more critical conditions being excluded from the design process.

The same messages will also be repeated at the bottom of the peak results worksheet for all end of deck displacements and longitudinal reactions since the choice of tracks and Train Loading Groups will have an identical effect on the extent of the tabular output. The exact messages reported reflect the choices within the **Modify Included Output** dialog.

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Check of Longitudinal Relative Displacement between Ends of Decks (Total Effects)					
Job Title: UIC 774-3 Model: LargeAnalysis_ModifyIncludedOutput Analysis Filename: LargeAnalysis_ModifyIncludedOutput*Train Loading Group 1 - Position 1 --> LargeAnalysis_ModifyIncludedOutput*Train Loading Group 8 - Position 11 Model Directory: F:\V20Manual\LargeAnalysis_ModifyIncludedOutput Analysis Date: 07/10/2021 --> 07/10/2021 Model Units: N, m, kg, s, C					
Analysis ID	Results Filename	Loading Type	Track1		
			Distance from Left End of the Model to the Starting Position of the Loading (m)	Distance from the Model Finishing Pos the Loadin	
23	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 1.mys	Temperature Only			
23	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 1.mys	Braking	-200		
24	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 2.mys	Braking	-130		
25	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 3.mys	Braking	-60		
26	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 4.mys	Braking	-10		
27	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 5.mys	Braking	80		
28	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 6.mys	Braking	150		
29	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 7.mys	Braking	220		
30	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 8.mys	Braking	290		
31	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 9.mys	Braking	360		
32	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 10.mys	Braking	430		
33	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 3 - Position 11.mys	Braking	500		
45	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 1.mys	Braking	-200		
46	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 2.mys	Braking	-130		
47	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 3.mys	Braking	-60		
48	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 4.mys	Braking	-10		
49	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 5.mys	Braking	80		
50	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 6.mys	Braking	150		
51	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 7.mys	Braking	220		
52	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 8.mys	Braking	290		
53	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 9.mys	Braking	360		
54	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 10.mys	Braking	430		
55	LargeAnalysis_ModifyIncludedOutput*Train Loading Group 5 - Position 11.mys	Braking	500		

Figure 95: Longitudinal Relative Displacement between Ends of Decks (Total Effects) Results for Tracks 1 and 2, Train Loading Groups 3 and 5, Rail Track Extent 100m to 400m (1 of 3)

Distance from Left End of the Model to the Finishing Position of the Loading (m)	Loading Type	Track2		Peak Relative Longitudinal Displacement between Ends of Decks. Positive = Opening, Negative = Closing (m)	Pier Number / Location Supporting Decks with Peak Displacement
		Distance from Left End of the Model to the Starting Position of the Loading (m)	Distance from Left End of the Model to the Finishing Position of the Loading (m)		
100	Accelerating	70	370	-0.014427929	Pier 25
170	Accelerating	140	440	-0.014426145	Pier 25
240	Accelerating	210	510	-0.014582524	Pier 7
310	Accelerating	280	580	-0.015759047	Pier 10
380	Accelerating	350	650	-0.01617827	Pier 13
450	Accelerating	420	720	-0.01618732	Pier 16
520	Accelerating	490	790	-0.016075464	Pier 19
590	Accelerating	560	860	-0.016238693	Pier 19
660	Accelerating	630	930	-0.016617575	Pier 22
730	Accelerating	700	1000	-0.01717358	Pier 25
800	Accelerating	770	1070	-0.014748286	Pier 25
100	Accelerating	70	370	-0.014421211	Pier 25
170	Accelerating	140	440	-0.014426145	Pier 25
240	Accelerating	210	510	-0.014582524	Pier 7
310	Accelerating	280	580	-0.015759047	Pier 10
380	Accelerating	350	650	-0.01617827	Pier 13
450	Accelerating	420	720	-0.01618732	Pier 16
520	Accelerating	490	790	-0.016075464	Pier 19
590	Accelerating	560	860	-0.016238693	Pier 19
660	Accelerating	630	930	-0.016617575	Pier 22
730	Accelerating	700	1000	-0.01717358	Pier 25
800	Accelerating	770	1070	-0.014748286	Pier 25

Figure 96: Longitudinal Relative Displacement between Ends of Decks (Total Effects) Results for Tracks 1 and 2, Train Loading Groups 3 and 5, Rail Track Extent 100m to 400m (2 of 3)

A1	B1	C1	D1	E1	F1	G1
22	33	LargeAnalysis_ModifyIncludedOutput"Train Loading Group 3 - Position 11.mys	Braking	500	800	Accelerating
23	45	LargeAnalysis_ModifyIncludedOutput"Train Loading Group 5 - Position 1.mys	Braking	-200	100	Accelerating
24	46	LargeAnalysis_ModifyIncludedOutput"Train Loading Group 5 - Position 2.mys	Braking	-130	170	Accelerating
25	47	LargeAnalysis_ModifyIncludedOutput"Train Loading Group 5 - Position 3.mys	Braking	-60	240	Accelerating
26	48	LargeAnalysis_ModifyIncludedOutput"Train Loading Group 5 - Position 4.mys	Braking	10	310	Accelerating
27	49	LargeAnalysis_ModifyIncludedOutput"Train Loading Group 5 - Position 5.mys	Braking	80	380	Accelerating
28	50	LargeAnalysis_ModifyIncludedOutput"Train Loading Group 5 - Position 6.mys	Braking	150	450	Accelerating
29	51	LargeAnalysis_ModifyIncludedOutput"Train Loading Group 5 - Position 7.mys	Braking	220	520	Accelerating
30	52	LargeAnalysis_ModifyIncludedOutput"Train Loading Group 5 - Position 8.mys	Braking	290	590	Accelerating
31	53	LargeAnalysis_ModifyIncludedOutput"Train Loading Group 5 - Position 9.mys	Braking	360	660	Accelerating
32	54	LargeAnalysis_ModifyIncludedOutput"Train Loading Group 5 - Position 10.mys	Braking	430	730	Accelerating
33	55	LargeAnalysis_ModifyIncludedOutput"Train Loading Group 5 - Position 11.mys	Braking	500	800	Accelerating
34						
35	Note: Selected tracks were included in the enveloping in Microsoft Excel and only these are listed in the table above. The effects of loading on excluded tracks is still considered in the model and all results reported in this table relate to the					
36	Warning: Only selected Train Loading Groups were included in the main results, enveloping and the table above. Exclusion of Train Loading Groups could result in peak behaviours from excluded results being missed and more critical conditi					
37						
38						
39						
40						
41						
42						
43						
44						
45						
46						
47						
48						
49						
50	Envelope - Decks	Halbed Check	Deck Long, Gap Check-Aval	Deck Long, Gap Check-End Rot	Deck Long, Gap Check-Total	Deck Vert

Figure 97: Longitudinal Relative Displacement between Ends of Decks (Total Effects) Results for Tracks 1 and 2, Train Loading Groups 3 and 5, Rail Track Extent 100m to 400m (3 of 3)

Post-processing of Selected Track / Rail Nodes

If spot checks need to be performed at specific locations on the tracks, the nodes of the track/rail can be post-processed individually. To perform the post-processing the selection in the LUSAS model created by the Rail Track Analysis spreadsheet must contain nodes that are part of the track/rail. If nodes from other parts of the model are selected, then these nodes will be ignored. All other selected objects will also be ignored.

Figure 98 shows sample output from the post-processing of a track. For each results file that is loaded the axial stress at the node(s) will be reported in a separate worksheet for each node.

Check of Axial Rail Stress for Track 1, Node 1031 X=32.0 Y=0.0 Z=0.0

Job Title: UIC 774-3 Model: UIC774washIP408ParamRail
 Analysis Filename: UIC774washIP408ParamRailPosition 1 -- UIC774washIP408ParamRailPosition 5
 Model Directory: C:\Project\U1250A\TrackStruct\user\interation
 Analysis Date: 21.03.19 -- 21.03.19
 Model Units: N/mm,kg,C

Analysis ID	Results Filename	Track 1		Track 2		Axial Stress of Rail for Track 1, Node 1031 (MPa)
		Loading Type	Distance from Left End of the Model to the Starting Position of the Loading (m)	Loading Type	Distance from Left End of the Model to the Starting Position of the Loading (m)	
1	UIC774washIP408ParamRailPosition 1.mys	Temperature Only	0	Temperature Only	270	15.49229434
2	UIC774washIP408ParamRailPosition 2.mys	Braking	81.25	300 Accelerating	551.25	14.97852621
3	UIC774washIP408ParamRailPosition 3.mys	Braking	161.25	402.5 Accelerating	651.25	16.18967722
4	UIC774washIP408ParamRailPosition 4.mys	Braking	241.75	543.75 Accelerating	792.5	16.51954639
5	UIC774washIP408ParamRailPosition 5.mys	Braking	325	625 Accelerating	895	16.61346017

Figure 98: Sample Output from an Individual Track/Rail Node



Note. The stresses reported in the track/rail node worksheets are the averaged nodal stresses. The stresses reported previously in the post-processing performed on the UIC774-3 groups are the unaveraged nodal stresses and therefore the values will differ slightly. The averaged nodal stresses can be obtained for the post-processing of the UIC77-3 groups by averaging the values reported for the elements either side of the node.

Post-processing of Selected Lines if Groups are Missing

If the model does not contain the expected rail track model group names (“Track 1”, “Track 2”, etc and “Decks”) or expected group contents then post-processing can be carried out on a line by line basis. To use this option the selection must contain lines that have 3D Thick Beam elements assigned. All other lines and objects will be ignored by the post-processor.

When post-processing selected lines it is assumed that these lines define a single path which travels in the direction of increasing line ID number. The lines will therefore be post-processed in increasing line ID order and the lowest line ID start point will be assumed to provide the reference position for the x-coordinate used to calculate the distances reported.

The output is almost identical to the output that is generated for the decks group with a summary table and tabulated output reported for all of the elements associated with the lines that have been selected. No graphs are generated for the post-processing of the selected lines since the distances may not be sequential if lines of the tracks / rails or decks have been omitted from the selection as illustrated in Figure 99 where there is a jump between distances of 10 and 32 m. Results are output for the temperature only (Increment 1) and the combined temperature and trainset loading (Increment 2) with

additional results files tabulated from left to right in the worksheet. If basic combinations or envelopes have been defined in the LUSAS model the results from these will also be output to the worksheet if they can be post-processed.

Job Title:																																																																																																															
Job Title: UIC 774-3 Model: UIC774-washiP403bParamRail																																																																																																															
Analysis Filename: UIC774-washiP403bParamRail_Selection*Position.1.mys																																																																																																															
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Analysis Date: 21/03/2019																																																																																																															
Model Units: N,m,kg,s,C																																																																																																															
1:Position 1 - Deck Temp (Manual NL)												2:Position 1 - Train Loads																																																																																																			
<table><thead><tr><th colspan="2"></th><th colspan="4">Maximum</th><th colspan="4">Minimum</th><th colspan="2"></th></tr><tr><th></th><th></th><th>Value</th><th>Element</th><th>Node</th><th>Dist (m)</th><th>Value</th><th>Element</th><th>Node</th><th>Dist (m)</th><th></th><th></th></tr></thead><tbody><tr><td>Disp X (m)</td><td>0.00967877</td><td>1913</td><td>325</td><td>-0.0060961</td><td>1290</td><td>100</td><td></td><td></td><td></td><td>Disp X (m)</td><td></td></tr><tr><td>Disp Y (m)</td><td>2.0418E-05</td><td>1873</td><td>311</td><td>-4.158E-05</td><td>1882</td><td>388</td><td></td><td></td><td></td><td>Disp Y (m)</td><td></td></tr><tr><td>Rot RZ (rad)</td><td>4.9038E-06</td><td>1241</td><td>935</td><td>0</td><td>-2501146.1</td><td>2684</td><td>1801</td><td>287</td><td></td><td>Rot RZ (rad)</td><td></td></tr><tr><td>Fx (N)</td><td>-40000.004</td><td>1241</td><td>935</td><td>0</td><td>-2501146.1</td><td>2684</td><td>1801</td><td>287</td><td></td><td>Fx (N)</td><td></td></tr><tr><td>Fy (N)</td><td>80060.2031</td><td>2504</td><td>1692</td><td>251</td><td>-88672.923</td><td>2866</td><td>1909</td><td>323</td><td></td><td>Fy (N)</td><td></td></tr><tr><td>My (Nm)</td><td>416626.112</td><td>1976</td><td>1311</td><td>125</td><td>-252976.33</td><td>2684</td><td>1801</td><td>287</td><td></td><td>My (Nm)</td><td></td></tr></tbody></table>														Maximum				Minimum								Value	Element	Node	Dist (m)	Value	Element	Node	Dist (m)			Disp X (m)	0.00967877	1913	325	-0.0060961	1290	100				Disp X (m)		Disp Y (m)	2.0418E-05	1873	311	-4.158E-05	1882	388				Disp Y (m)		Rot RZ (rad)	4.9038E-06	1241	935	0	-2501146.1	2684	1801	287		Rot RZ (rad)		Fx (N)	-40000.004	1241	935	0	-2501146.1	2684	1801	287		Fx (N)		Fy (N)	80060.2031	2504	1692	251	-88672.923	2866	1909	323		Fy (N)		My (Nm)	416626.112	1976	1311	125	-252976.33	2684	1801	287		My (Nm)					
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28	1263	951	5	5	0	-0.0043383	-1.263E-05	-2.319E-06	-360000.03	63932.7843	-42691.145	1263	951																																																																																																		
29	1267	951	5	5	0	-0.0043383	-1.263E-05	-2.319E-06	-440000.03	63932.8089	-52198.353	1267	951																																																																																																		
30	1267	952	6	6	0	-0.0041396	-1.487E-05	-2.186E-06	-440000.03	63932.8089	-52198.353	1267	952																																																																																																		
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32	1273	957	7	7	0	-0.0039412	-1.695E-05	-2.011E-06	-520000.04	63932.8097	-61705.548	1273	957																																																																																																		
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34	1276	958	8	8	0	-0.0037431	-1.895E-05	-1.816E-06	-600000.04	63932.8092	-71212.742	1276	958																																																																																																		
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38	1288	964	10	10	0	-0.0033475	-2.197E-05	-1.326E-06	-760000.05	63932.8093	-90227.129	1288	964																																																																																																		
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40	1293	969	11	11	0	-0.0031501	-2.314E-05	-1.044E-06	-840000.05	63932.8093	-99734.322	1293	969																																																																																																		
41	1296	969	11	11	0	-0.0031501	-2.314E-05	-1.044E-06	-920000.05	63932.8093	-109241.51	1296	969																																																																																																		
42	1296	972	12	12	0	-0.002953	-2.401E-05	-7.353E-07	-920000.05	63932.8093	-109241.51	1296	972																																																																																																		

| Selection Envelope-Selection | | | | | | | | | | | | | | | |

Figure 99: Sample Output from Post-Processing of Selected Lines when the Groups are Missing or Invalid

If more than one results file is loaded, basic combinations are defined in the model that may be post-processed (see the restrictions under the **Post-processing of automatically defined groups** section on page 63) and enveloping has been selected then the spreadsheet will contain an additional worksheet that holds these enveloping results. The envelopes generated will be the same as those for the tracks and decks:

- ☐ Maximum and minimum envelopes for temperature loading only
- ☐ Maximum and minimum envelopes for temperature and trainset rail loading
- ☐ Maximum and minimum envelopes for all of the basic combinations defined in the model (if valid basic combinations are present)
- ☐ Maximum and minimum envelopes for all configurations (an envelope of the above results)

The following figure illustrates the tabulated enveloped results when selected lines are post-processed if expected model groups are either missing or invalid. No automatic graphing is possible when post-processing with enveloping is carried out on selected lines (since these lines may not be continuous). Should graphs of the results be required

Limitations of Use

- ❑ Since the analysis is two-dimensional (even though three-dimensional elements are used) the offsets are not modelled for the bearing/section centrelines nor for the section/rail centrelines (see figure below). Currently all track centrelines are coincident with the centreline of the deck.
- ❑ Curved bridges cannot be modelled.

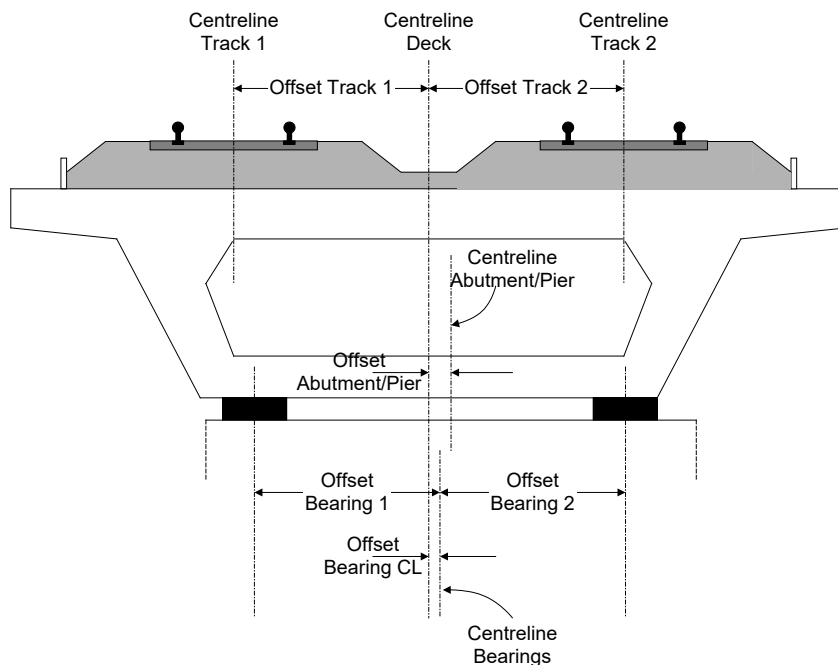


Figure 101: Offsets of Tracks/Bearings/Piers from Centreline Of Deck

References

- B1 BS EN 1991-2:2003 Eurocode 1: Actions on structures - Part 2: Traffic loads on bridges
- U1 UIC Code 774-3, Track/bridge Interaction. Recommendations for calculations. 2nd Edition, (October 2001)

Appendix A:

Verification Testing

Introduction

This appendix includes some background to the calculation of the UIC774-3 track/bridge interaction analyses in LUSAS. It explains why results from running a LUSAS nonlinear analysis that considers all thermal and train effects for the test cases in question in one analysis does not over-predict the rail stresses occurring under the combined thermal and rail loading - unlike results from simplified hand calculations or from results from other finite element analysis software systems where thermal and train effects are carried out by running separate nonlinear analyses.

From the verification testing carried out we can say that...

Even though a computer program may be validated against the standard test cases in the UIC774-3 code of practice, in situations when combined thermal and train loading from separate analyses gives track-structure interaction forces that exceed the stated yield resistance of the track-restraint system (i.e. the ballast) then the separate analysis method will potentially overpredict the rail stresses unless the loaded track yield surface is reduced by the mobilised track resistance over the extent of the train loading. Rail stress over-predictions of up to 30% have been seen when thermal and train loading results are combined from separate analyses.

Description

The rail track analysis (UIC774-3) option in LUSAS allows the construction and solution of finite element models to study the interaction between the rail track and a bridge. This forms an essential part of the design process as the stresses within the rails of the tracks must remain within specified limits based upon the design and the state of maintenance. A number of calculation methods are available and each of these can lead to a slightly different solution for the combined thermal and rail loading condition. Each of these methods (except the hand calculation) has been investigated in this technical note prior to carrying out the analysis in LUSAS using the rail track analysis option. In all tests 1.0 m element sizes have been used.

The Hwashil Viaduct, a railway bridge in South Korea, has been used for this testing with continuous welded rail (CWR) and thermal effects only present in the structure for the following analyses:

- ☐ **Combination of Separate Thermal And Rail Loading**
- ☐ **Analysis Of Combined Thermal And Rail Loading (One Step)**
- ☐ **Analysis Of Combined Thermal And Rail Loading Taking Account Of Effects Of Material Change Under Rail Loading**

In addition, two of the UIC standard test cases have also been reinvestigated to demonstrate that these results can be matched even if the analysis type is potentially invalid prior to providing guidance and conclusions on this type of analysis. These analyses were:

- ☐ **Revisit Of UIC774-3 Test E1-3 Using The Separate And LUSAS Methods Of Analysis**
- ☐ **Revisit Of UIC774-3 Test H1-3 Using The Separate And LUSAS Methods Of Analysis**

Combination of Separate Thermal and Rail Loading

In this form of analysis two or more separate analyses are carried out with each analysis considering a different loading regime to the structure. This is the simplest form of analysis of the track/bridge interaction as it assumes that superposition is valid for a nonlinear system and, according to the UIC774-3 code of practice, can generally overestimate the rail stresses with percentage errors up to 20 to 30% be it through hand calculation or computer methods.

This analysis procedure is replicated in LUSAS by performing two separate nonlinear analyses. The first considers only the thermal effects and uses the unloaded resistance bilinear curve for modelling the interaction between the track and bridge. The results of this analysis are identical for the two tracks in the model and so only the results for the first track are presented in the following figure.

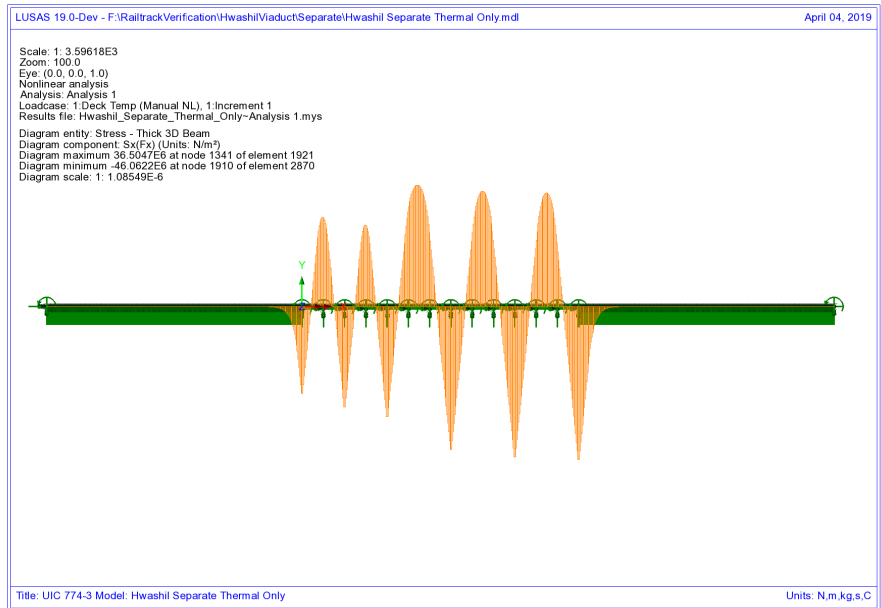


Figure 102: Axial Stress In Rails Due To Thermal Effects Only

These thermal effects give a peak compressive rail stress of 46.06 N/mm^2 . Having carried out the thermal analysis the rail loading will be considered in a separate analysis (both horizontal and vertical loading) for the ‘worst’ conditions. This rail load analysis is again a nonlinear analysis but it has no knowledge of the history from the thermal effects and therefore assumes a zero strain initial state prior to the application of the load. In addition to this unstrained condition, the loaded resistance bilinear curve is used underneath the locations of the rail loading while the unloaded lengths of track use the unloaded resistance bilinear curve. The results from the rail loading analyses are presented in the following two figures, the first being the track that has the braking train loading and the second being the track that has the accelerating train loading.

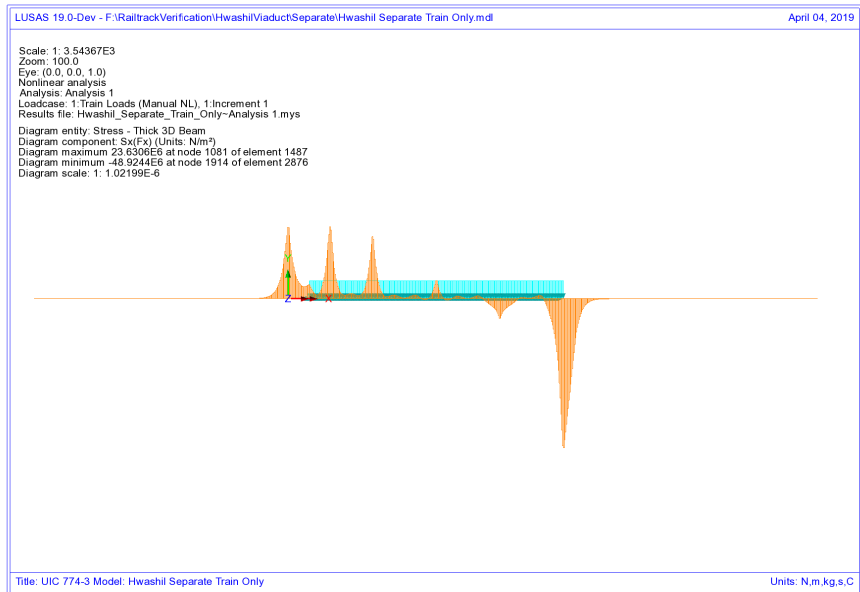


Figure 103: Axial Stress In Rails Due To Braking Train Loads On Track 1

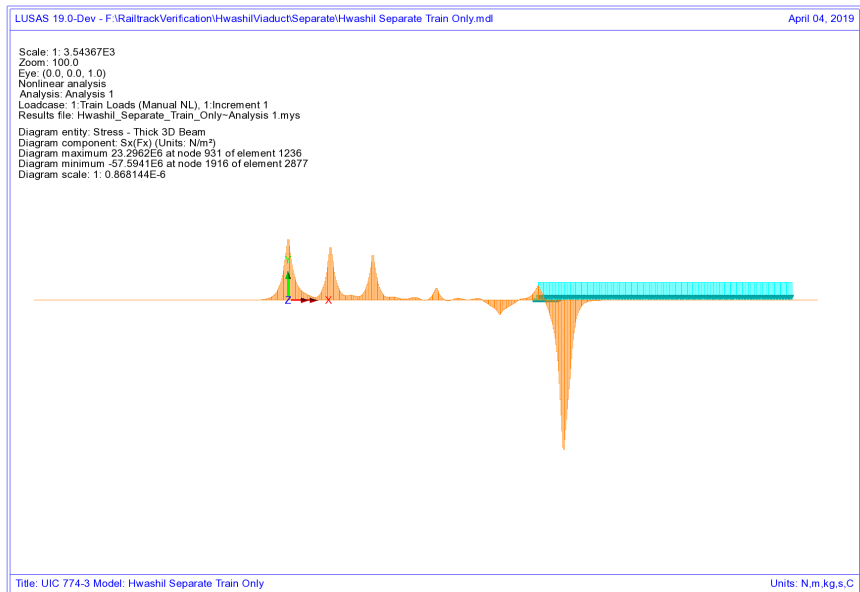


Figure 104: Axial Stress In Rails Due To Accelerating Train Loads On Track 2

From these results the peak compressive rail stresses for the two tracks are as follows:

Track 1:	48.92 N/mm²
Track 2:	57.59 N/mm²

A basic combination of the loading can be defined to add the results from the thermal and rail loading analyses together which gives the following track peak compressive stresses (see following figures):

Track 1:	94.99 N/mm²
Track 2:	103.66 N/mm²

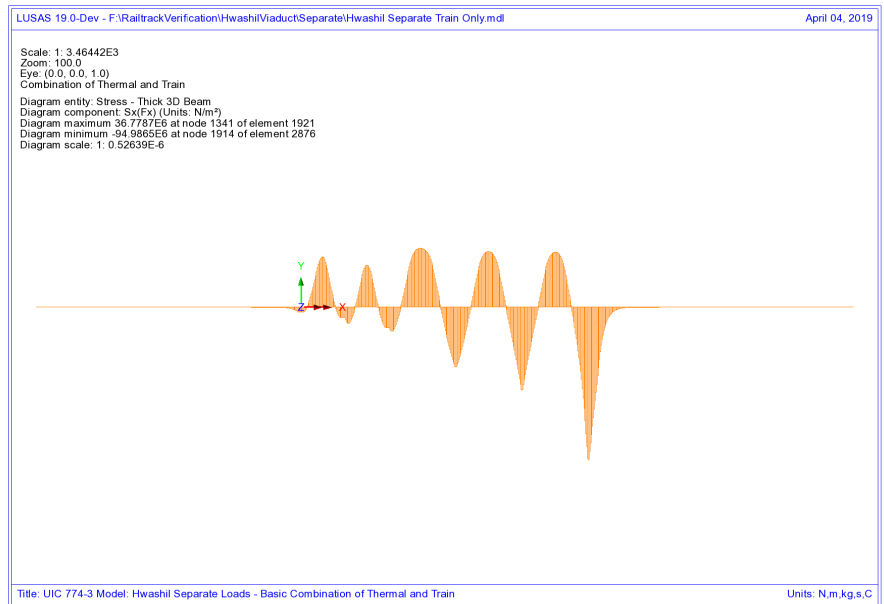


Figure 105: Axial Stress In Rails Due To Combined Thermal And Train Loads In Track 1

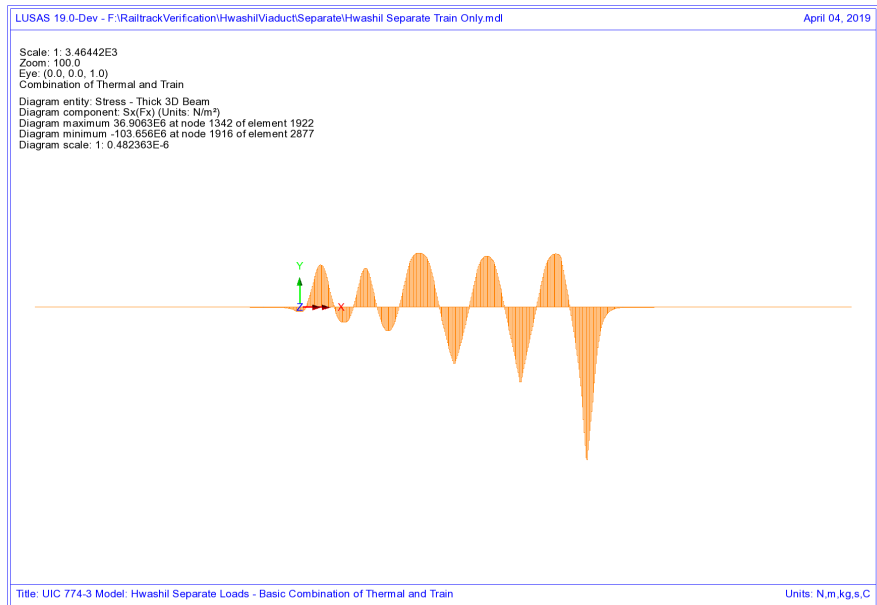


Figure 106: Axial Stress In Rails Due To Combined Thermal And Train Loads In Track 2

Inspection of the two plots shows that there is a reduction in the axial rail stresses over the first two deck transition piers towards the left end of the structure for track 1 only (subjected to the braking train). The following figures show zoomed plots of the rail axial stress for this location with the thermal diagram showing identical values either side of these piers for all of the decks in the model. The reason for the reduction in the axial stress becomes clear from the axial stress diagram for the train braking load alone, Figure 108, where the axial stress has a positive peak over the deck transition piers which is not symmetrical. Looking at the transition from the first deck to the second (2nd pier from left abutment) the axial stress in the rail over the end of the first deck is equal to a tensile stress of 23.63 N/mm² while the axial stress over the start of the second deck is equal to a tensile stress of 22.47 N/mm². Like for like comparison of the elements a certain distance from the pier for each deck shows that the second deck is consistently lower and this difference has caused the non-symmetric nature of the combined axial rail stress diagram over the deck transition piers when the axial rail stresses from the train loading are combined with the axial rail stresses from the thermal loading.

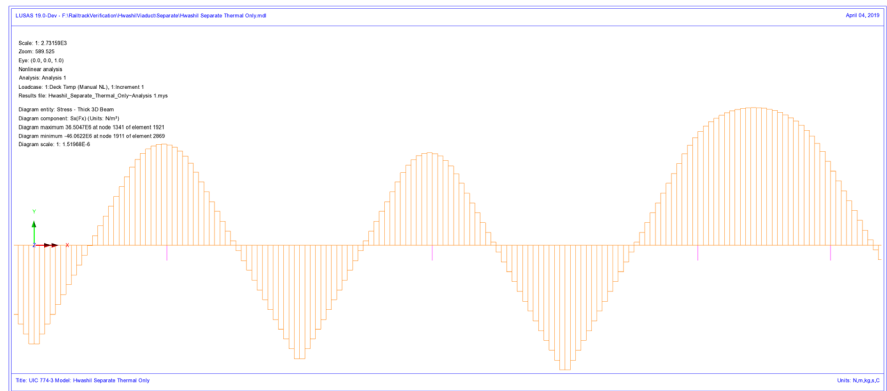


Figure 107: Zoomed Axial Stress In Rails Due To Thermal Effects Only

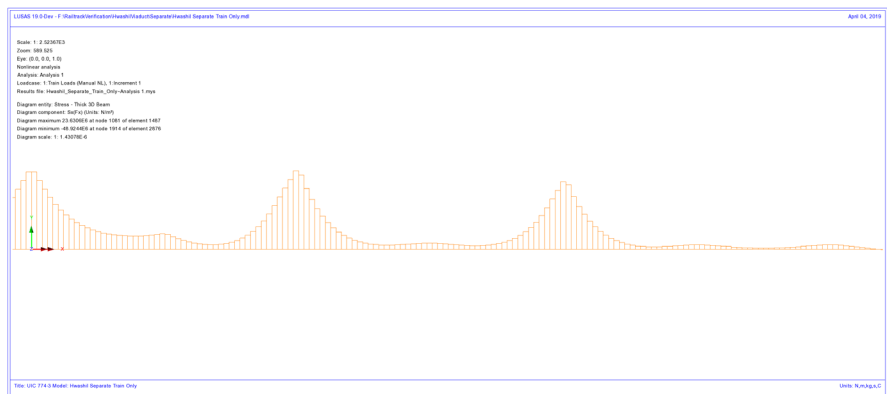


Figure 108: Zoomed Axial Stress In Rails Due To Braking Train Loads On Track 1

NOTE: When viewing this axial force diagram it should be recognised that while the first two decks (2*25m each) have identical geometry and pier/bearing properties, the first span segment of the first deck does not carry any of the braking train load and this is contributing to the difference in the behaviours observed over the piers.

Looking at the yield in the track/bridge interaction for this track, Figure 109, the reason for the differences in axial stress either side of the pier becomes clear as yielding has occurred to the left but not to the right of the deck transition pier for these first two decks.

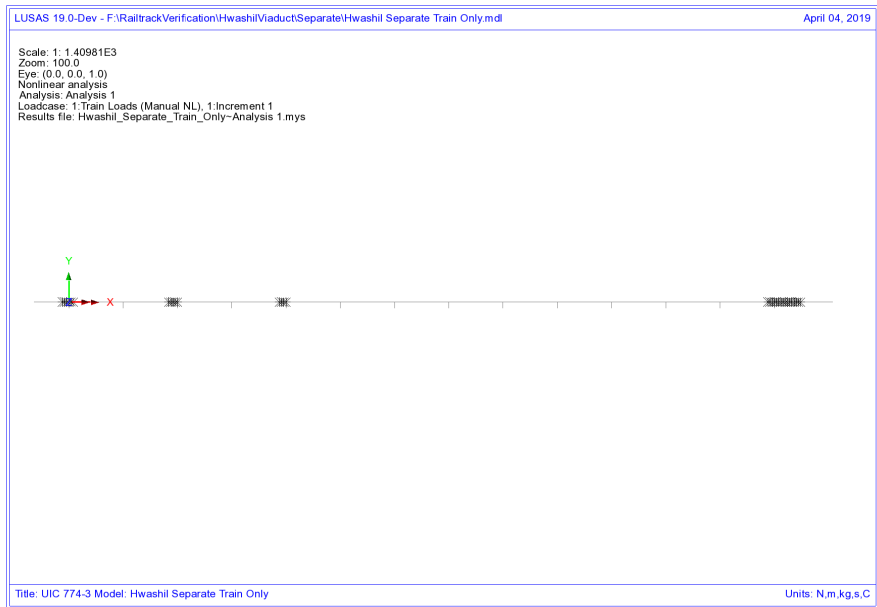


Figure 109: Yield In Track/Bridge Interaction Due To Train Braking Load On Track 1

2

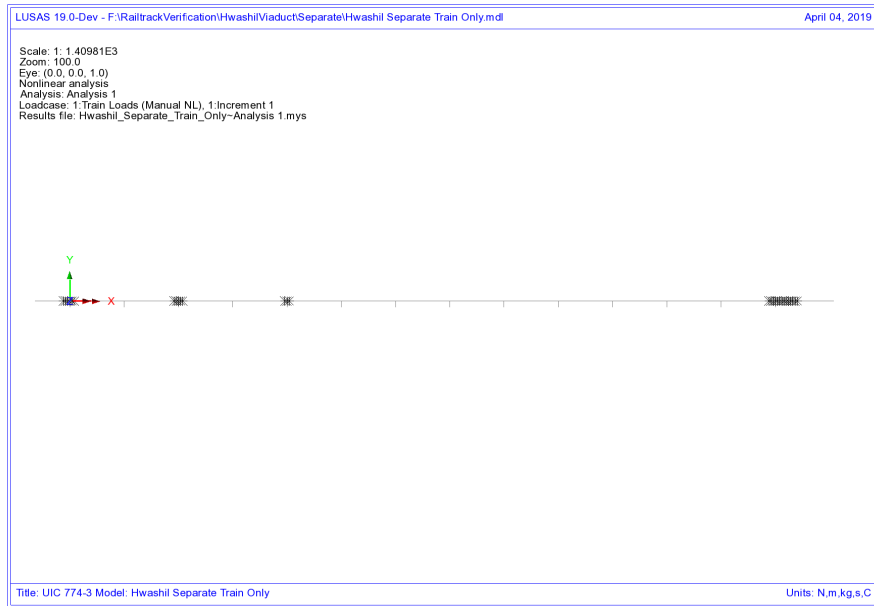


Figure 111: Yield In Track/Bridge Interaction Due To Train Acceleration Load On Track 2

Analysis of Combined Thermal and Rail Loading (One Step)

In this form of analysis a single nonlinear analysis is carried out where the thermal and rail loading are applied concurrently to the model. In terms of the track/bridge interaction, the resistance bilinear curves used in the modelling are determined by the positioning of the rail loading so that loaded properties are used where the rail loading is applied and unloaded properties everywhere else. As with the separate method highlighted above, this analysis ignores any initial straining of the track/bridge interaction under pure thermal loading and therefore assumes that the loaded resistance properties are active under the thermal loading over the extent of the train loading.

The results from the analysis are shown in the following figures and give the following results for the track peak compressive stresses:

Track 1:	85.61 N/mm²
Track 2:	100.61 N/mm²

NOTE: For this analysis the reduction in axial rail stress is not observed at the span discontinuities towards the left end of the structure.

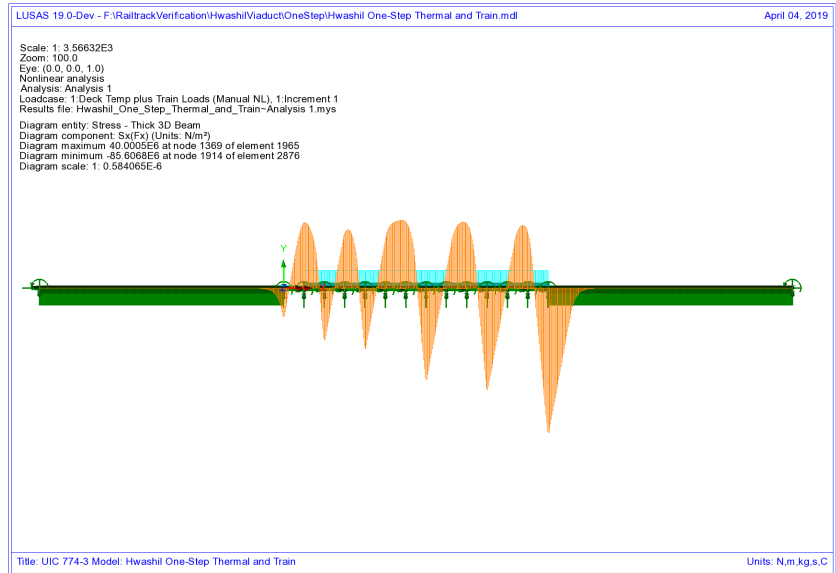


Figure 112: Axial Stress In Rails Due To Combined Thermal And Train Loads In Track 1 (One Step)

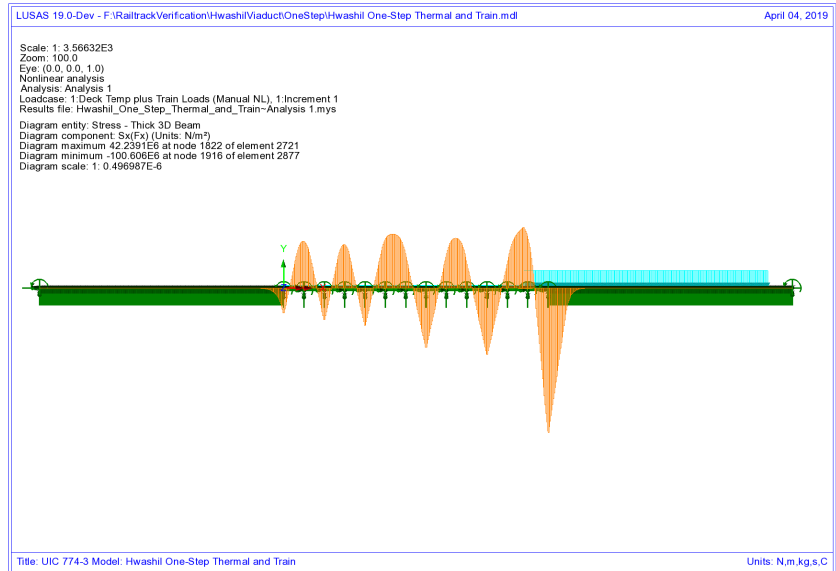


Figure 113: Axial Force In Rails Due To Combined Thermal And Train Loads In Track 2 (One Step)

Analysis of Combined Thermal and Rail Loading Taking Account of Effects of Material Change Under Rail Loading

The previous two analysis methods fail to take account of the train rail loading being applied to the rail when it has already undergone movement/stresses due to thermal effects alone. In this current form of analysis (implemented into LUSAS) the initial thermal effects are considered prior to the application of the train rail loading and the behaviour under this rail loading takes account of this history.

To illustrate the analysis, consider the following:

When the train is not on the track the stresses in the rails are governed purely by the thermal effects. For the Hwashil Viaduct the thermal effects due to the bridge only are considered and therefore the action of this causes the structure to move thus inducing relative movement between the track and the bridge and therefore an associated stress in the rail. For this condition the unloaded resistance properties apply across the whole extent of the track

As the train load arrives over a particular part of the bridge the initial relative movement of the track/bridge from the thermal effects remains and therefore the application of the train load changes the resistance state from unloaded to loaded without the loss of this initial rail stress caused by the relative movement

The train load causes increased slip of the interaction based on the loaded resistance with the end of the force-displacement curve for the unloaded resistance used as the starting point for the loaded resistance

If it was modelled, the departure of the train load would change the resistance state back to unloaded

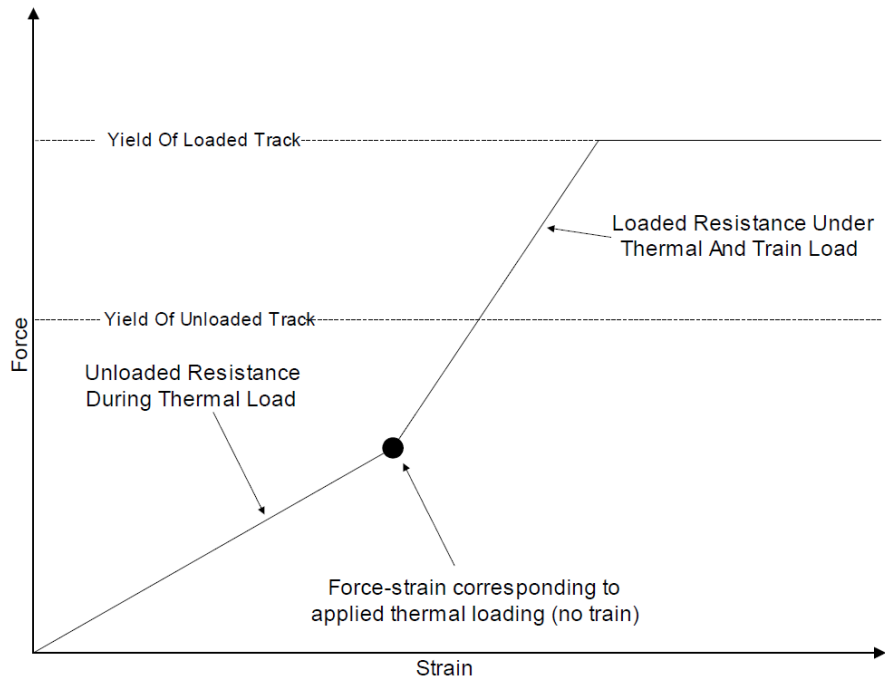


Figure 114: Representation of Transition From Unloaded To Loaded In LUSAS

The key is that the interaction resistance switches from unloaded to loaded the moment the rail load arrives thereby ‘locking in’ any initial movement that has occurred under the thermal loading until that rail load departs. The results from this form of analysis are shown in the following figures which give peak compressive rail stresses of:

Track 1 and 2 (Thermal Only):	46.06 N/mm²
Track 1 (Thermal and Train):	79.06 N/mm²
Track 2 (Thermal and Train):	92.60 N/mm²

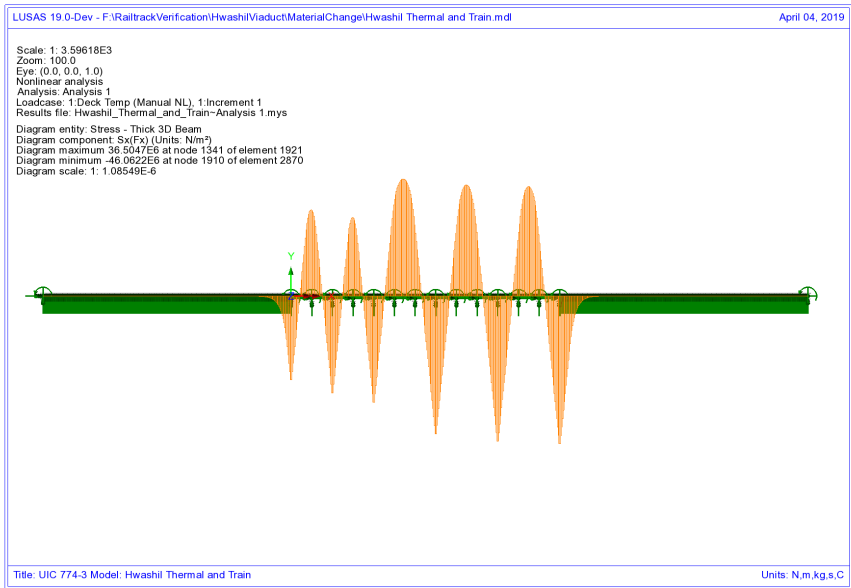


Figure 115: Axial Stress In Rails Due To Thermal Only

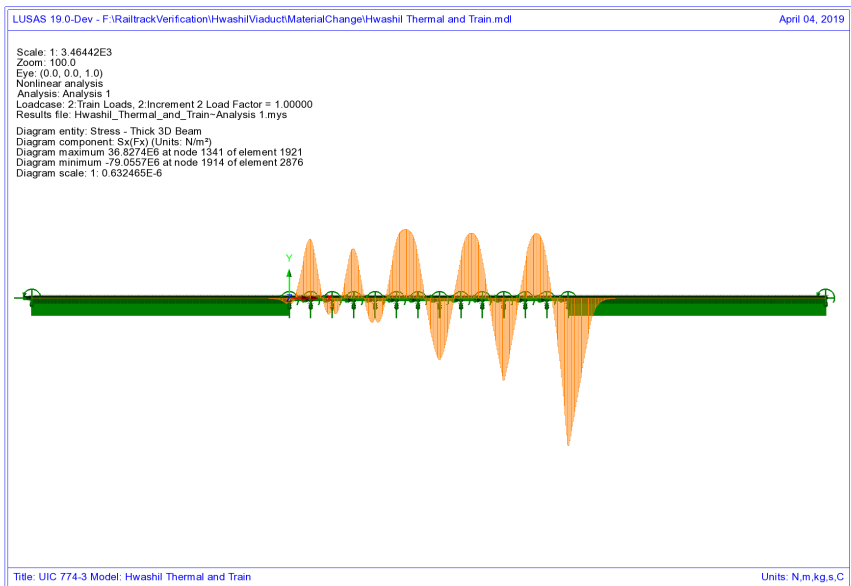


Figure 116: Axial Stress In Rails Due To Combined Thermal And Train Loads In Track 1

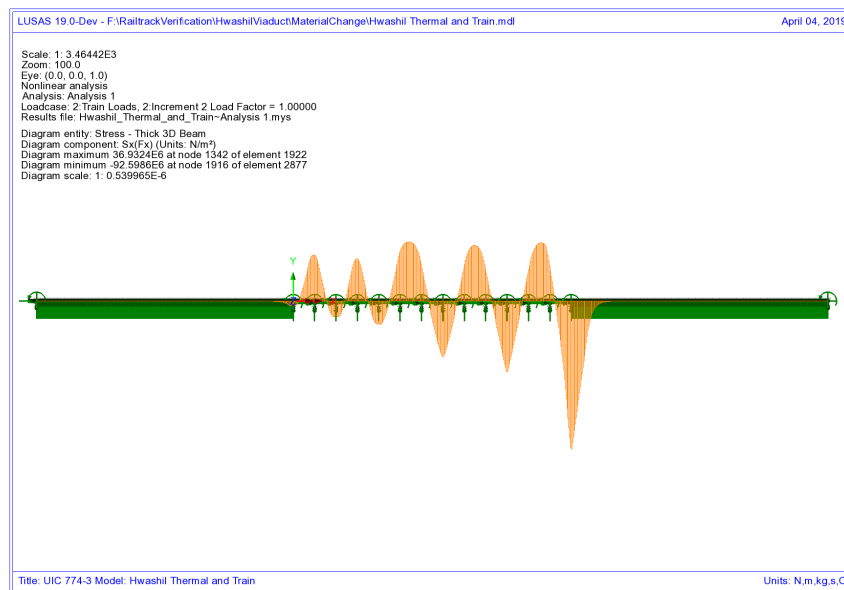


Figure 117: Axial Stress In Rails Due To Combined Thermal And Train Loads In Track 2

The analyses produced using this method can give a lower peak compressive stress in the rails than observed using the other approaches but agrees closely with the published test cases using rigorous methods in UIC774-3 as observed in the following sections for test E1-3 and H1-3.

Discussion

The peak compressive stresses in track/rail 2 which has the accelerating load and track/rail 1 that is subjected to the braking train show differences in the peak compressive stress in the rails based on the position of the train loads used in the analysis. As the loading and geometry of the models are identical the differences can only be associated with the track resistance modelling/behaviour. It has been noted previously above that the transition from unloaded resistance to loaded resistance is only incorporated into the LUSAS modelling so this track resistance is investigated by looking at the yield under the effects of the rail loading.

Looking first at the second track/rail that has the accelerating load, the yielding occurring from the three analyses are shown in the following figures. Comparing the yield layout for the LUSAS analysis (Figure 121) and the concurrent thermal/train loading analysis (Figure 120) shows that the amount of yielding of the interaction joints (ballast) at the right-hand abutment is similar but the yielding diminishes away from the accelerating locomotive at the front of the train which has only just entered the

structure at the right-hand abutment in the LUSAS analysis whereas in the concurrent loading analysis it is predicting large regions of yielded interaction joints. In the LUSAS analysis yielding may have previously occurred of unloaded material under thermal only loading but relieving of the forces in the unloaded interaction joints away from the accelerating train has caused them to return to elastic behaviour with a permanent deformation, hence the absence of indicated active yield flags.

Looking now at the separate analysis, the yield layout for the concurrent thermal/train analysis is comparable to the yield layout for the thermal effects alone (Figure 118). In the separate train loading analysis very little yielding is indicated as being associated with the accelerating train loading analysis (Figure 119). This is due to the accelerating train only just entering the bridge with the majority of the loads over the right approach embankment, which are vertical not horizontal. The potential relieving effects of the train loading in this analysis are combined through a basic combination (unlike in the LUSAS material change method) but for this separate analysis the yield strength of both the unloaded and loaded materials are both counted so if both analyses yield at the same position (as is the case at the right-hand abutment and elsewhere) then it is possible that the interaction joints / ballast could be considered too strong – see below.

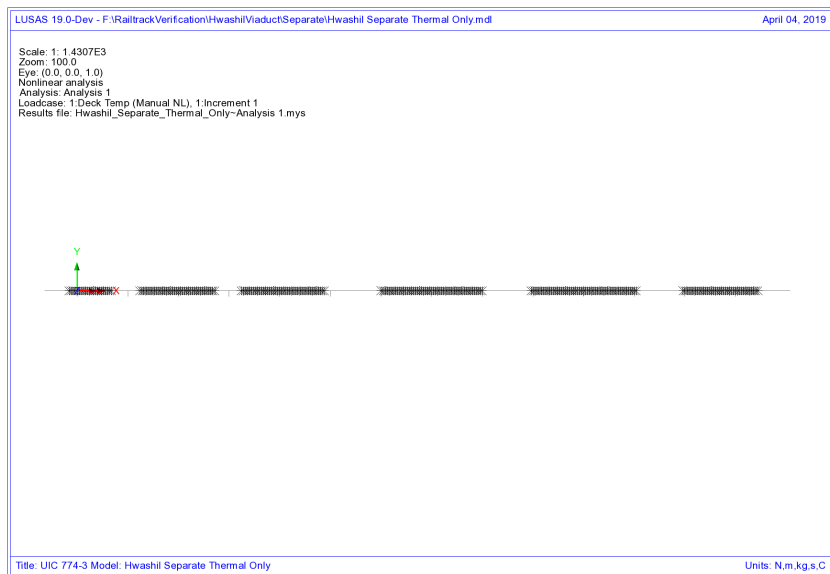


Figure 118: Track/Rail 2 Yield Due To Thermal Load On Track Alone

Analysis of Combined Thermal and Rail Loading Taking Account of Effects of Material Change Under Rail Loading

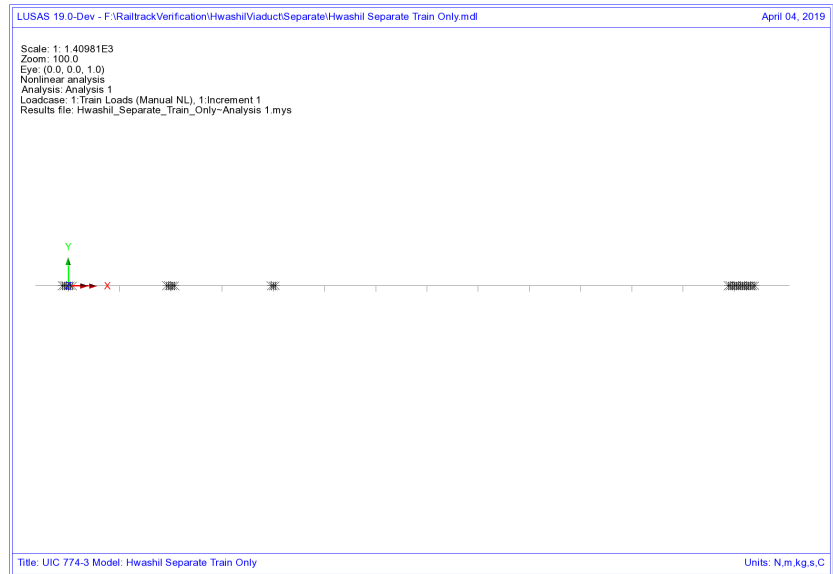


Figure 119: Track/Rail 2 Yield Due To Accelerating Train Loads On Track 2 – Separate Analysis

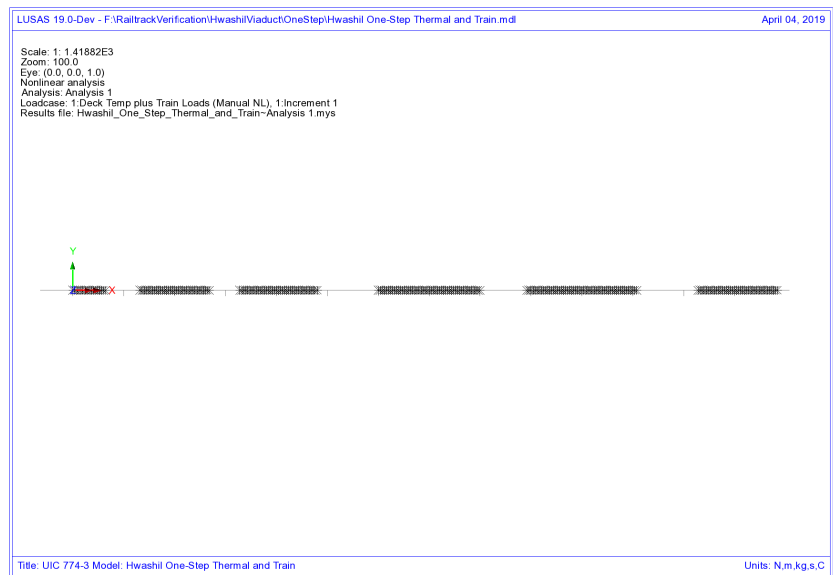


Figure 120: Track/Rail 2 Yield Due To Accelerating Train Loads On Track 2 - Thermal And Rail Applied Concurrently

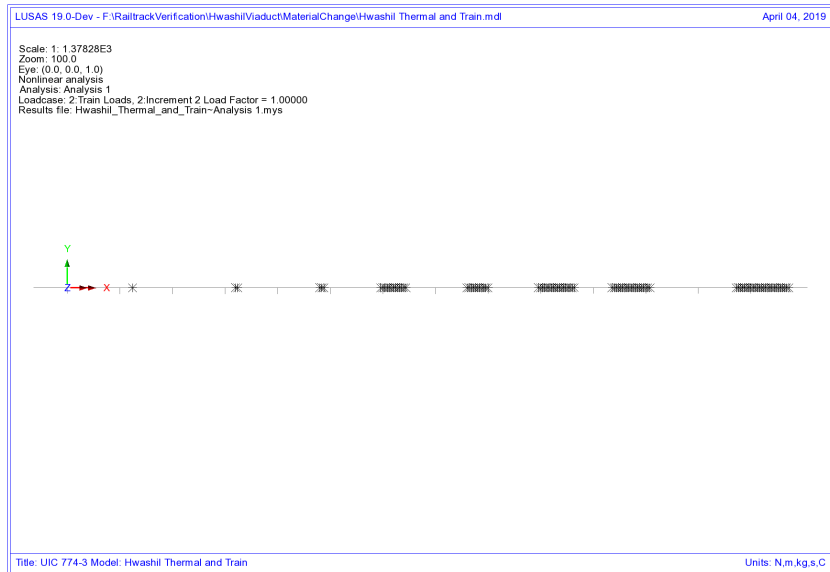


Figure 121: Track/Rail 2 Yield Due To Accelerating Train Load On Track 2 - LUSAS Combined Analysis

Looking at what is effectively happening in these analyses, Figure 122, the concurrent loading analysis uses the loaded resistance throughout the analysis and follows the loaded stiffness curve from the origin and potentially gives the location indicated on the plastic part of this curve as illustrated with a force in the interaction limited to the resistance of the loaded track. For the separate analysis, the thermal effects use the unloaded curve and the behaviour of this part of the analysis is limited by the resistance of the unloaded track. Under these conditions the analysis may give a location indicated by the 'Thermal Alone' point on the unloaded curve. Separate consideration of the train loading effectively places the origin of the loaded bilinear curve at this 'Thermal Alone' position and any loading could potentially give the location indicated by the 'Separate Train Load Added To Thermal' position. This could give an apparent increase in the resistance of the track and therefore increase rail stresses in the loaded track.

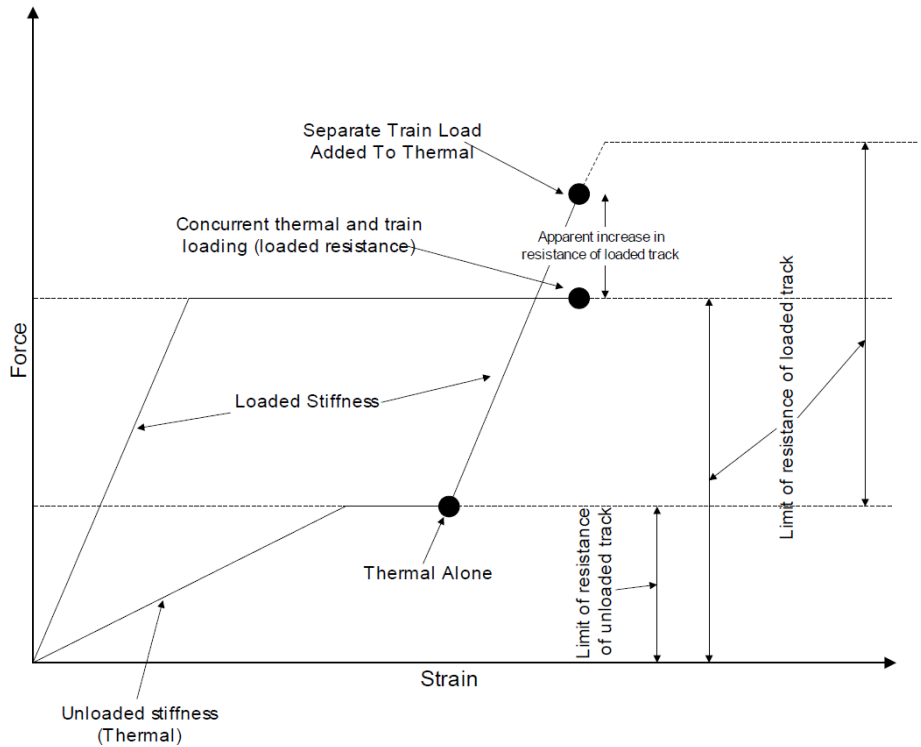


Figure 122: Illustration Of Behaviour Of Separate Analysis Vs. Concurrent Thermal And Rail Loading

Similar comparisons can be made between the separate analysis and the LUSAS analysis - Figure 123. While both of these effectively use the 'Thermal Alone' location as an origin for the loaded resistance curve, the key difference between the two approaches is that the LUSAS analysis enforces the track resistance at which plasticity occurs instead of allowing the potential for an apparent increase in the track resistance equal up to the unloaded plus the loaded track resistance.

These differences have affected the peak compressive rail stresses in the track subjected to accelerating train loads with all three analyses predicting stresses in the range of 92.6 to 103.7 N/mm².

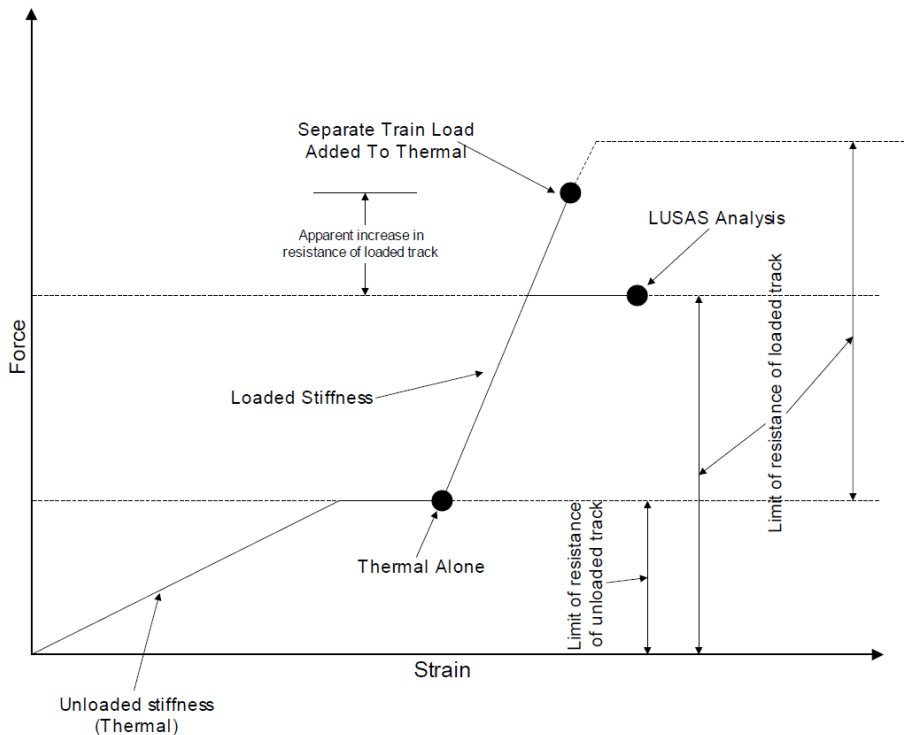


Figure 123: Illustration Of Behaviour Of Separate Analysis Vs. LUSAS Analysis

Looking now at the track/rail that has the braking train on it, the following figures show the same yield plots for this track/rail resistance. The immediate observation again is the different yield behaviour observed for the LUSAS analysis. Looking initially at the separate analysis and the concurrent thermal and rail loading analysis the yielding observed in the thermal alone for the separate analysis (Figure 124) shows close similarity to the yielding observed when the thermal and train loading are applied concurrently (Figure 126) – minimal yielding is observed under the action of the train load alone in the separate analysis (Figure 125).

Concentrating on the LUSAS analysis, the front of the braking train load is just over the right end of the structure and the carriages cover most of the remaining bridge. This has the effect, unlike the accelerating track, of changing nearly all of the resistance from unloaded to loaded for this track over the bridge and therefore the interaction is no longer under yield because the loaded resistance now governs plastic yield. The LUSAS analysis however does not display the possible apparent increase in the resistance of the track that can be observed with the separate analysis method. This means the track interaction around the front of the braking train resisting the movement of the rails cannot sustain the same level of loading and therefore yield to a larger

Analysis of Combined Thermal and Rail Loading Taking Account of Effects of Material Change Under Rail Loading

extent than observed in the separate analysis, thereby reducing the compressive stress in the rails underneath the train – compare Figure 125 and Figure 127 where the yielding underneath the braking train is greater for the LUSAS analysis than in the separate rail load analysis.

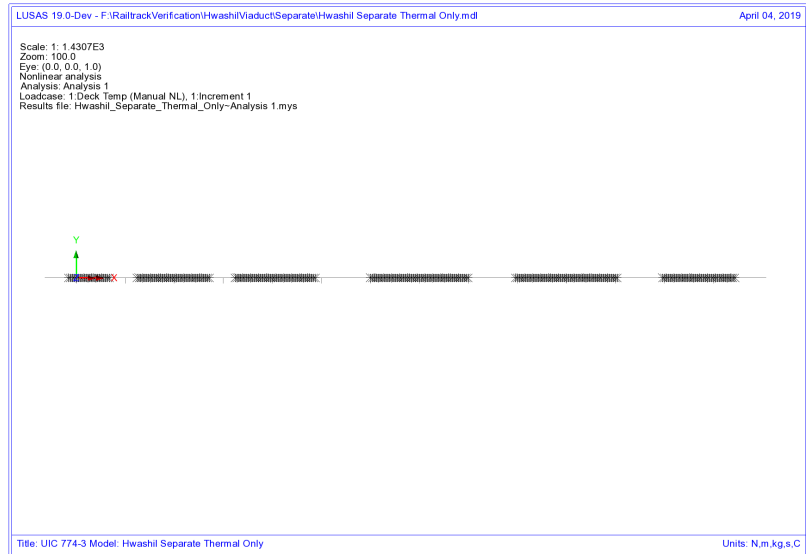


Figure 124: Track/Rail 1 Yield Due To Thermal Load On Track Alone

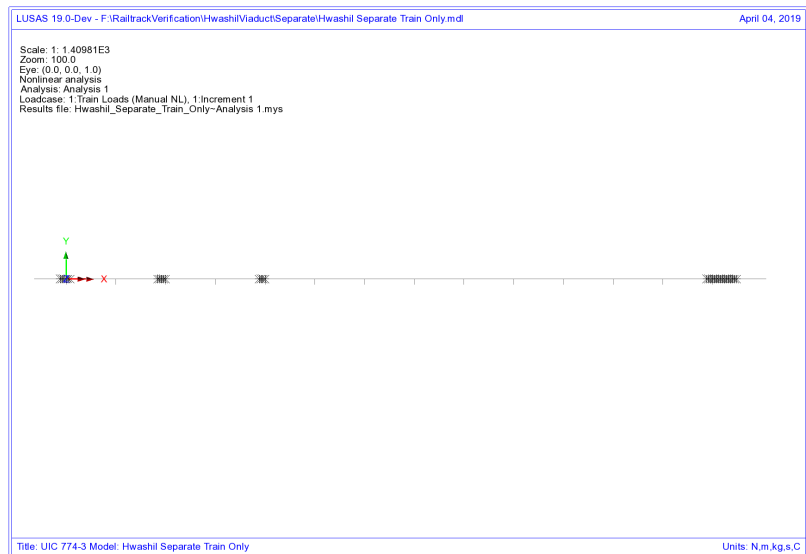


Figure 125: Track/Rail 1 Yield Due To Braking Train Loads On Track 1 – Separate Analysis

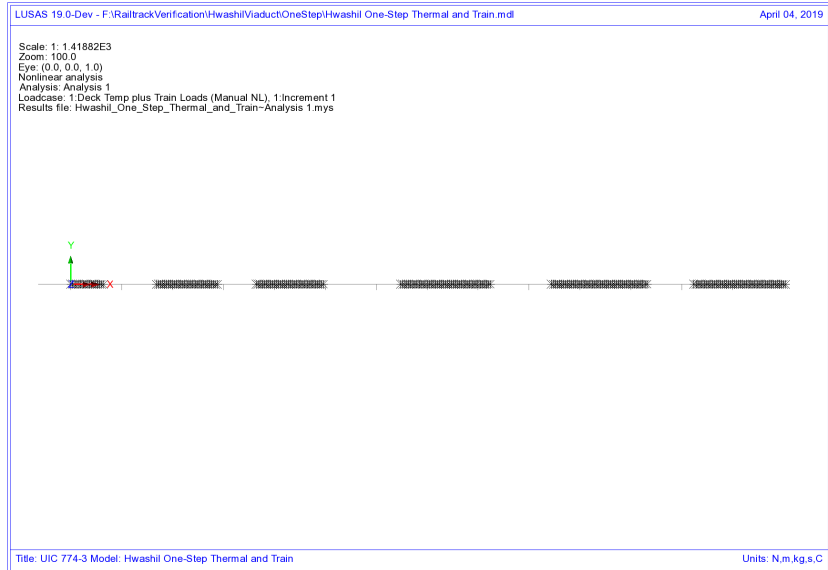


Figure 126: Track/Rail 1 Yield Due To Braking Train Loads On Track 1 - Thermal And Rail Applied Concurrently

Analysis of Combined Thermal and Rail Loading Taking Account of Effects of Material Change Under Rail Loading

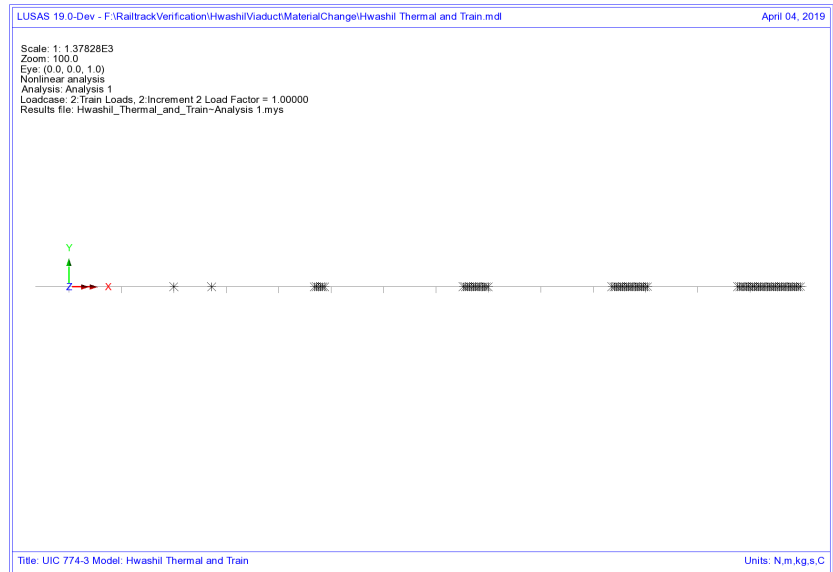


Figure 127: Track/Rail 1 Yield Due To Braking Train Load On Track 1 - LUSAS Combined Analysis

Looking at the behaviour of the track interaction for the separate analysis we can plot the values of the force per metre length for the track subjected to the braking train loads. Figure 128 and Figure 129 show the forces per metre length for the thermal loading and the train braking loading for the separate analyses. Clearly, near the right-hand abutment, the force per metre length under the thermal loading is equal to 40kN/m and due to the train loading is equal to 60kN/m. Combination of these two results means that the track interaction has mobilised 100kN/m in this region when it is actually only able to mobilise 60kN/m based on the loaded track resistance bilinear curve – the separate analysis method is giving an apparent increase in the loaded track resistance that can be mobilised before plastic yielding occurs. This apparent increase in the loaded track resistance has the consequence of allowing the rail stresses to increase beyond the value that would occur if the true loaded track resistance was used as in the LUSAS modelling where the track resistance is correctly limited to the loaded value of 60kN/m – Figure 130.

NOTE: This difference in the amount of track resistance that can be mobilised in the loaded condition is the main reason for the differences in the solutions obtained for the separate and LUSAS methods and demonstrates that the correct modelling of the interaction is critical to the solution.

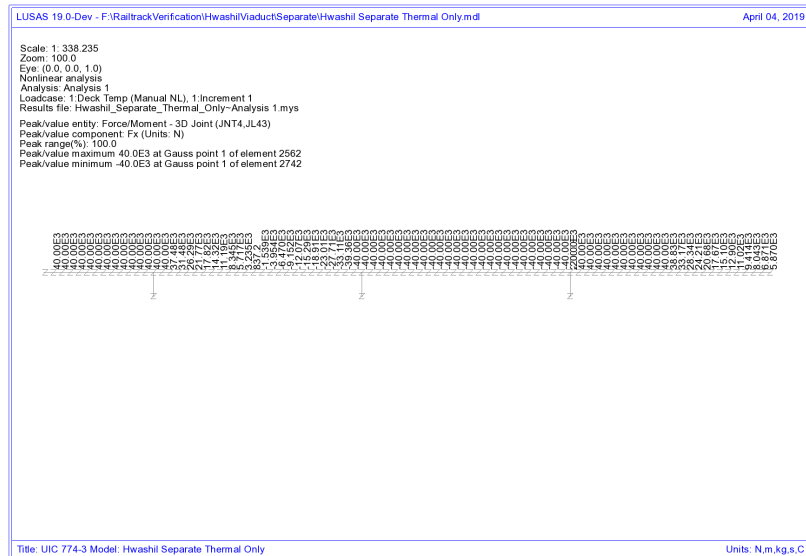


Figure 128: Force In Interaction At Right-Hand End Of Structure Where Peak Compressive Stresses Occur In The Rail - Track 1 – Separate Thermal Loading (N/m length)

Analysis of Combined Thermal and Rail Loading Taking Account of Effects of Material Change Under Rail Loading

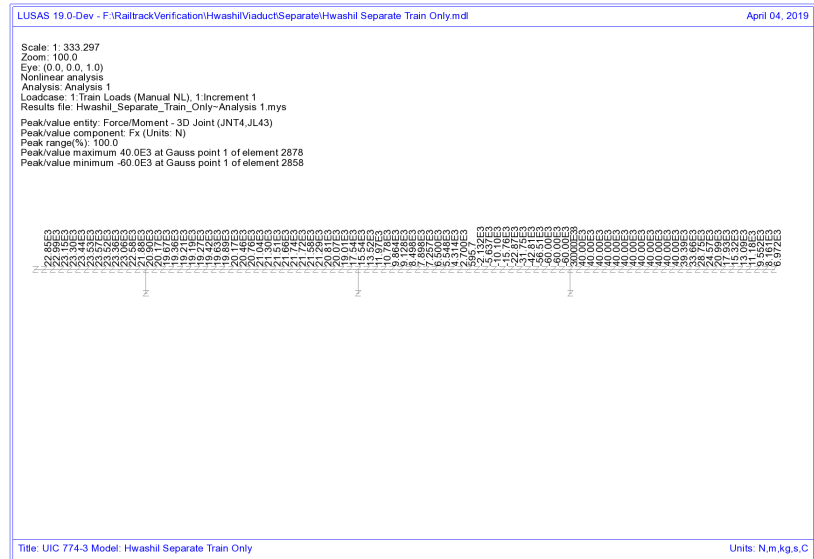


Figure 129: Force In Interaction At Right-Hand End Of Structure Where Peak Compressive Stresses Occur In The Rail - Track 1 - Separate Train Loading (N/m length)

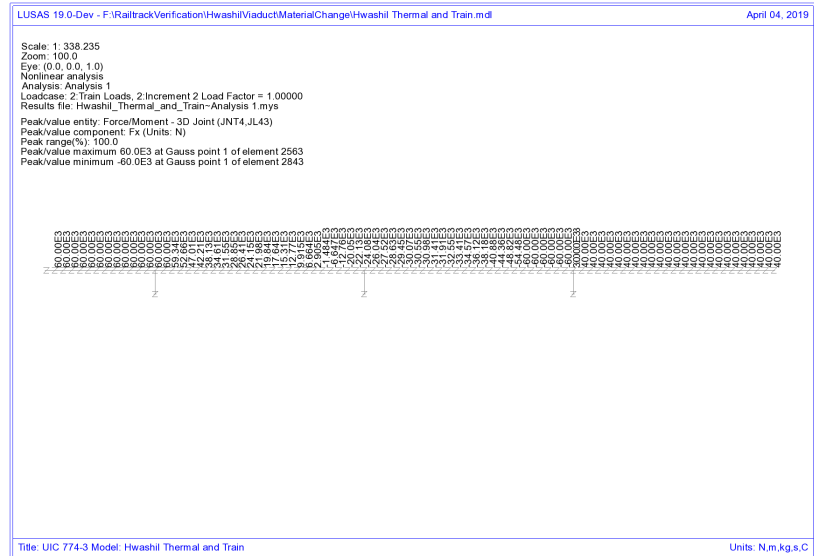


Figure 130: Force In Interaction At Right-Hand End Of Structure Where Peak Compressive Stresses Occur In The Rail - Track 1 – LUSAS Nonlinear (N/m length)

Revisit of UIC774-3 Test E1-3 Using the Separate and LUSAS Methods of Analysis

The standard UIC774-3 test E1-3 has been reanalysed using the following two approaches:

- ❑ Separate analysis of thermal and rail loading effects
- ❑ LUSAS full nonlinear analysis

The results of these two analyses are presented in the following sections and then discussed briefly.

Separate Analyses

The analysis of the thermal effects due to the temperature in the bridge and rail are presented in the following figure. These two thermal effects give a peak compressive rail stress of 155.63 N/mm^2 which compares well with the code of practice value of 156.67 N/mm^2 .

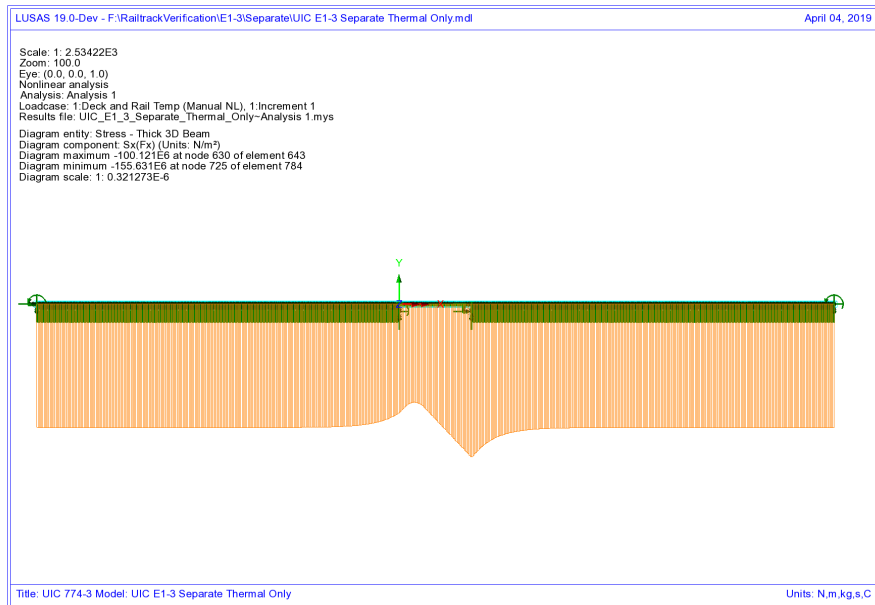


Figure 131: Axial Stress In Rails Due To Temperature In Bridge And Rail

To determine the worst location of the train load for compressive rail stresses the bridge has been analysed with the rail loading at 31 separate locations (starting from the left abutment of the bridge and finishing 90m from the right abutment of the bridge

– train moving from left to right) and these results enveloped. The results of this analysis are presented in the following figure which give a peak compressive rail stress of 40.64 N/mm².

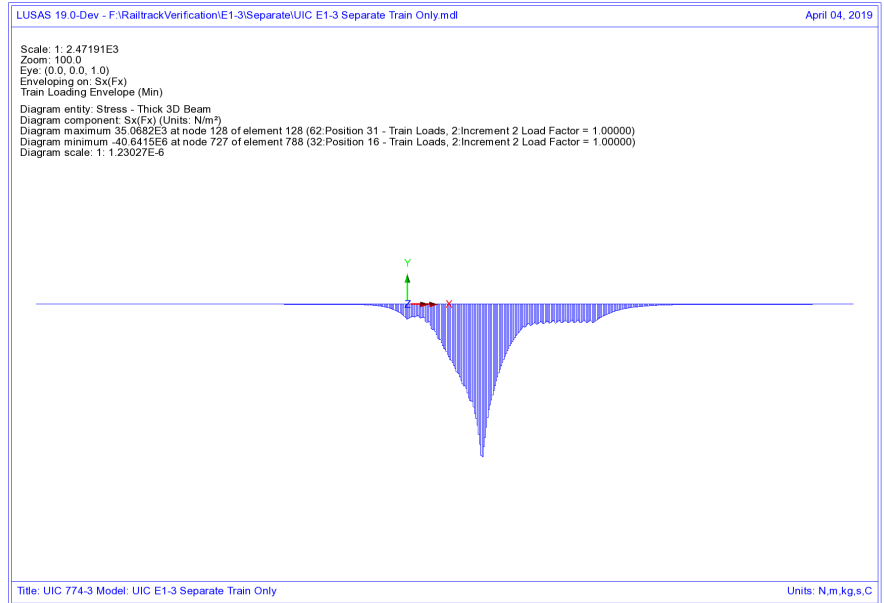


Figure 132: Envelope Of Axial Stress In Rails Due To Rail Loading

Manual combination of the peaks would give a peak compressive rail stress of 196.27 N/mm² (ignoring locations of the peaks) and combination of the results in LUSAS gives the same peak compressive rail stress of 196.27 N/mm² which occurs over the transition from the structure to the embankment at the right-hand abutment.

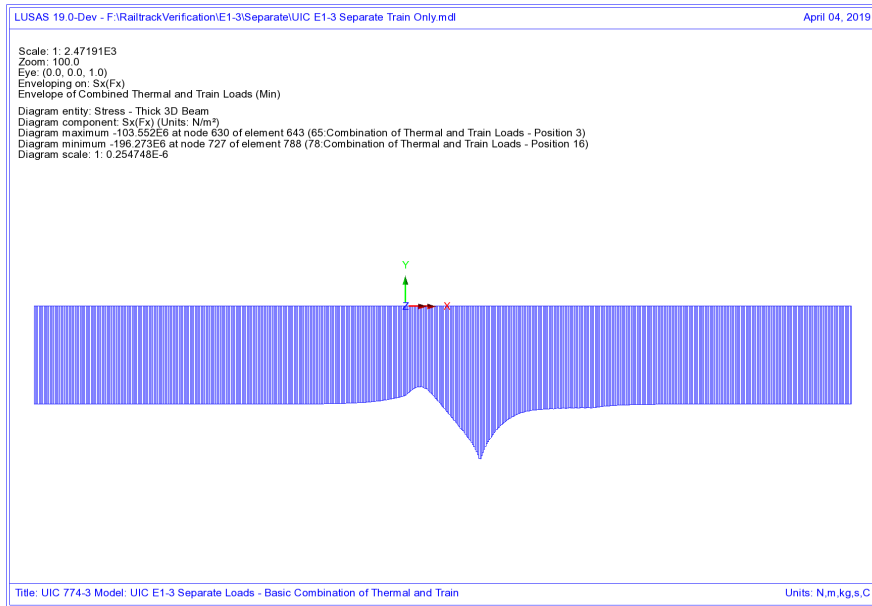


Figure 133: Axial Stress In Rails Due To Combined Temperature And Rail Loading

Comparison of these results with the UIC774-3 code of practice test results shows that the result compares well with the 190.07 N/mm² compressive rail stress from the simplified analysis in the test case (which is based on evaluating the effect of each part of the loading separately).

LUSAS Nonlinear Analysis

The UIC774-3 E1-3 test case has been reanalysed using the LUSAS rail option and gives the following peak compressive rail stress for the thermal loading alone and the combined thermal and rail loading:

Thermal:	155.63 N/mm²
Thermal & Rail:	193.06 N/mm²

Comparison of the results shows that the rail stresses are in excellent agreement for both parts of the analysis with the peak compressive rail stress of the combined thermal and train loading having a percentage error of 5.8% when compared against the target rigorous solution of 182.4 N/mm².

Revisit of UIC774-3 Test E1-3 Using the Separate and LUSAS Methods of Analysis

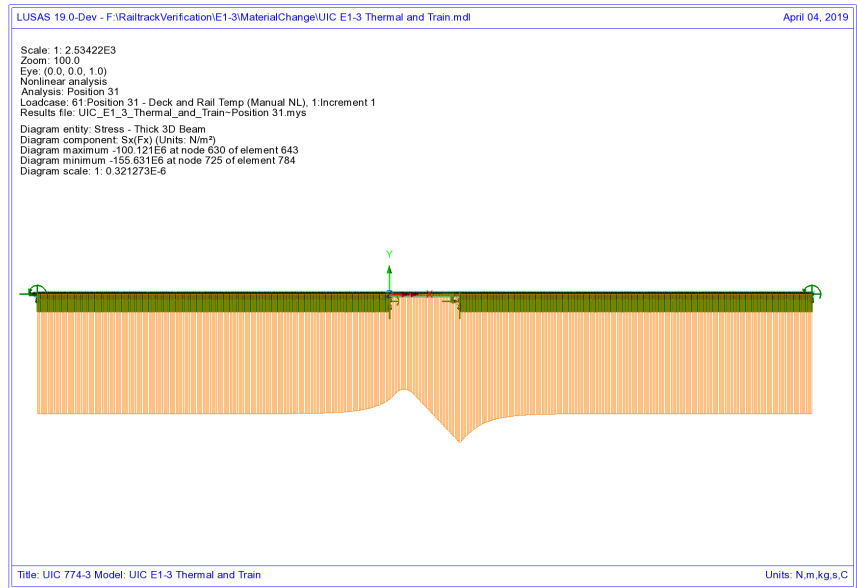


Figure 134: Axial Stress In Rails Due To Temperature In Bridge And Rail

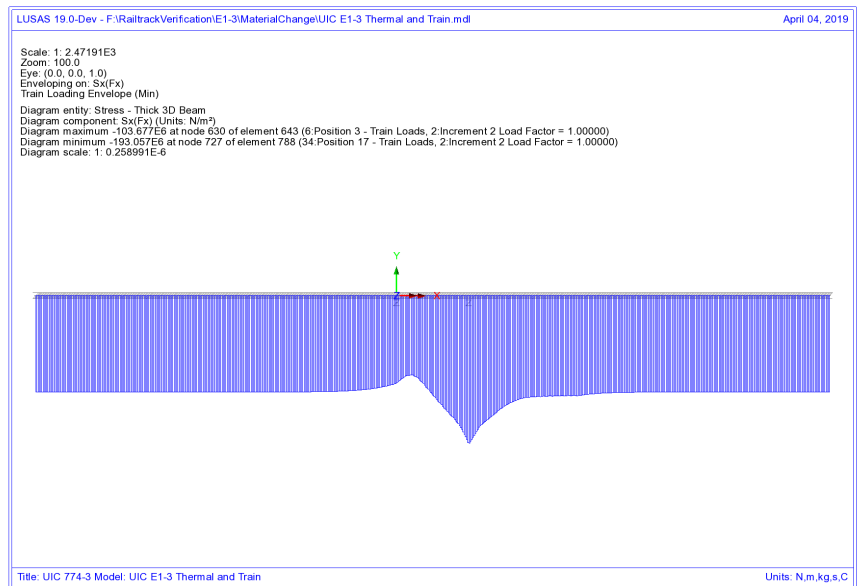


Figure 135: Axial Stress In Rails Due To Combined Temperature And Enveloped Rail Loading

Discussion

For this test case the difference in the results due to the track resistance modelling between the two methods is minimal. Combining the results of two nonlinear analysis, while invalid, gives almost identical results to the LUSAS analysis which correctly represents the transition from unloaded to loaded resistance on arrival of the train load. The train load position that gives the worst compressive stress in the rail does however differ slightly between the two analyses with the separate analysis giving a train front position of 75m from the left abutment of the bridge and the LUSAS combined analysis giving a train front position of 80m from the left abutment of the bridge.

Looking at the yield behaviour it becomes clear why the two methods agree so closely for this UIC774-3 standard test case and not for the Hwashil Viaduct. For both analyses, the rail stresses and interaction yield over the single span bridge due to thermal loading are identical – Figure 136. On consideration of the train loading, the right-hand end of the structure (roller bearing) where the peak compressive rail stresses are observed shows no sign of yield with yield only occurring over the left end and embankment – Figure 137 and Figure 138. This indicates that the separate analysis, while invalid due to the linear combination of two nonlinear analyses, is giving the correct result and this only occurs because the interaction over the structure at this location is nowhere near yield.

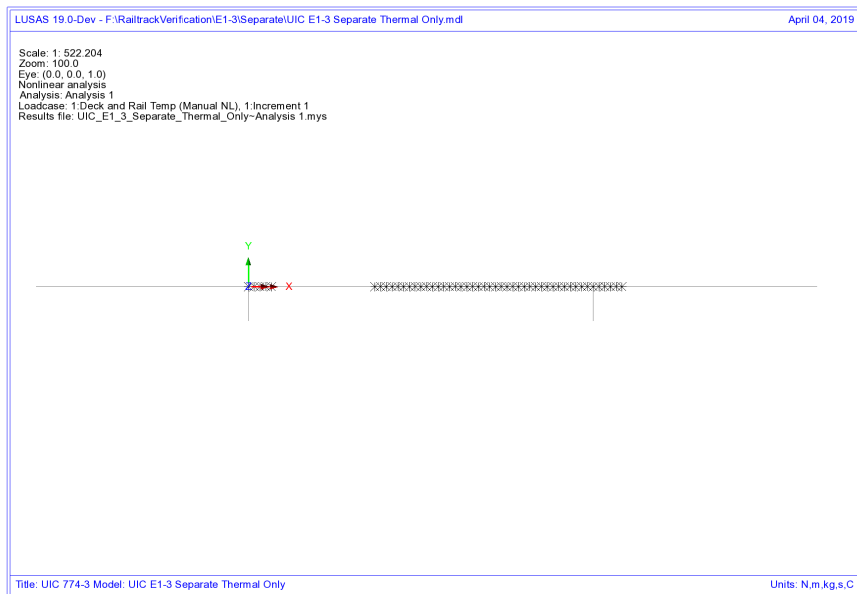


Figure 136: Yield Layout For Thermal Loading Only

Revisit of UIC774-3 Test E1-3 Using the Separate and LUSAS Methods of Analysis

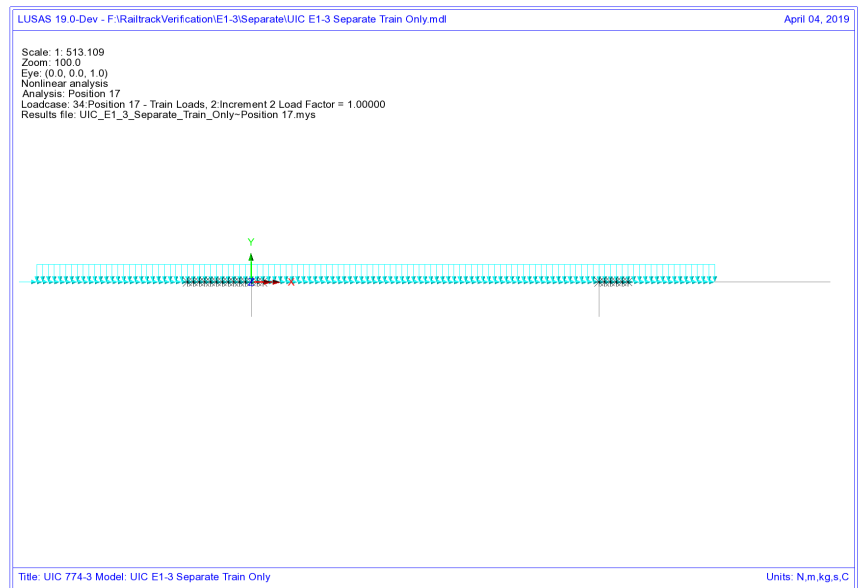


Figure 137: Yield Layout For Train Loading Only From Separate Analysis

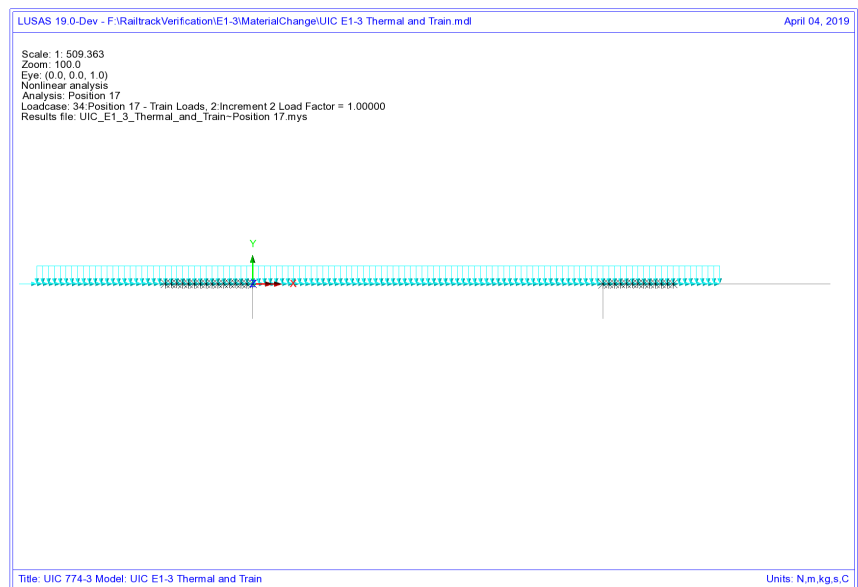


Figure 138: Yield Layout For Combined Thermal And Train Loading From LUSAS Nonlinear Analysis

If, however, the train loading had induced interaction forces in the region of 40 kN/m (taking account of the track resistance already mobilised by the thermal loading) instead of the observed 25.6 kN/m then significant differences could be observed in the two analysis methods as the separate method would still allow a further 20 kN/m track resistance to be mobilised before the onset of plastic yielding and the separate analysis would potentially over predict the rail stresses occurring. This potentially means that...

Revisit of UIC774-3 Test E1-3 Using the Separate and LUSAS Methods of Analysis

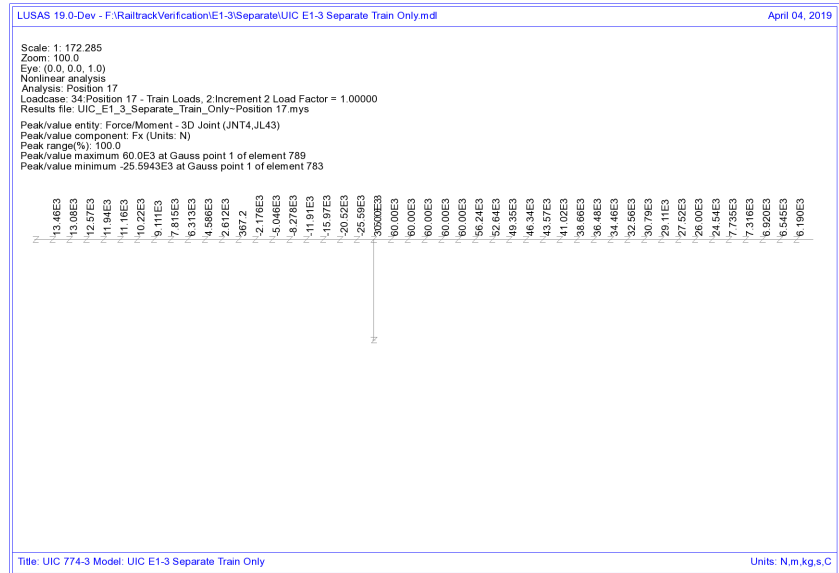


Figure 140: Force Per Metre Length In Interaction From Train Loading - Separate Analysis

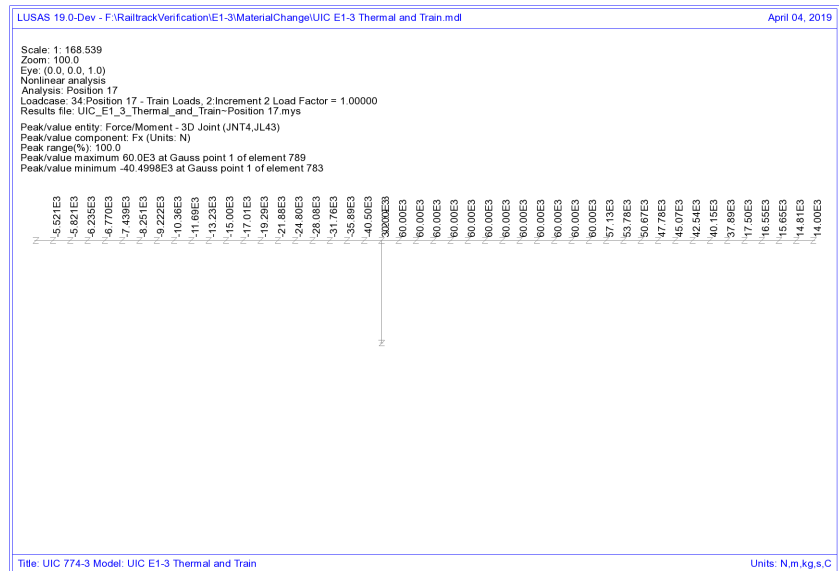


Figure 141: Force Per Metre Length In Interaction From Combined Loading - LUSAS Analysis

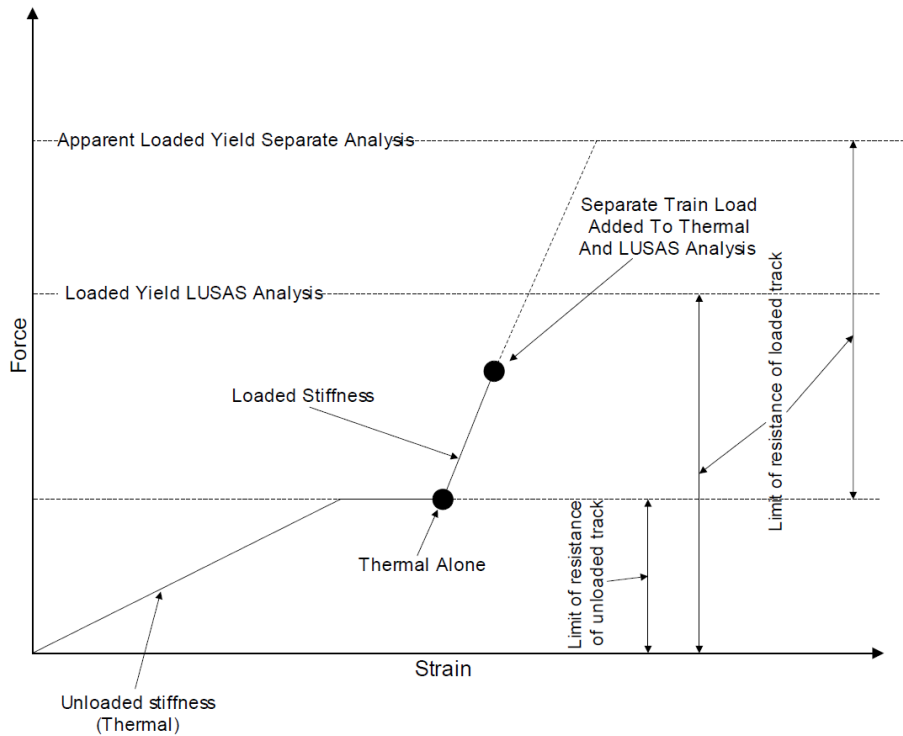


Figure 142: Illustration Of Behaviour For UIC774-3 Standard Test E1-3 For Separate And LUSAS Analyses

Revisit of UIC774-3 Test H1-3 Using the Separate and LUSAS Methods of Analysis

The previous test case (E1-3) is one of the key test cases that must be matched for computer programs carrying out this form of analysis with the results for both the separate method and the LUSAS method being in close agreement to the results required. The deck type for this test is however a concrete slab underlain by I-section steel beams which does not compare with the deck being used for Hwashil Viaduct. For this reason the H1-3 test is also revisited and solved using the two methods of analysis.

Separate Analyses

The analysis of the thermal effects due to the temperature in the bridge and rail are presented in the following figure. These two thermal effects give a peak compressive rail stress of 167.77 N/mm^2 which compares very well with the code of practice value of 169.14 N/mm^2 .

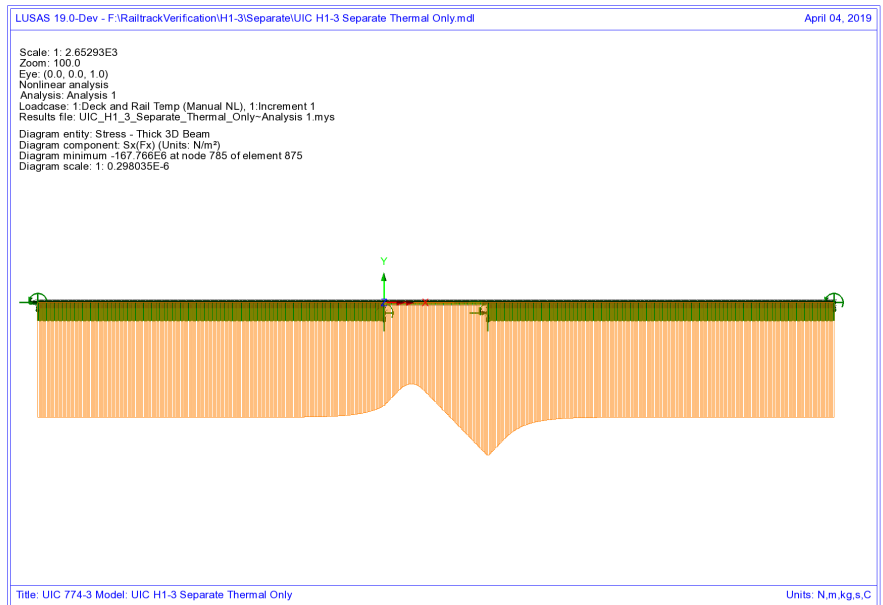


Figure 143: Axial Stress In Rails Due To Temperature In Bridge And Rail

To determine the worst location of the train load for compressive rail stresses the bridge has been analysed with the rail loading at 37 separate locations (starting from the left abutment of the bridge and finishing 90m from the right abutment of the bridge – train moving from left to right) and these results enveloped. The results of this

analysis are presented in the following figure which give a peak compressive rail stress of 29.09 N/mm².

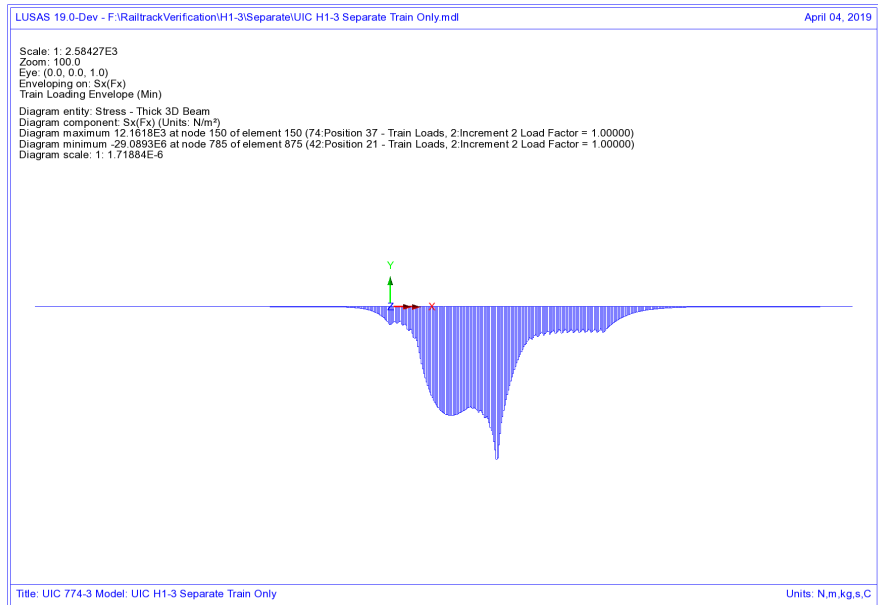


Figure 144: Envelope Of Axial Stress In Rails Due To Rail Loading

Manual combination of the peaks would give a peak compressive rail stress of 196.86 N/mm² (ignoring locations of the peaks) and combination of the results in LUSAS gives 196.86 N/mm² which occurs over the transition from the structure to the embankment at the right-hand abutment.

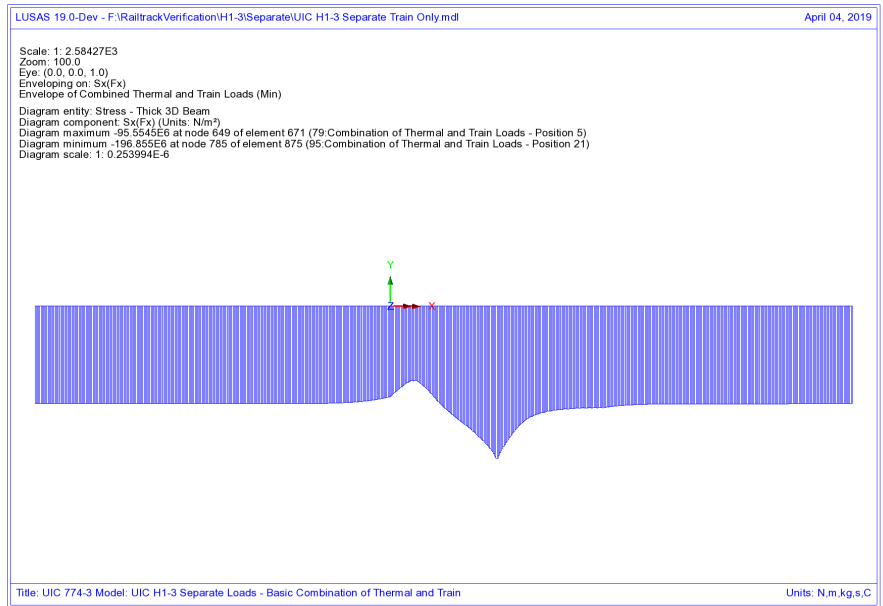


Figure 145: Axial Stress In Rails Due To Combined Temperature And Rail Loading

Comparison of these results with the UIC774-3 code of practice test results shows that the result compares well with the 211.37 N/mm² compressive rail stress from the simplified and the 188.23 N/mm² compressive rail stress from the rigorous analysis in the test case.

LUSAS Nonlinear Analysis

The UIC774-3 H1-3 test case has been reanalysed using the LUSAS rail option and gives the following peak compressive rail stress for the thermal loading alone and the combined thermal and rail loading:

Thermal:	167.77 N/mm²
Thermal & Rail:	195.91 N/mm²

Comparison of the results shows that the rail stresses are in excellent agreement for both parts of the analysis with the peak compressive rail stress of the combined thermal and train loading having a percentage error of 4.1% when compared against the target rigorous solution of 188.23 N/mm².

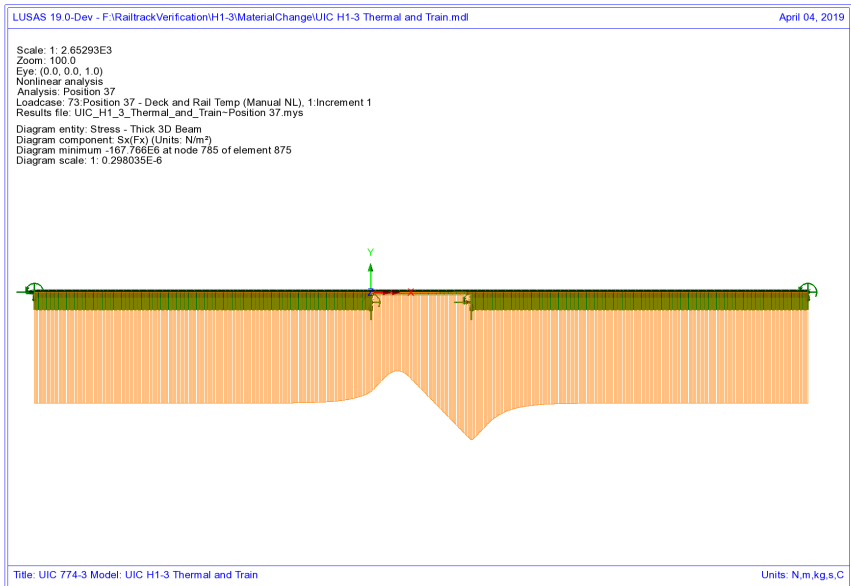


Figure 146: Axial Stress In Rails Due To Temperature In Bridge And Rail

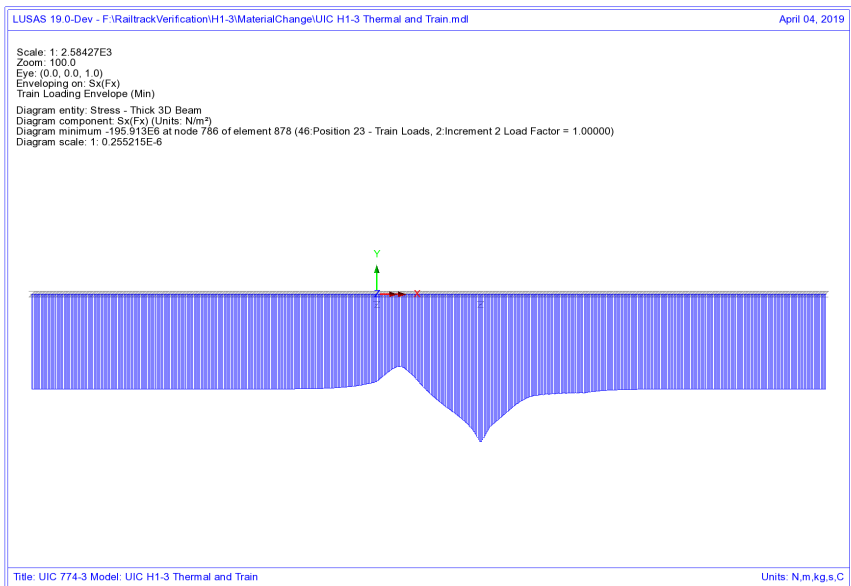


Figure 147: Axial Stress In Rails Due To Combined Temperature And Enveloped Rail Loading

Discussion

As with the previous E1-3 test case, the difference in the results due to the track resistance modelling between the two methods is minimal. Combining the results of two nonlinear analysis, while invalid, gives almost identical results to the LUSAS analysis which correctly represents the transition from unloaded to loaded resistance on arrival of the train load. The train load position that gives the worst compressive stress in the rail does however differ slightly between the two analyses with the separate analysis giving a train front position of 100m from the left abutment of the bridge and the LUSAS combined analysis giving a train front position of 110m from the left abutment of the bridge.

Referring back to test E1-3, similar plots can be generated for the yield and forces in the interaction. These, as with the E1-3 test, show that the train loading is not bringing the force per metre length in the interaction close the loaded yield resistance of 60 kN/m and therefore the separate analysis and LUSAS analysis methods agree even though the separate method potentially allows more track resistance to be mobilised than is allowed when the thermal and rail results are combined.

Separate:	27.6 kN/m
LUSAS:	26.1 kN/m

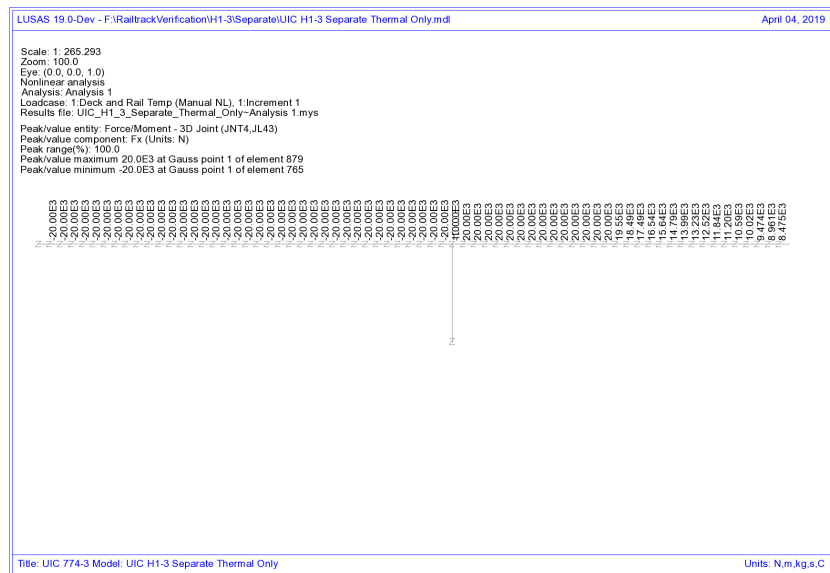


Figure 148: Force Per Metre Length In Interaction From Thermal Loading - Separate Analysis

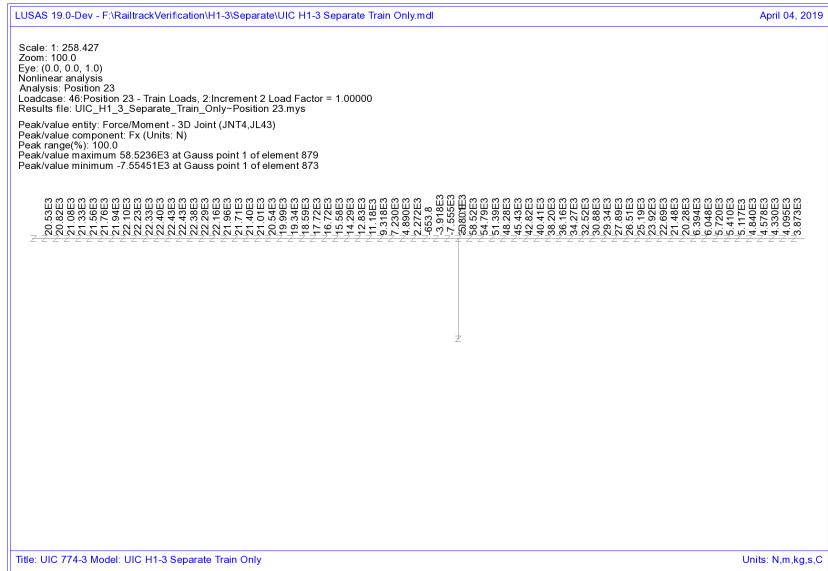


Figure 149: Force Per Metre Length In Interaction From Train Loading - Separate Analysis

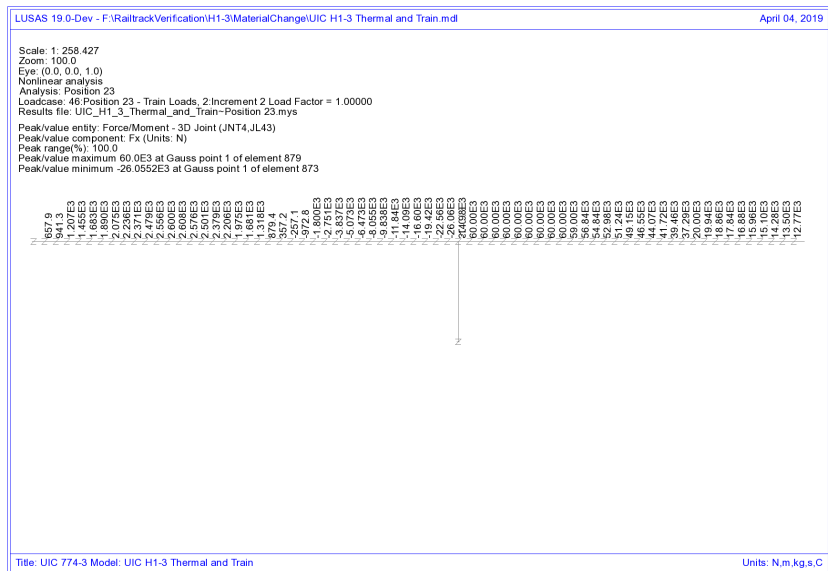


Figure 150: Force Per Metre Length In Interaction From Combined Loading - LUSAS Analysis

Conclusions

Three solution methods for carrying out the UIC track/bridge interaction analyses have been investigated and differences observed in the assumed behaviour and results highlighted. The key observations were as follows:

Separate Thermal and Rail Loading Analysis

- ☐ Correct unloaded track resistance used for thermal effects across whole model
- ☐ Correct yielding of unloaded ballast/frozen ballast-no ballast track under thermal effects
- ☐ Incorrect yielding of loaded ballast/frozen ballast-no ballast track assuming that thermal effects are present, only correct if there are no thermal effects
- ☐ Invalid combination of two nonlinear analyses results gives apparent increase in the resistance of the track due to stresses in ballast/frozen ballast-no ballast track from the unloaded thermal effects being ignored in the ultimate yield of the loaded analysis – to correctly model the reduction of the resistance of the track before yielding occurs under loaded conditions, the yield resistance for the loaded condition should be reduced by the amount of resistance already mobilised due to the thermal effects
- ☐ Separate analysis ignores the movement that has already occurred under the thermal effects when the load from the train acts on the rails

Concurrent Thermal and Rail Loading Analysis

- ☐ Incorrect loaded track resistance used for thermal effects under location of train loads
- ☐ Incorrect yielding of ballast/frozen ballast-no ballast track under thermal effects as loaded track resistance used
- ☐ Correct track resistance for yielding under the train loading
- ☐ Movement due to thermal effects alone only approximated

LUSAS Nonlinear Thermal and Rail Analysis with Material Change

- ☐ Correct unloaded track resistance used for thermal effects across whole model
- ☐ Correct yielding of unloaded ballast/frozen ballast-no ballast track under thermal effects

- ❑ Correct yielding of loaded ballast/frozen ballast-no ballast track under action of combined thermal and train loading effects as track resistance correctly modelled (yield occurs at the correct loading – no apparent increase in the yield value)
- ❑ Instantaneous change from unloaded to loaded track resistance correctly takes account of movement that has already occurred under thermal effects alone.

Referring back to Figure 122 and Figure 123, the key issue with the separate analysis approach is the ability for the track resistance to be overestimated by the combination of the two nonlinear analyses and potentially cause the rail stresses to be overestimated.

In the concurrent loading and LUSAS rail option analyses the limit of track resistance is correctly modelled as the value determined from the loaded bilinear curve and therefore this potentially leads to reduced rail stresses observed in the analyses.

As the initial movement under pure thermal loading in the concurrent analysis uses the loaded track resistance, this will give different results to the LUSAS rail option analysis.

Referring back to the Hwashil Viaduct analyses, the rail stresses observed for the three analysis types are:

	Separate Analysis Of Thermal And Train Loading	Concurrent Thermal And Train Loading	LUSAS Nonlinear Thermal And Train Loading With Material Change
Track 1 (Braking)	94.99	85.61	79.06
Track 2 (Accelerating)	103.66	100.61	92.60

Table 2: Comparison Of Peak Compressive Rail Stresses (in N/mm²) For Different Analysis Methods

Comparison of the results for the separate and LUSAS analyses shows that the peak compressive stress for the separate analysis is 1.2 times that of the LUSAS analysis for track 1 and 1.12 times for track 2. It should be noted however that the separate analysis could be giving an apparent increase in track resistance of up to 1.6 times that of the loaded track due to the combination of the nonlinear results.

The concurrent analysis gave results that are between the separate and LUSAS analysis as expected since the correct limit of loaded track resistance is modelled even though the thermal effects are only approximated.

One overall conclusion is obvious from these test case analyses and discussions made in this appendix:

When a combined thermal and train loading from a separate analysis gives interaction forces that exceed the stated yield resistance then the separate analysis method will potentially over predict the rail stresses unless the loaded track yield surface is reduced by the mobilised track resistance over the extent of the train loading.

References

- U1 UIC Code 774-3 R. Track/bridge Interaction. Recommendations for Calculations (2001) Union Internationale des Chemins de fer, Paris, France

Appendix B:

Definition of

Complex Trainset

Configurations

Introduction

Although some trainsets can be simplified with a few uniformly distributed loads (UDLs) to describe the loading pattern, many trainsets are more complex than this and require the definition of multiple components to describe the overall pattern of loading. Some of these trainset configurations require the modelling of point loads, Uniformly Distributed Loads (UDLs) or the combination of the two. This appendix includes some examples of the definition of more complex trainset configurations which require such loading patterns.

Definition of Trainset Configurations With UDLs Alone

The UDL loading allows the definition of trainset configurations where the load is spread over lengths of the track as illustrated by the example shown in Figure 151. In this configuration the vertical load varies along the length of the trainset and the acceleration / traction load acts only over the length of the locomotive(s). In the definition the train is accelerating to the left for any structure model it is applied to with the origin of the trainset loading defined at the left-hand extent of the configuration. Any number of UDLs can be used for the definition of the trainsets in the **Loading** worksheet of the input Excel or compatible XLSX spreadsheet to allow more complex configurations to be defined.

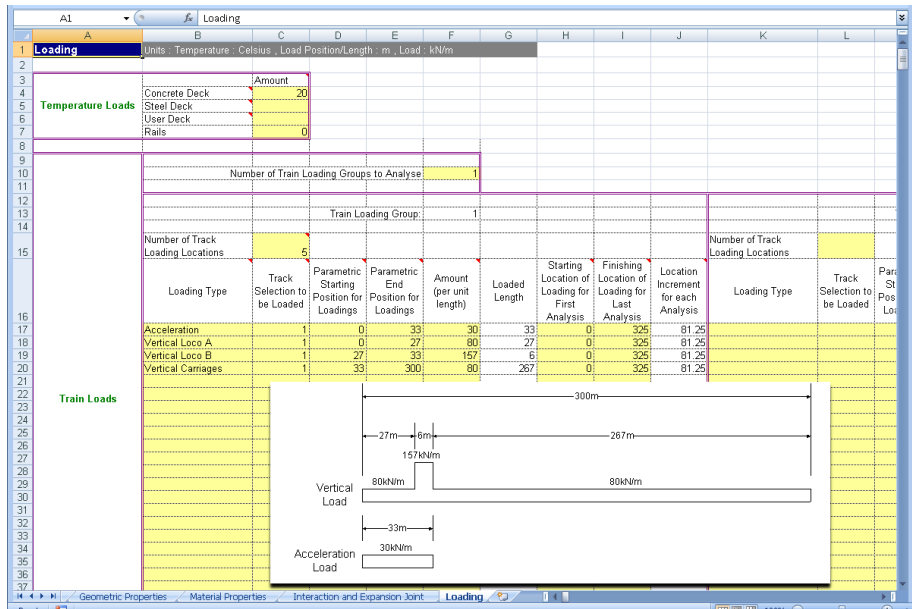


Figure 151: More Complex Train Loading Definition in Spreadsheet

Additional simple examples were illustrated in Figure 44 on page 42 showing the types of loading configurations that can be defined.

EuroCode Load Model SW/0 Loading Configuration

The SW/0 vertical loading pattern is shown in Figure 152 which has two separated UDLs. In addition, Note 1 of Clause 6.5.3 'Actions due to traction and braking' within BS EN 1991-2:2003 states that *'For Load Models SW/0 and SW/2 traction and braking forces need only be applied to those parts of the structure which are loaded according to Figure 6.2 and Table 6.1'* where this figure is equivalent to Figure 152 below. The definition of the SW/0 trainset configuration will therefore be described below according to these conditions.

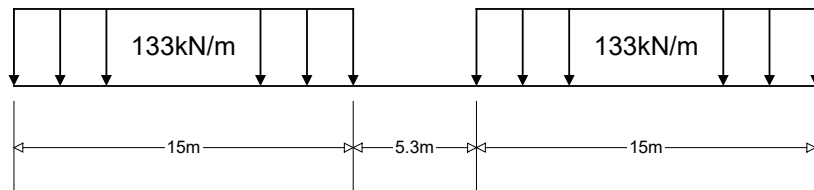


Figure 152: EuroCode Load Model SW/0 Train Vertical Load Pattern

For trainset loading configurations such as EuroCode SW/0 (and also SW/2) it is often best (but not essential) to define the origin of the trainset configuration at the centre of the load pattern.

Considering first the vertical loading, if we take the centre of the load configuration as the origin we can define the UDLs as follows:

Loading Type	Left Coordinate (m)	Right Coordinate (m)	Amount per Unit Length (kN/m)
Vertical SW/0 (Left UDL)	-17.65	-2.65	133.0
Vertical SW/0 (Right UDL)	+2.65	+17.65	133.0

Table 3: SW/0 Parametric Vertical Loading Definition

As stated in BS EN 1991-2:2003 Clause 6.5.3, the braking load from the SW/0 trainset should be defined as a UDL over the parts that are loaded and with a value of 20kN/m (limited to 6000kN total load) in the direction of travel. Assuming that we are defining the SW/0 trainset travelling to the right in the Rail Track Analysis model the loading configuration will be as illustrated in Figure 153 with the loading origin at the centre.

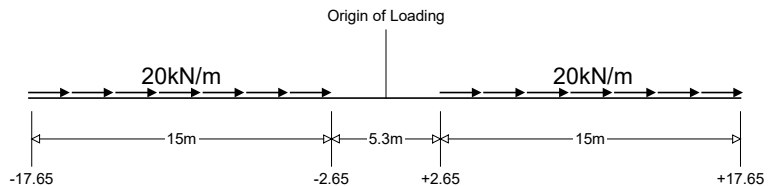


Figure 153: EuroCode SW/0 Train Braking Load Pattern

The total braking load in accordance with the figure above will be only 600kN which is below the limit, therefore the braking load requires no adjustment and can be defined as follows:

Loading Type	Left Coordinate (m)	Right Coordinate (m)	Amount per Unit Length (kN/m)
Braking SW/0 (Left UDL)	-17.65	-2.65	20.0
Braking SW/0 (Right UDL)	+2.65	+17.65	20.0

Table 4: SW/0 Parametric Braking Loading Definition

longitudinal braking and traction loads that should be considered with Load Model 71 but these are not considered here. For this example we will only consider the definition of the four 250kN concentrated loads shown in Figure 156 (with the origin of the loading taken at the centre) and how these can be approximated within the Rail Track Analysis tool.

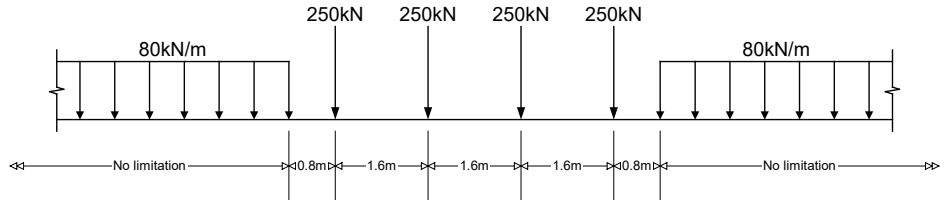


Figure 155: EuroCode Load Model 71 Train Vertical Load Pattern

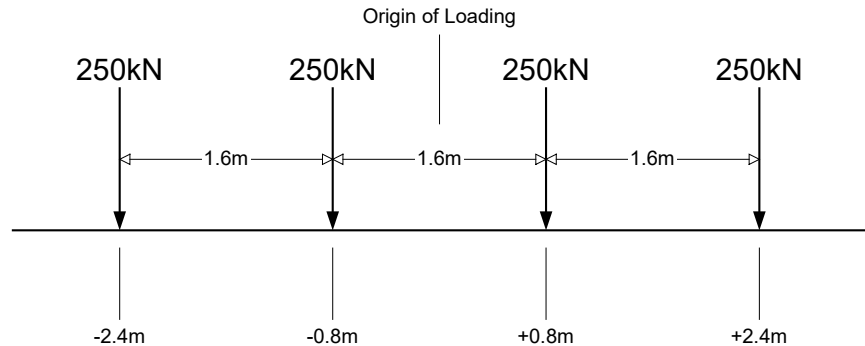


Figure 156: Load Model 71 Concentrated Loads Only

Although the Rail Track Analysis tool only allows the input of trainset loading through UDLs these concentrated loads can be defined by recognising that for the size of elements used in the model the concentrated load is equivalent to a UDL over a very small length. If our structural modelling has element lengths of 1.0 to 2.0m then the setting of the contact length as 1 to 5% of this length (0.01 to 0.05m for 1.0m and 0.02 to 0.1m for 2.0m elements) should be sufficient to define the equivalent UDL to the concentrated load for a good number of structural configurations. Obviously the smaller the contact length the closer the equivalent UDL comes to a concentrated load.



Note. The choice of the contact length to be used to define the equivalent UDL to a concentrated load must be decided by the user based on the configuration of the model

and the element lengths used for the meshing of that model. The illustration here should be viewed as a guide on how to incorporate concentrated loads with a trainset definition and not as the de facto contact length to be used for all circumstances.

Taking the contact length for this example as 0.01m the equivalent UDLs for the modelling will therefore have a value of:

$$\text{UDL} = \text{Conc.Load/ContactLength} = 250\text{kN}/0.01\text{m} = 25000\text{kN/m}$$

The definition of the four concentrated loads of Load Model 71 now becomes the four UDLs indicated in Figure 157.

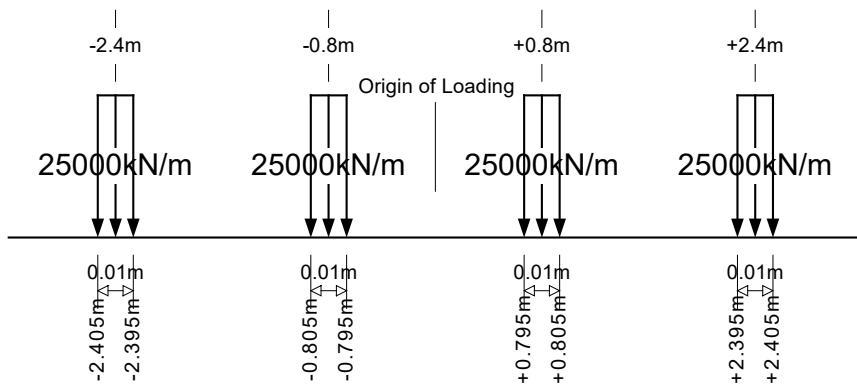


Figure 157: Load Model 71 Equivalent UDLs to Concentrated Loads

This UDL definition of the four concentrated loads of Load Model 71 can now be defined in the **Loading** worksheet of the input XLSX spreadsheet as illustrated in Figure 158.

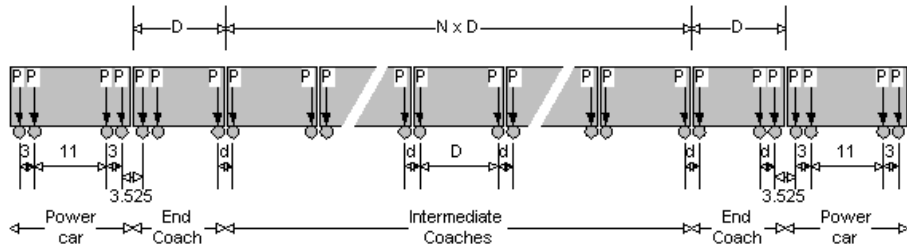


Figure 159: EuroCode Load Model HSLM-A Train Vertical Load Pattern

Figure 160 shows a HSLM-A1 trainset (with braking loads) which has been defined in the **Loading** worksheet using the equivalent UDL approach for the concentrated loads. The input just for the single HSLM-A1 braking trainset requires 51 rows of data input to define all of the axle loads and the braking load.

A1 Loading											
S	T	U	V	W	X	Y	Z	AA	AB	AC	
1											
2											
3											
4											
5											
6											
7											
8											
9											
10											
11											
12											
13											
14											
15											
16											
17											
18											
19											
20											
21											
22											
23											
24											
25											
26											
27											
28											
29											
30											
31											
32											
33											
34											
35											
36											
37											

Figure 160: HSLM-A1 Trainset Defined In Loading Worksheet

It would take some time (and be prone to errors) to manually input all of the equivalent UDLs for the concentrated loads illustrated above for the HSLM-A trainset

configuration. These loads should therefore be defined through an automated method such as another an Excel or compatible XLSX spreadsheet which defines the required data or by using the VBScript capabilities of LUSAS Modeller to parametrically define the trainset loads. Such a VBScript has been written as a demonstration for these HSLM-A trainset configurations.



Note. The VBScript included within this appendix was used to generate the data used in the worked example. The implementation has a number of assumptions which are detailed below.

The HSLM-A trainset definition VBScript is written based on the following assumptions (code is listed at the end of this appendix and is also available from the User Area on the LUSAS website):

- The braking trainset load definition assumes that the HSLM-A train is moving from left to right, the accelerating trainset load definition assumes that the HSLM-A train is moving from right to left (these can be changed by simply reversing the sign of the longitudinal loading values)
- Traction loads are applied as a UDL between the front and back axles of each of the power cars only. If the maximum load of 1000kN stated in Clause 6.5.3 of BS EN 1991-2:2003 is exceeded the loading is factored to ensure only 1000kN is defined
- Braking loads are applied as a UDL over the whole length of the trainset between the first and last axles. If the maximum load of 6000kN stated in Clause 6.5.3 of BS EN 1991-2:2003 is exceeded the loading is factored to ensure only 6000kN is defined
- The point loads are defined as equivalent UDLs using a user defined contact length (default = 0.01m)
- The origin of the HSLM-A trainset is defined at the centre of the trainset configuration when specifying the locations for the trainset across the embankments and structure
- The units are kN and m in accordance with the input requirements of the Rail Track Analysis tool.

The VBScript is run as follows:

- 1) Run the “Define_HSLM-A_for_RT.A.vbs” VBScript
- 2) Enter the HSLM-A universal train ID (1 to 10) as shown below:

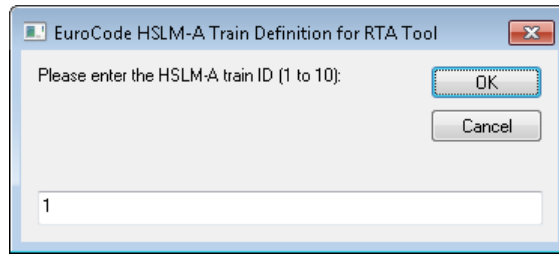


Figure 161: Input of the HSLM-A Train Configuration ID

3) Enter the contact length for the equivalent UDLs to represent the axle concentrated loads (in m):

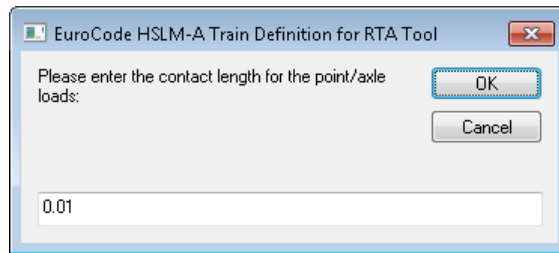


Figure 162: Input of the Contact Length for the UDLs Equivalent to the Concentrated Loads

4) Enter the filename for the generated TAB delimited trainset loading definition (with the *.prn extension):

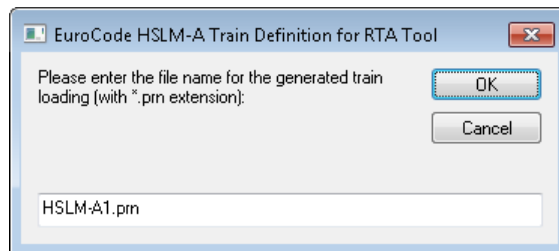


Figure 163: Input of the Filename for the Output of the HSLM-A Train Configuration

On clicking OK the VBScript will now process the HSLM-A loading and generate a TAB delimited text file defining all of the loading for a braking train and an accelerating train as indicated in Figure 164 and Figure 165 (for a HSLM-A1 trainset with 0.01m contact length for the equivalent UDLs).

Definition of Trainset Configurations With Concentrated Loads

```

1 This TAB delimited file defines the HSLM-A1 train definitions for a braking train travelling in the
2 positive (to the right) direction in the RTA model
3 and an accelerating train travelling in the negative (to the left) direction in the RTA model.
4
5 The vertical and braking loads for the braking train are defined first, followed by the vertical and
6 traction loads for the accelerating train.
7
8 After importing into Microsoft Excel the appropriate loads for the analysis being considered can be
9 copied and pasted into the input spreadsheet.
10
11 Contact length for point/axle loads = 0.01
12 Origin for loading is the middle of the trainset.
13
14 BRAKING HSLM-A1 TRAIN
15 Vertical (Left power car axle 1) TrackID -198.7675 -198.7575 17000
16 Vertical (Left power car axle 2) TrackID -195.7675 -195.7575 17000
17 Vertical (Left power car axle 3) TrackID -184.7675 -184.7575 17000
18 Vertical (Left power car axle 4) TrackID -181.7675 -181.7575 17000
19 Vertical (Left end coach axle 1) TrackID -178.2425 -178.2325 17000
20 Vertical (Left end coach axle 2) TrackID -176.2425 -176.2325 17000
21 Vertical (Left end coach axle 3) TrackID -163.005 -162.995 17000
22 Vertical (Int. coach 1 axle 1) TrackID -161.005 -160.995 17000
23 Vertical (Int. coach 1 axle 2) TrackID -145.005 -144.995 17000
24 Vertical (Int. coach 2 axle 1) TrackID -143.005 -142.995 17000
25 Vertical (Int. coach 2 axle 2) TrackID -127.005 -126.995 17000
26 Vertical (Int. coach 3 axle 1) TrackID -125.005 -124.995 17000
27 Vertical (Int. coach 3 axle 2) TrackID -109.005 -108.995 17000
28 Vertical (Int. coach 4 axle 1) TrackID -107.005 -106.995 17000
29
30 Braking load UDL has been factored as total load over the 397.525 m trainset is 7950.5 kN (> 6000 kN
31 limit for default UDL)
32 Braking load UDL reduced to = 15.093390352808 kN/m
33
34 ACCELERATING HSLM-A1 TRAIN
35 Vertical (Left power car axle 1) TrackID -198.7675 -198.7575 17000
36 Vertical (Left power car axle 2) TrackID -195.7675 -195.7575 17000
37 Vertical (Left power car axle 3) TrackID -184.7675 -184.7575 17000
38 Vertical (Left power car axle 4) TrackID -181.7675 -181.7575 17000
39 Vertical (Left end coach axle 1) TrackID -178.2425 -178.2325 17000
40 Vertical (Left end coach axle 2) TrackID -176.2425 -176.2325 17000
41 Vertical (Left end coach axle 3) TrackID -163.005 -162.995 17000
42 Vertical (Int. coach 1 axle 1) TrackID -161.005 -160.995 17000
43 Vertical (Int. coach 1 axle 2) TrackID -145.005 -144.995 17000
44 Vertical (Int. coach 2 axle 1) TrackID -143.005 -142.995 17000
45 Vertical (Int. coach 2 axle 2) TrackID -127.005 -126.995 17000
46 Vertical (Int. coach 3 axle 1) TrackID -125.005 -124.995 17000
47 Vertical (Int. coach 3 axle 2) TrackID -109.005 -108.995 17000
48 Vertical (Int. coach 4 axle 1) TrackID -107.005 -106.995 17000
49
50 Braking load UDL has been factored as total load over the 397.525 m trainset is 7950.5 kN (> 6000 kN
51 limit for default UDL)
52 Braking load UDL reduced to = 15.093390352808 kN/m
53
54
55 Vertical (Int. coach 18 axle 2) TrackID 160.995 161.005 17000
56 Vertical (Right end coach axle 1) TrackID 162.995 163.005 17000
57 Vertical (Right end coach axle 2) TrackID 176.2325 176.2425 17000
58 Vertical (Right end coach axle 3) TrackID 178.2325 178.2425 17000
59 Vertical (Right power car axle 1) TrackID 181.7575 181.7675 17000
60 Vertical (Right power car axle 2) TrackID 184.7575 184.7675 17000
61 Vertical (Right power car axle 3) TrackID 195.7575 195.7675 17000
62 Vertical (Right power car axle 4) TrackID 198.7575 198.7675 17000
63 Braking TrackID -198.7625 198.7625 15.093390352808
64
65 Braking load UDL has been factored as total load over the 397.525 m trainset is 7950.5 kN (> 6000 kN
66 limit for default UDL)
67 Braking load UDL reduced to = 15.093390352808 kN/m
68
69
70 ACCELERATING HSLM-A1 TRAIN
71 Vertical (Left power car axle 1) TrackID -198.7675 -198.7575 17000
72 Vertical (Left power car axle 2) TrackID -195.7675 -195.7575 17000
73 Vertical (Left power car axle 3) TrackID -184.7675 -184.7575 17000
74 Vertical (Left power car axle 4) TrackID -181.7675 -181.7575 17000
75 Vertical (Left end coach axle 1) TrackID -178.2425 -178.2325 17000
76 Vertical (Left end coach axle 2) TrackID -176.2425 -176.2325 17000
77 Vertical (Left end coach axle 3) TrackID -163.005 -162.995 17000
78 Vertical (Int. coach 1 axle 1) TrackID -161.005 -160.995 17000
79 Vertical (Int. coach 1 axle 2) TrackID -145.005 -144.995 17000
80 Vertical (Int. coach 2 axle 1) TrackID -143.005 -142.995 17000
81 Vertical (Int. coach 2 axle 2) TrackID -127.005 -126.995 17000
82 Vertical (Int. coach 3 axle 1) TrackID -125.005 -124.995 17000
83 Vertical (Int. coach 3 axle 2) TrackID -109.005 -108.995 17000
84 Vertical (Int. coach 4 axle 1) TrackID -107.005 -106.995 17000
85
86 Braking load UDL has been factored as total load over the 397.525 m trainset is 7950.5 kN (> 6000 kN
87 limit for default UDL)
88 Braking load UDL reduced to = 15.093390352808 kN/m
89
90
91
92
93
94
95
96
97
98
99
100

```

Figure 164: Output for a HSLM-A1 Trainset Configuration (1 of 2)

```

100 Vertical (Int. coach 12 axle 1) TrackID 36.995 37.005 17000
101 Vertical (Int. coach 12 axle 2) TrackID 52.995 53.005 17000
102 Vertical (Int. coach 13 axle 1) TrackID 54.995 55.005 17000
103 Vertical (Int. coach 13 axle 2) TrackID 70.995 71.005 17000
104 Vertical (Int. coach 14 axle 1) TrackID 72.995 73.005 17000
105 Vertical (Int. coach 14 axle 2) TrackID 88.995 89.005 17000
106 Vertical (Int. coach 15 axle 1) TrackID 90.995 91.005 17000
107 Vertical (Int. coach 15 axle 2) TrackID 106.995 107.005 17000
108 Vertical (Int. coach 16 axle 1) TrackID 108.995 109.005 17000
109 Vertical (Int. coach 16 axle 2) TrackID 124.995 125.005 17000
110 Vertical (Int. coach 17 axle 1) TrackID 126.995 127.005 17000
111 Vertical (Int. coach 17 axle 2) TrackID 142.995 143.005 17000
112 Vertical (Int. coach 18 axle 1) TrackID 144.995 145.005 17000
113 Vertical (Int. coach 18 axle 2) TrackID 160.995 161.005 17000
114 Vertical (Right end coach axle 1) TrackID 162.995 163.005 17000
115 Vertical (Right end coach axle 2) TrackID 176.2325 176.2425 17000
116 Vertical (Right end coach axle 3) TrackID 178.2325 178.2425 17000
117 Vertical (Right power car axle 1) TrackID 181.7575 181.7675 17000
118 Vertical (Right power car axle 2) TrackID 184.7575 184.7675 17000
119 Vertical (Right power car axle 3) TrackID 195.7575 195.7675 17000
120 Vertical (Right power car axle 4) TrackID 198.7575 198.7675 17000
121 Traction (Left power car) TrackID -198.7625 -181.7625 29.4117647058824
122 Traction (Right power car) TrackID 181.7625 198.7625 29.4117647058824
123
124 Traction load UDL has been factored as total load over the two 17 m power cars is 1122 kN (> 1000 kN
    limit for default UDL)
125 Traction load UDL reduced to = 29.4117647058824 kN/m
126
  
```

Figure 165: Output for a HSLM-A1 Trainset Configurations (2 of 2)

To use this trainset loading within the **Loading** worksheet of the input XLSX spreadsheet you should initially have the input spreadsheet which has been edited to represent the structure loaded. To transfer this data defined by the VBScript into the worksheet:

- 1) Import the TAB delimited file generated above into Microsoft Excel (or an equivalent application).
- 2) Highlight the braking or accelerating/traction loading to be copied (only the rows defining the vertical and braking/traction loading) and choose Copy – below we are copying the braking trainset

Definition of Trainset Configurations With Concentrated Loads

A13 Vertical (Left power car axle 1)												
A	B	C	D	E	F	G	H	I	J	K	L	
1	This TAB delimited file defines the HSLM-A1 train definitions for a braking train travelling in the positive (to the right) direction in the RTA model											
2	and an accelerating train travelling in the negative (to the left) direction in the RTA model.											
3												
4	The vertical and braking loads for the braking train are defined first, followed by the vertical and traction loads for the accelerating train.											
5	After importing into Microsoft Excel the appropriate loads for the analysis being considered can be copied and pasted into the input spreadsheet.											
6												
7	Contact length for point/axle loads = 0.01											
8	Origin for loading is the middle of the trainset.											
9												
10												
11												
12	BRAKING HSLM-A1 TRAIN											
13	Vertical (Left power car axle 1)	TrackID	-198.7675	-198.7575	17000							
14	Vertical (Left power car axle 2)	TrackID	-195.7675	-195.7575	17000							
15	Vertical (Left power car axle 3)	TrackID	-184.7675	-184.7575	17000							
16	Vertical (Left power car axle 4)	TrackID	-181.7675	-181.7575	17000							
17	Vertical (Left end coach axle 1)	TrackID	-178.2425	-178.2325	17000							
18	Vertical (Left end coach axle 2)	TrackID	-176.2425	-176.2325	17000							
19	Vertical (Left end coach axle 3)	TrackID	-163.005	-162.995	17000							
20	Vertical (Int. coach 1 axle 1)	TrackID	-161.005	-160.995	17000							
21	Vertical (Int. coach 1 axle 2)	TrackID	-145.005	-144.995	17000							
22	Vertical (Int. coach 2 axle 1)	TrackID	-143.005	-142.995	17000							
23	Vertical (Int. coach 2 axle 2)	TrackID	-127.005	-126.995	17000							
24	Vertical (Int. coach 3 axle 1)	TrackID	-125.005	-124.995	17000							
25	Vertical (Int. coach 3 axle 2)	TrackID	-109.005	-108.995	17000							
26	Vertical (Int. coach 4 axle 1)	TrackID	-107.005	-106.995	17000							
27	Vertical (Int. coach 4 axle 2)	TrackID	-91.005	-90.995	17000							
28	Vertical (Int. coach 5 axle 1)	TrackID	-89.005	-88.995	17000							
29	Vertical (Int. coach 5 axle 2)	TrackID	-73.005	-72.995	17000							
30	Vertical (Int. coach 6 axle 1)	TrackID	-71.005	-70.995	17000							
31	Vertical (Int. coach 6 axle 2)	TrackID	-55.005	-54.995	17000							
32	Vertical (Int. coach 7 axle 1)	TrackID	-53.005	-52.995	17000							
33	Vertical (Int. coach 7 axle 2)	TrackID	-37.005	-36.995	17000							
34	Vertical (Int. coach 8 axle 1)	TrackID	-35.005	-34.995	17000							
35	Vertical (Int. coach 8 axle 2)	TrackID	-19.005	-18.995	17000							
36	Vertical (Int. coach 9 axle 1)	TrackID	-17.005	-16.995	17000							
37	Vertical (Int. coach 9 axle 2)	TrackID	-1.005	-0.995	17000							
38	Vertical (Int. coach 10 axle 1)	TrackID	0.995	1.005	17000							
39	Vertical (Int. coach 10 axle 2)	TrackID	16.995	17.005	17000							
40	Vertical (Int. coach 11 axle 1)	TrackID	18.995	19.005	17000							
41	Vertical (Int. coach 11 axle 2)	TrackID	34.995	35.005	17000							
42	Vertical (Int. coach 12 axle 1)	TrackID	36.995	37.005	17000							
43	Vertical (Int. coach 12 axle 2)	TrackID	52.995	53.005	17000							
44	Vertical (Int. coach 13 axle 1)	TrackID	54.995	55.005	17000							
45	Vertical (Int. coach 13 axle 2)	TrackID	70.995	71.005	17000							
46	Vertical (Int. coach 14 axle 1)	TrackID	72.995	73.005	17000							
47	Vertical (Int. coach 14 axle 2)	TrackID	88.995	89.005	17000							
48	Vertical (Int. coach 15 axle 1)	TrackID	90.995	91.005	17000							
49	Vertical (Int. coach 15 axle 2)	TrackID	106.995	107.005	17000							
50	Vertical (Int. coach 16 axle 1)	TrackID	108.995	109.005	17000							
51	Vertical (Int. coach 16 axle 2)	TrackID	124.995	125.005	17000							
52	Vertical (Int. coach 17 axle 1)	TrackID	126.995	127.005	17000							
53	Vertical (Int. coach 17 axle 2)	TrackID	142.995	143.005	17000							
54	Vertical (Int. coach 18 axle 1)	TrackID	144.995	145.005	17000							
55	Vertical (Int. coach 18 axle 2)	TrackID	160.995	161.005	17000							
56	Vertical (Right end coach axle 1)	TrackID	162.995	163.005	17000							
57	Vertical (Right end coach axle 2)	TrackID	176.2325	176.2425	17000							
58	Vertical (Right end coach axle 3)	TrackID	178.2325	178.2425	17000							
59	Vertical (Right power car axle 1)	TrackID	181.7575	181.7675	17000							
60	Vertical (Right power car axle 2)	TrackID	184.7575	184.7675	17000							
61	Vertical (Right power car axle 3)	TrackID	195.7575	195.7675	17000							
62	Vertical (Right power car axle 4)	TrackID	198.7575	198.7675	17000							
63	Braking	TrackID	-198.7625	198.7625	15.09339035							
64												
65	Braking load UDL has been factored as total load over the 397.525 m trainset is 7950.5 kN (> 6000 kN limit for default UDL)											
66	Braking load UDL reduced to = 15.093390352808 kN/m											
67												
68												
69												
70	ACCELERATING HSLM-A1 TRAIN											
71	Vertical (Left power car axle 1)	TrackID	-198.7675	-198.7575	17000							
72	Vertical (Left power car axle 2)	TrackID	-195.7675	-195.7575	17000							

Figure 166: Select the Braking (or Acceleration) Loading to be Copied

3) Select the first **Loading Type** cell of the Train Loading Group which the HSLM-A1 trainset is to be placed in and choose **Paste Values** to only paste the data and not any formatting.

Vertical (Left power car axle 1)									
Loading									
Units: Temperature: Celsius, Load Position/Length: m, Load: kN/m									
Temperature Loads									
Amount									
Concrete Deck									
Steel Deck									
User Deck									
Rails									
Number of Train Loading Groups to Analyse									
Train Loading Group: 1									
Number of Track Loading Locations									
Loading Type									
Track Selection to be Loaded									
Parametric Starting Position for Loadings									
Parametric End Position for Loadings									
Amount (per unit length)									
Loaded Length									
Starting Location of Loading for First Analysis									
Finishing Location of Loading for Last Analysis									
Location Increment for each Analysis									
Num Load									
Train Loads									
Vertical (Left power car axle 1) TrackID	-198.7675	-198.7675	17000	0.01					
Vertical (Left power car axle 2) TrackID	-195.7675	-195.7675	17000	0.01					
Vertical (Left power car axle 3) TrackID	-184.7675	-184.7675	17000	0.01					
Vertical (Left power car axle 4) TrackID	-181.7675	-181.7675	17000	0.01					
Vertical (Left end coach TrackID	-178.2425	-178.2325	17000	0.01					
Vertical (Left end coach TrackID	-176.2425	-176.2325	17000	0.01					
Vertical (Left end coach TrackID	-163.005	-162.995	17000	0.01					
Vertical (Int. coach 1 axle TrackID	-161.005	-160.995	17000	0.01					
Vertical (Int. coach 1 axle TrackID	-145.005	-144.995	17000	0.01					
Vertical (Int. coach 2 axle TrackID	-143.005	-142.995	17000	0.01					
Vertical (Int. coach 2 axle TrackID	-127.005	-126.995	17000	0.01					
Vertical (Int. coach 3 axle TrackID	-124.005	-123.995	17000	0.01					

Figure 167: Paste the HSLM-A1 Trainset Definition into the Loading Worksheet

- 4) Change the **TrackID** in the **Track Selection to be Loaded** column to represent the track that the HSLM-A1 trainset is to be passed along
- 5) Define the movement of the HSLM-A1 trainset loading across the structure (noting that the origin is at the centre of the loading pattern)
- 6) If any further trainsets are to be applied another track within the same Train Loading Group then define these below the loading that has just been defined.



Note. The principles applied here for the definition of the HSLM-A trainset loads for the Rail Track Analysis tool can be applied to other trainset configurations that include concentrated loads or can be defined in a parametric way. A single VBScript could be written which defined a range of trainsets by having different subroutines to just the writeHSLMATrain() subroutine or having a single common definition processing subroutine which tabulates the loading using internally defined arrays holding the loading defined by multiple trainset creation subroutines. This is, however, beyond the scope of this demonstration example.

VBScript Source Code for “Define_HSLM-A_for_RTA.vbs”

The following VBScript source code performs the definition of the HSLM-A TAB delimited files containing the loading configuration in accordance with the following assumptions:

- The braking trainset load definition assumes that the HSLM-A train is moving from left to right, the accelerating trainset load definition assumes that the HSLM-A train is moving from right to left (these can be changed by simply reversing the sign of the longitudinal loading values)
- Traction loads are applied as a UDL between the front and back axles of each of the power cars only. If the maximum load of 1000kN stated in Clause 6.5.3 of BS EN 1991-2:2003 is exceeded the loading is factored to ensure only 1000kN is defined
- Braking loads are applied as a UDL over the whole length of the trainset between the first and last axles. If the maximum load of 6000kN stated in Clause 6.5.3 of BS EN 1991-2:2003 is exceeded the loading is factored to ensure only 6000kN is defined
- The point loads are defined as equivalent UDLs using a user defined contact length (default = 0.01m)
- The origin of the HSLM-A trainset is defined at the centre of the trainset configuration when specifying the locations for the trainset across the embankments and structure
- The units are kN and m in accordance with the input requirements of the Rail Track Analysis tool.

This source code is also available from the LUSAS User Area on the website.

```
$ENGINE=VBSCRIPT
'
' Simple VBScript to define the HSLM-A EuroCode train loads for the RTA tool
' using a user-defined contact length for each point load / axle. The braking
' train is travelling in the positive (to right in RTA model) direction and
' the accelerating train is travelling in the negative (to the left in the RTA
' model) direction. To change the directions the signs of the braking and
' traction loads just need to be reversed.
'
' This defines the loads in a TAB delimited file which can be imported into
' a spreadsheet editor and the data then copied and pasted into the Loading
' worksheet of the RTA input spreadsheet.
'
' NOTE: This VBScript is provided AS-IS based on the assumption that the
' traction loads are applied as a UDL over the length between the first
' and last axles of the powercars and the braking loads are applied as a
' UDL over the entire length of the trainset axles (and factored to ensure
' that the BrakingLoad <= 6000 kN condition is satisfied).
'
' Vertical point / axle loads for the HSLM-A trainsets are applied as a
' UDL over the contact length defined by the user and it is up to the user
' to ensure that this contact length is appropriate. The magnitude of the
```

```
'      UDL is calculated as follows: UDL = PointForce / ContactLength
'
'      The origin of the HSLM-A loading is the middle of the trainset.
'
'      Units assumed are kN and m in accordance with the RTA tool.
'
'      This VBScript is not supported by LUSAS and it is up to the user to
'      decide that the assumptions above are correct.
'
' Dr. G.M.Paice, Project Leader, LUSAS, 14th February 2019
'=====
' HSLM-A id, 1 to 10
Dim HSLMA_ID
' Contact length for a point load / axle
Dim contactLength
' FileSystemObject
Dim fso
Set fso = CreateObject("Scripting.FileSystemObject")
' Output files
Dim outFile
Dim outFileName
' Dialog text
Const dialogTitle = "EuroCode HSLM-A Train Definition for RTA Tool"
Dim dialogInputText
' Current working directory (folder)
Dim CWD
CWD = getCWD() & "\"
' Flag for continuing
Dim contDefn
contDefn = True
'-----
' Get the HSLM-A train ID
errTxt = "The HSLM-A train ID must be an integer between 1 and 10"
dialogInputText = Trim(InputBox("Please enter the HSLM-A train ID (1 to 10):",
dialogTitle, "1"))
If Len(dialogInputText) > 0 Then
    If IsNumeric(dialogInputText) Then
        HSLMA_ID = CLng(dialogInputText)
        If HSLMA_ID < 1 Or HSLMA_ID > 10 Then contDefn = False
    Else
        contDefn = False
    End If
Else
    contDefn = False
End If
If Not contDefn Then
    Call MsgBox(errTxt, vbInformation + vbOKOnly, dialogTitle)
Else
    ' Get the contact length for the point/axle loads
    errTxt = "The contact length for the point/axle loads should be a positive
number and small"
    dialogInputText = Trim(InputBox("Please enter the contact length for the
point/axle loads:", dialogTitle, "0.01"))
    If Len(dialogInputText) > 0 Then
        If IsNumeric(dialogInputText) Then
            contactLength = CDBl(dialogInputText)
            If Not (contactLength > 0.0) Then contDefn = False
        Else
            contDefn = False
        End If
    Else
        contDefn = False
    End If
    If Not contDefn Then
        Call MsgBox(errTxt, vbInformation + vbOKOnly, dialogTitle)
    Else
```

```

' Get the output file (*.prn to match the spreadsheet input)
errTxt = "The output file should be a valid file with the *.prn extension
for import into the spreadsheet"
dialogInputText = Trim(InputBox("Please enter the file name for the
generated train loading (with *.prn extension):", dialogTitle, "HSLM-A" &
CStr(HSLMA_ID) & ".prn"))
If Len(dialogInputText) > 0 Then
    posPrn = InStrRev(dialogInputText, ".prn", -1, 1)
    If posPrn <> (Len(dialogInputText) - 3) Then
        contDefn = False
    Else
        outFileName = dialogInputText
    End If
Else
    contDefn = False
End If
If Not contDefn Then
    Call MsgBox(errTxt, vbInformation + vbOKOnly, dialogTitle)
Else
    ' Open the output file
    Set outFile = fso.CreateTextFile(CWD & outFileName, True)
    ' Define the HSLM-A train within the file
    Call writeHSLMATrain(outFile, HSLMA_ID, contactLength)
    ' Close the output file
    Call outFile.Close()
    Set outFile = Nothing
End If
End If
End If

Sub writeHSLMATrain(fileObj, trainID, contLen)
'Purpose
' Defines and writes the HSLM-A train data to the file using TAB delimited
' format.
'Externals
' fileObj -File object
' trainID -HSLM-A train ID (1-10)
' contLen -Contact length to be used for defining the point/axle loads
'History
' Name Date      Comment
' GP   14Feb19 Initial coding
'Internals
' axleCoord      -Coordinates for the axles defining the HSLM-A trainset
' axleDesc       -Axle description
' bogieAxle      -Bogie axle spacing for each HSLM-A trainset
' brakLoadLen    -Braking loaded length (overall axles for the trainset)
' brakTotLoad    -Braking total load
' brakUDL        -Braking load UDL after factoring for the trainset length
' coachLen       -Coach lengths for each HSLM-A trainset
' curAxleID      -Current axle ID being defined
' endCoachSpc    -Spacing between the 2nd and 3rd end coach axles
' equivVertUDL   -Equivalent vertical UDL for the point / axle load over the contact
length
' nCoaches       -Number of intermediate coaches for each HSLM-A trainset
' pointForce     -Point / axle force for each HSLM-A trainset
' powerCarBog    -Spacing between the axles of the power car bogies
' powerCarSpc    -Spacing between the 2nd and 3rd power car axles
' powerEndSpc    -Spacing between the last power car and the 1st end coach axle
' totNumAxles    -Total number of axles for defining the HSLM-A trainset
' tracBack       -Coordinate of the back of the traction loads for the power car
' tracFront      -Coordinate of the front of the traction loads for the power car
' tracLenPwr     -Length of the traction load for each power car
' tracTotLoad    -Traction total load
' tracUDL        -Traction load UDL after any factoring for power car length
'-----
    Dim axleCoord

```

```
Dim axleDesc
Dim brakLoadLen
Dim brakUDL
brakUDL = 20.0
Dim curAxleID
Dim endCoachSpc
Dim equivVertUDL
Const powerCarBog = 3.0
Const powerCarSpc = 11.0
Const powerEndSpc = 3.525
Dim totNumAxles
Dim tracBack
Dim tracFront
Const tracLenPwr = 17.0
Dim tracTotLoad
Dim tracUDL
tracUDL = 33.0
' NOTE: The N number of intermediate coaches can be odd or even, therefore for
' simplicity we will initially define the point/axle loads with the origin
' at the left extent of the trainset before shifting them to be centred.
'
' In the zero-based arrays below, the index is the HSLM-A train ID minus 1
'
' Number of intermediate coaches, N
Dim nCoaches(9)
nCoaches(0) = 18
nCoaches(1) = 17
nCoaches(2) = 16
nCoaches(3) = 15
nCoaches(4) = 14
nCoaches(5) = 13
nCoaches(6) = 13
nCoaches(7) = 12
nCoaches(8) = 11
nCoaches(9) = 11
' Coach length, D (m)
Dim coachLen(9)
coachLen(0) = 18.0
coachLen(1) = 19.0
coachLen(2) = 20.0
coachLen(3) = 21.0
coachLen(4) = 22.0
coachLen(5) = 23.0
coachLen(6) = 24.0
coachLen(7) = 25.0
coachLen(8) = 26.0
coachLen(9) = 27.0
' Bogie axle spacing, d (m)
Dim bogieAxle(9)
bogieAxle(0) = 2.0
bogieAxle(1) = 3.5
bogieAxle(2) = 2.0
bogieAxle(3) = 3.0
bogieAxle(4) = 2.0
bogieAxle(5) = 2.0
bogieAxle(6) = 2.0
bogieAxle(7) = 2.5
bogieAxle(8) = 2.0
bogieAxle(9) = 2.0
' Point force, P (kN)
Dim pointForce(9)
pointForce(0) = 170.0
pointForce(1) = 200.0
pointForce(2) = 180.0
pointForce(3) = 190.0
pointForce(4) = 170.0
```

```

pointForce(5) = 180.0
pointForce(6) = 190.0
pointForce(7) = 190.0
pointForce(8) = 210.0
pointForce(9) = 210.0
' Calculate the equivalent UDL for spreading the point/axle load over the contact
length
equivVertUDL = pointForce(trainID - 1) / contLen
' Determine the number of axles that are required for defining the whole trainset.
' Trainset has 2 powercars + 2 end coaches + N * intermediate coaches
' Power cars have 4 axles each, end coaches have 3 axles each, intermediate coaches
have 2 axles each
totNumAxles = 2 * (4 + 3) + 2 * nCoaches(trainID - 1)
' Dimension the storage for the axles coordinates and descriptions
ReDim axleCoord(totNumAxles - 1)
ReDim axleDesc(totNumAxles - 1)
' Define the left powercar
axleCoord(0) = 0.0
axleDesc(0) = "Left power car axle 1"
axleCoord(1) = powerCarBog
axleDesc(1) = "Left power car axle 2"
axleCoord(2) = axleCoord(1) + powerCarSpc
axleDesc(2) = "Left power car axle 3"
axleCoord(3) = axleCoord(2) + powerCarBog
axleDesc(3) = "Left power car axle 4"
' Define the left end coach
axleCoord(4) = axleCoord(3) + powerEndSpc
axleDesc(4) = "Left end coach axle 1"
axleCoord(5) = axleCoord(4) + bogieAxle(trainID - 1)
axleDesc(5) = "Left end coach axle 2"
axleCoord(6) = (axleCoord(3) + axleCoord(4)) / 2.0 + coachLen(trainID - 1) -
bogieAxle(trainID - 1) / 2.0
axleDesc(6) = "Left end coach axle 3"
endCoachSpc = axleCoord(6) - axleCoord(5)
' Define the N intermediate coaches
curAxleID = 7
For icoach = 1 To nCoaches(trainID - 1)
curAxleID = curAxleID + 1
axleCoord(curAxleID - 1) = axleCoord(curAxleID - 2) + bogieAxle(trainID -
1)
axleDesc(curAxleID - 1) = "Int. coach " & CStr(icoach) & " axle 1"
curAxleID = curAxleID + 1
axleCoord(curAxleID - 1) = axleCoord(curAxleID - 3) + coachLen(trainID - 1)
axleDesc(curAxleID - 1) = "Int. coach " & CStr(icoach) & " axle 2"
Next
' Define the right end coach
curAxleID = curAxleID + 1
axleCoord(curAxleID - 1) = axleCoord(curAxleID - 2) + bogieAxle(trainID - 1)
axleDesc(curAxleID - 1) = "Right end coach axle 1"
curAxleID = curAxleID + 1
axleCoord(curAxleID - 1) = axleCoord(curAxleID - 2) + endCoachSpc
axleDesc(curAxleID - 1) = "Right end coach axle 2"
curAxleID = curAxleID + 1
axleCoord(curAxleID - 1) = axleCoord(curAxleID - 2) + bogieAxle(trainID - 1)
axleDesc(curAxleID - 1) = "Right end coach axle 3"
curAxleID = curAxleID + 1
axleCoord(curAxleID - 1) = axleCoord(curAxleID - 2) + powerEndSpc
axleDesc(curAxleID - 1) = "Right power car axle 1"
curAxleID = curAxleID + 1
axleCoord(curAxleID - 1) = axleCoord(curAxleID - 2) + powerCarBog
axleDesc(curAxleID - 1) = "Right power car axle 2"
curAxleID = curAxleID + 1
axleCoord(curAxleID - 1) = axleCoord(curAxleID - 2) + powerCarSpc
axleDesc(curAxleID - 1) = "Right power car axle 3"
curAxleID = curAxleID + 1
axleCoord(curAxleID - 1) = axleCoord(curAxleID - 2) + powerCarBog

```

```

    axleDesc(curAxleID - 1) = "Right power car axle 4"
' Determine the total length for the braking load and echo the length
    brakLoadLen = axleCoord(totNumAxles - 1)
    Call getTextWindow.writeLine("Braking loads will be defined over a total length
of " & CStr(brakLoadLen) & " (and factored to ensure limit is observed)")
' Determine if the braking load needs to be scaled (most likely)
    brakTotLoad = brakUDL * brakLoadLen
    If brakTotLoad > 6000.0 Then
        brakUDL = brakUDL * 6000.0 / brakTotLoad
        Call getTextWindow.writeLine("Braking load UDL has been factored as " &
CStr(brakTotLoad) & " > 6000 kN for default UDL")
    End If
    Call getTextWindow.writeLine("Braking load UDL = " & CStr(brakUDL) & " kN/m")
' Shift the axles
    Dim shiftAxles
    shiftAxles = axleCoord(totNumAxles - 1) / 2.0
    For iaxle = 0 To totNumAxles - 1
        axleCoord(iaxle) = axleCoord(iaxle) - shiftAxles
    Next
' Determine the coordinates for the power car traction loads and report the lengths
    tracFront = axleCoord(totNumAxles - 1)
    tracBack = axleCoord(totNumAxles - 4)
    Call getTextWindow.writeLine("Traction loads will be defined for each power car
length of " & CStr(tracLenPwr) & " for both leading and trailing power cars")
' Determine if the traction load for the two power cars needs to be scaled
    tracTotLoad = 2.0 * tracUDL * tracLenPwr
    If tracTotLoad > 1000.0 Then
        tracUDL = tracUDL * 1000.0 / tracTotLoad
        Call getTextWindow.writeLine("Traction load UDL has been factored as " &
CStr(tracTotLoad) & " > 1000 kN for default UDL")
    End If
    Call getTextWindow.writeLine("Traction load UDL = " & CStr(tracUDL) & " kN/m")
' Let us now write out the information to the file
    Call fileObj.writeLine("This TAB delimited file defines the HSLM-A" &
CStr(trainID) & " train definitions for a braking train travelling in the positive
(to the right) direction in the RTA model")
    Call fileObj.writeLine("and an accelerating train travelling in the negative
(to the left) direction in the RTA model.")
    Call fileObj.writeLine("")
    Call fileObj.writeLine("The vertical and braking loads for the braking train
are defined first, followed by the vertical and traction loads for the accelerating
train.")
    Call fileObj.writeLine("After importing into the spreadsheet the appropriate
loads for the analysis being considered can be copied and pasted into the input
spreadsheet.")
    Call fileObj.writeLine("")
    Call fileObj.writeLine("Contact length for point/axle loads = " &
CStr(contLen))
    Call fileObj.writeLine("Origin for loading is the middle of the trainset.")
    Call fileObj.writeLine("")
    Call fileObj.writeLine("")
    Call fileObj.writeLine("")
    Call fileObj.writeLine("BRAKING HSLM-A" & CStr(trainID) & " TRAIN")
    For iaxle = 0 To totNumAxles - 1
        Call fileObj.writeLine("Vertical (" & axleDesc(iaxle) & ") " & Chr(9) &
"TrackID" & Chr(9) & CStr(axleCoord(iaxle) - contLen / 2.0) & Chr(9) &
CStr(axleCoord(iaxle) + contLen / 2.0) & Chr(9) & CStr(equivVertUDL))
    Next
    Call fileObj.writeLine("Braking" & Chr(9) & "TrackID" & Chr(9) &
CStr(axleCoord(0)) & Chr(9) & CStr(axleCoord(totNumAxles - 1)) & Chr(9) &
CStr(brakUDL))
    Call fileObj.writeLine("")
    If brakTotLoad > 6000.0 Then Call fileObj.writeLine("Braking load UDL has been
factored as total load over the " & CStr(brakLoadLen) & " m trainset is " &
CStr(brakTotLoad) & " kN (> 6000 kN limit for default UDL)")

```

```
Call fileObj.WriteLine("Braking load UDL reduced to = " & CStr(brakUDL) & "
kN/m")
Call fileObj.WriteLine("")
Call fileObj.WriteLine("")
Call fileObj.WriteLine("")
Call fileObj.WriteLine("ACCELERATING HSLM-A" & CStr(trainID) & " TRAIN")
For iaxle = 0 To totNumAxles - 1
    Call fileObj.WriteLine("Vertical (" & axleDesc(iaxle) & ") " & Chr(9) &
"TrackID" & Chr(9) & CStr(axleCoord(iaxle) - contLen / 2.0) & Chr(9) &
CStr(axleCoord(iaxle) + contLen / 2.0) & Chr(9) & CStr(equivVertUDL))
Next
Call fileObj.WriteLine("Traction (Left power car)" & Chr(9) & "TrackID" &
Chr(9) & CStr(-tracFront) & Chr(9) & CStr(-tracBack) & Chr(9) & CStr(tracUDL))
Call fileObj.WriteLine("Traction (Right power car)" & Chr(9) & "TrackID" &
Chr(9) & CStr(tracBack) & Chr(9) & CStr(tracFront) & Chr(9) & CStr(tracUDL))
Call fileObj.WriteLine("")
If tracTotLoad > 1000.0 Then Call fileObj.WriteLine("Traction load UDL has been
factored as total load over the two " & CStr(tracLenPwr) & " m power cars is " &
CStr(tracTotLoad) & " kN (> 1000 kN limit for default UDL)")
Call fileObj.WriteLine("Traction load UDL reduced to = " & CStr(tracUDL) & "
kN/m")
End Sub
```

References

- B1 BS EN 1991-2:2003 Eurocode 1: Actions on structures - Part 2: Traffic loads on bridges

Appendix C:

Calculation of Deck Displacements at Alternative Locations to Top of Slab / Deck

Introduction

The finite element modelling of the deck is carried out with the elements / nodal line along the top of the slab / at the location where the track-structure-interaction occurs to ensure that this track-structure-interaction behaviour is modelled correctly in the analyses. The behaviour of the deck itself is modelled through eccentricity in the beam elements with rigid offsets at the support locations to ensure that the support conditions / bearings are at the correct elevations and the overall bending behaviour of the decks is accurate.

As a result of the requirements of the track-structure-interaction the deck displacement results in the post-processing are output at the top of the slab / at the location of the track-structure-interaction. It is however possible to obtain the displacements at other locations such as the neutral axis and the bottom of the slab / section through basic calculation methods which will be highlighted below.

Calculation of Displacements / Rotation at Alternative Locations

The calculations require the following assumptions:

- ❑ Plane sections remain plane under bending
- ❑ Rotations are small

Considering the behaviour at the end of a deck as illustrated in Figure 168, from the post-processor we have the displacements and rotation (dx_T, dy_T, θ_T) at the top of slab/deck and we will also have its coordinates (x_T, y_T). The only additional piece of information we need to calculate the alternative displacements and rotation is the location within the section that the calculation is to be performed at. In Figure 168 two locations are illustrated, the neutral axis by a depth D_{NA} from the top and the overall Depth of Section by a depth D .

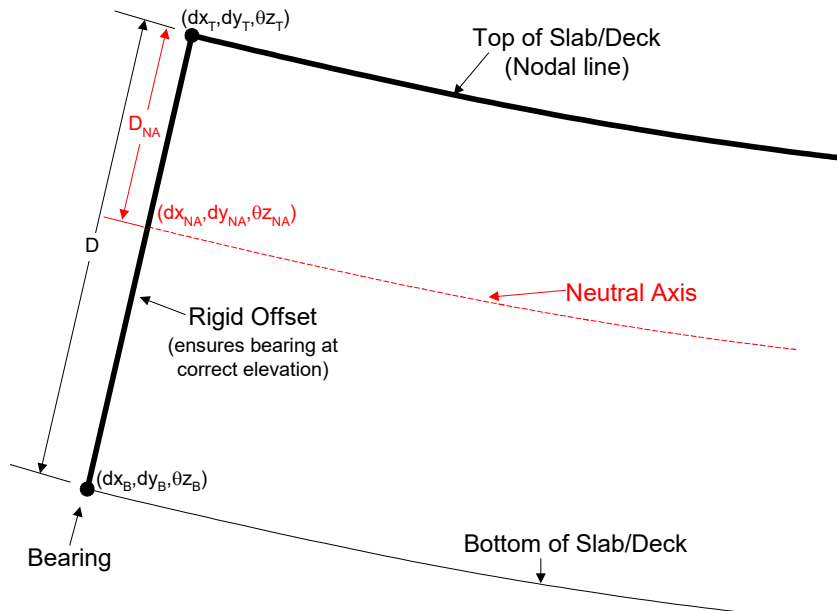


Figure 168: Illustration of Deck at Bearing (Bold Lines Represent Modelling)

Within the rail track analysis tool the rigid support offsets are all built vertically so the coordinates of the location of interest can easily be calculated since the X-coordinate of the location of interest will be identical to the X-coordinate of the top of the slab / deck and the Y-coordinate will just be the required depth from the top of the slab / deck:

$$x_{\text{Depth}} = x_T$$

$$y_{\text{Depth}} = y_T - \text{Depth}$$

To calculate the displacements for the location of interest we need to obtain the deformed coordinates of this location. First of all we need to know the deformed coordinates of the top of the slab / deck:

$$x_{T(\text{deformed})} = x_T + dx_T$$

$$y_{T(\text{deformed})} = y_T + dy_T$$

We can now calculate the deformed coordinates of the location of interest (noting the assumptions):

$$x_{\text{Depth}(\text{deformed})} = x_{T(\text{deformed})} + \text{Depth} * \sin(\theta_{z_T})$$

$$y_{\text{Depth}(\text{deformed})} = y_{T(\text{deformed})} - \text{Depth} * \cos(\theta_{z_T})$$

We can now calculate the displacements and rotation for the location of interest:

$$dx_{\text{Depth}} = x_{\text{Depth}(\text{deformed})} - x_{\text{Depth}}$$

$$dy_{\text{Depth}} = y_{\text{Depth}(\text{deformed})} - y_{\text{Depth}}$$

$$\theta_{z_{\text{Depth}}} = \theta_{z_T}$$

These calculations for the displacements and rotation can be reduced to:

$$dx_{\text{Depth}} = x_T + dx_T + \text{Depth} * \sin(\theta_{z_T}) - x_T$$

$$= dx_T + \text{Depth} * \sin(\theta_{z_T})$$

$$dy_{\text{Depth}} = y_T + dy_T - \text{Depth} * \cos(\theta_{z_T}) - (y_T - \text{Depth})$$

$$= dy_T + \text{Depth} * (1 - \cos(\theta_{z_T}))$$

$$\theta_{z_{\text{Depth}}} = \theta_{z_T}$$

From an analysis the following displacements / rotations were obtained:

	DX[m]	DY[m]	THZ[rad]
Top of slab	-1.00273097E-02	-1.21738413E-06	-2.22602390E-04
Bottom of slab	-1.06951168E-02	-1.12373920E-06	-2.22602390E-04

Table 5: Sample Top and Bottom of Slab Displacement Results for 3m Deep Section

The bottom of slab displacements can be calculated from the top of slab using the equations above as follows and utilising the knowledge that the Depth of Section is 3.0m:

$$\begin{aligned}
 dx_B &= dx_T + D * \sin(\theta_{z_T}) \\
 &= -1.00273097E-02 + 3.0 * \sin(-2.22602390E-04) \\
 &= -1.06951168E-02 \text{ m} \\
 dy_B &= dy_T + \text{Depth} * (1 - \cos(\theta_{z_T})) \\
 &= -1.21738413E-06 + 3.0 * (1 - \cos(-2.22602390E-04)) \\
 &= -1.14305640E-06 \text{ m} \\
 \theta_{z_B} &= \theta_{z_T} = -2.22602390E-04 \text{ radians}
 \end{aligned}$$

The values for dx_B and θ_{z_B} agree exactly with the values in the table, the value for dy_B is within about a percent (it differs very slightly because the 'rigid' offset is not infinitely stiff in the model). It should however be noted that the magnitude of the vertical displacements are of the order of $1.0E-6$ m so they are insignificant in terms of the scale of the longitudinal (dx) displacement results in the analysis.

If instead of the bottom of the slab / section, if we wished to calculate the displacements at another location such as the neutral axis of the deck section then all that is needed is to substitute the depth in the calculation with the depth D_{NA} .



Note. The displacements and rotation at the ends of decks / support / bearing locations can also be obtained directly out of Modeller from the results loadcases by manually post-processing the rail track analysis. This can be done by inspecting the displacement results for the **Support Offsets** group in the **Groups** treeview alone for the model. This **Support Offsets** group contains all of the rigid offsets used to ensure that the supports/bearings are at the correct elevations for the decks of the structure and extraction of the displacements (DX, DY) / rotation (THZ) from the model for the bottom node will generally provide the results at the support / bearing elevation.



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